MODELING DIMINISHING MARGINAL RETURNS: AN APPLICATION TO THE AIRCRAFT AVAILABILITY MODEL

THESIS

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AFIT/GOA/ENS/96M-10

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THESIS

Presented to the Faculty of the School of Engineering of the Air Force Institute of Technology

Air University

In Partial Fulfillment of the

Requirements for the Degree of

Master of Science in Operations Research

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March 1996

Approved for public release; distribution unlimited

THESIS APPROVAL

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THESIS TITLE: Modeling Diminishing Marginal Returns: An Application to the

Aircraft Availability Model

DEFENSE DATE: 22 February 1996

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Acknowledgments

This thesis topic originated in the mind of the author in the weight room of the Wright Field Fitness Center in Area B of Wright-Patterson Air Force Base. Without a dedication to healthy living by two Air Force Officers the effort as presented here may have never found its start in the Summer of 1995.

I would like to thank my powerful advisorship, Major Lee Lehmkuhl and Dr.

Richard Deckro, for motivating and supporting the completion of this incredible endeavor.

Mr. Fred Rexroad made this effort possible through his greatly appreciated support and input. His AAM expertise and insight (not to mention data) made those model formulations found here possible.

The only way I kept my sanity throughout this process was with the undying love and support of my beautiful wife and the 45 holes of golf located on Wright-Patterson Air Force Base.

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Abstract

The Aircraft Availability Model (AAM) provides the Air Force with a worldwide peacetime requirement for reparable spare parts. Reparable spares are a critical cost area for the Air Force with an average annual budget of one billion dollars. This research models AAM methodology as it relates to the concept of diminishing marginal returns in resource application. Three separate modeling techniques are investigated with the goal of reformulating the AAM as a mathematical programming model that provides a comparable solution and a capable tool for the conduct of sensitivity analysis.

The general formulations presented here are continuous non-linear, continuous linear, and piecewise linear discrete/continuous models. Two formulations of the piecewise linear discrete/continuous model are presented. The piecewise linear model based on AAM sort values shows the dominance of an optimization routine relative to the AAM shopping list greedy heuristic. Research shows that the optimization algorithm provides the greatest improvement to mission design series (MDS) availability per dollar spent. The piecewise linear model based on availability rates provides the capability to maximize the MDS availability level. It has the potential to obtain the highest possible MDS availability relative to reparable spares inventory levels. This mathematical model is discussed in complete detail as a robust platform for conducting extensive post-optimality analysis.

MODELING DIMINISHING MARGINAL RETURNS: AN APPLICATION TO THE AIRCRAFT AVAILABILITY MODEL

I. Introduction

Background

The Air Force Materiel Command implemented the Aircraft Availability Model (AAM) to determine its safety level for reparable items in the Spring of 1988. Reparable spares are a critical cost area for the Air Force with an average annual budget of one billion dollars. The AAM provides the Air Force with a predetermined level of support at the lowest cost (Rexroad, 1992:1). The goal of the model is to minimize procurement costs while achieving a required end item availability target. The model determines system availability based on an established stock level of line-replaceable-units (LRUs). LRUs are defined as those items that can be removed and replaced directly on the aircraft while it remains on the flight line. If an LRU is "down" and there is no spare to replace it, the aircraft is not available. Therefore, these LRUs are a primary contributor to aircraft availability.

The basic mathematical approach of the AAM involves the computation of each item's contribution to system availability. Factors included in the model are the quantity of the item used on each aircraft, the proportion of aircraft in the inventory that contain the item, the number of aircraft being modeled, and the expected back order (EBO) value for the LRU. Each item's number of spares, or stock level, determines its EBO value.

System availability is simply the product of the computed item availability of those parts on the aircraft (Rexroad, 1982:5,6).

The AAM determines which parts to purchase and the order of these purchases based on a sort value. Each part is ranked according to the amount of improvement to aircraft availability the next unit of inventory will provide per unit price. The concept behind this marginal approach is to spend the next dollar on that part which provides the most improvement to system availability. This method provides the decision maker with a shopping list of those items which provide the most improvement to availability per dollar spent. Parts can be procured until funding is depleted or until the target availability value is reached.

The AAM provides a somewhat limited capability to conduct sensitivity, or "whatif" analysis. The model's current output only allows a decision maker to determine the
impact of his or her procurement policies on availability goals and funding levels, since
other issues are not represented in the model. An alternate formulation that captures the
intent of the AAM while providing the capability for in-depth sensitivity analysis would
prove valuable to a decision maker.

Statement of the Problem

The purpose of this research is to develop a reformulation of the AAM that provides a comparable solution to the current model while adding the capability to conduct relevant sensitivity analysis.

Research Approach

Each item's availability function demonstrates the principle of diminishing marginal returns. As the number of parts in inventory increases, a point is reached where the next part procured does not provide as much improvement in availability as the last. It is possible to determine the stock level required to realize this condition. This level represents the lower bound stock level for each unit. At the same time, it is possible to determine the level where the next item procured provides a negligible increase to system availability per dollar spent, a legitimate upper bound on the stock level.

Using AAM output data, these bounds can be explicitly defined. The output data provides the capability to construct a mathematical program that achieves an optimal solution comparable to that obtained by the AAM. Enrichment of this mathematical program to include additional constraints provides insight to the sensitivity of the model's optimal procurement plan to outside influences. The research will explore the ability of various mathematical modeling techniques such as continuous nonlinear programming, continuous linear programming, and piece-wise linear discrete/continuous programming to capture the impact of the diminishing marginal returns in a well defined region.

Scope

This study provides a general modeling approach that can be applied to any weapon system under consideration. Research focuses on a specific aircraft (the F-15E) based on AAM output relative to that aircraft. The result is a model representing those factors considered important to the modeled weapon system's availability. This basic

framework provides the methodology required to apply equivalent techniques to other systems modeled by the AAM.

II. Literature Review

Overview

A reformulation of the AAM requires a comprehensive understanding of the model. This literature review provides the historical aspects of the model, including its relation to the Multi-Echelon-Technique-for-Recoverable-Item-Control (METRIC) family of spares models and the AAM's development. A discussion of the conceptual framework and mathematical basis of the AAM is included in this section. A review of current literature provides insight into inventory modeling based on its application to model building and constraints, including the use of reparable part models in industry. Finally, the concept of diminishing marginal returns is reviewed and applied to the alternate form of the AAM.

The METRIC Family of Models

The AAM is part of a family of Reparable Item Inventory Models based on the METRIC philosophy used by the United States Air Force. Other related models include the METRIC model, Mod-METRIC, Vari-METRIC, Dyna-METRIC, and the Aircraft Sustainability Model (ASM). In general, each of these models is constructed to minimize expected backorders or maximize aircraft availability. Each of these models assumes independent demand for parts; that is, the failure of any given part is assumed to have no influence on the status of any other parts. The METRIC family of models is then divided into two major categories: those that model stationary demand and those that model dynamic demand. Stationary demand models assume that the distribution of demand for

parts over some future time period is constant. The dynamic demand models provide the capability of modeling varying distributions of demand that may occur during contingency operations. Figure 2-1 illustrates the development of the METRIC family of reparable item inventory models.

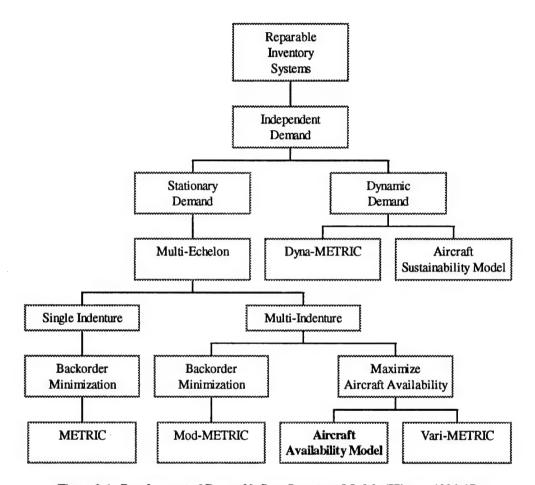


Figure 2-1. Development of Reparable Item Inventory Models (Klinger, 1994:15)

The AAM falls into the stationary demand class of METRIC models. This study is therefore focused in that area.

METRIC Development

A cornerstone of reparable item inventory theory is Palm's Theorem. This theorem enables the estimation of the steady state probability distribution of the number

of units in repair from the probability distribution of the demand process and the mean of the repair time distribution (Sherbrooke, 1992:21).

PALM'S THEOREM: If demand for an item is a Poisson process with annual mean m and if the repair time for each failed unit is independently and identically distributed according to any distribution with mean T years, then the steady-state probability distribution for the number of units in repair has a Poisson distribution with mean mT (Sherbrooke, 1992:21).

Palm's Theorem makes it unnecessary to measure the shape of the repair distribution. For any specified mean time T, regardless of the distribution, the steady state probability distribution for the number of units in repair is Poisson with mean mT (Sherbrooke, 1992:21).

The basis for the METRIC family of models is a mathematical theory that considers the multi-echelon and multi-indenture supply system of reparable parts used by the U.S. Air Force. The multi-echelon element of the supply system represents multiple levels of supply and repair. METRIC and the AAM model the base and depot levels of the hierarchy. Base level supply maintains those items that are immediately available upon a given demand. Base level repair handles those items that can be repaired without the need for extensive overhaul or rework. The depot maintains a supply of reparable units for any number of subordinate bases, thus it is an upper echelon element of the supply system. At the same time depot level repair operates at an upper echelon, conducting major repair and overhaul for those units received from its subordinate bases. The concept of multi-indentured parts breaks down units based on their relationship to the operational end item. The AAM defines operational end items as mission designs (MD) or mission design systems (MDS). (These are discussed in detail later.) First indenture

items, or line replaceable units (LRU), are those units that are essential to the operation of the MD. If a first indenture item is down the MD is unavailable. Second indenture items are subunits of first indenture items, third indenture items are subunits of second indenture items, and so on. The status of units at each level of indenture effects the availability of the next higher assembly in the chain of indentured items (O'Malley, 1983:6-3).

The problem environment at its most basic level involves the diagnosis of a malfunction on an aircraft. Once determined, the malfunctioning item is removed from the aircraft and brought into base supply. If a spare is available, it is issued and installed on the aircraft; otherwise a backorder is established for that aircraft. When a base backorder for a first indenture item is issued, the corresponding aircraft has a "hole" and is non-mission capable; it is unavailable for service. This is the extent of the first-indenture stock item scenario. The METRIC model extends only to second indenture items called shop replaceable units (SRU) and two echelons of supply and repair at the base and depot levels as described above (Sherbrooke, 1992:6).

METRIC theory utilizes a system approach aimed at confronting issues on a larger than item level. "In the system approach, questions are asked such as: How can we insure that 95% of our scheduled aircraft flights will not be delayed for lack of spare parts? How much more money do we need to move from 95% to something higher?" (Sherbrooke, 1992:2). The major purpose of the METRIC model is to determine optimal stock levels for each item, subject to a constrained budget or a specified level of system performance such as availability of mission capable aircraft (Sherbrooke, 1967:123).

The theory supporting this purpose involves the development of item and system performance measures. There are two principle measures of item performance: fill rate, the expected percentage of orders filled at the time of placement, and backorders, the expected number of unfilled requests for demand (Sherbrooke, 1992:24). Reparable spares provide the capability to fill a backorder with an item that has been repaired if there is not an item in resupply. The primary system performance measure used in the METRIC model is aircraft availability, the expected percentage of the fleet not down for spares at a random point in time (Sherbrooke, 1992:27).

Application of METRIC Theory in Literature

METRIC theory provides a robust framework upon which several reparable spares models have been based. The basic development tree was provided earlier in this review. A brief description of each model in it is provided here. (For a more in depth discussion of reparable spares modeling see Nahmias, 1981.) Nahmias discusses the significance of METRIC in the field of reparable spares modeling. He notes that METRIC "is important in that it appears to capture many of the significant features of the problem of determining suitable spares levels in a large-scale reparable item inventory system, and, as a result, it is one of the few multi-echelon inventory models to be implemented" (Nahmias, 1981:258). Some weaknesses with the underlying assumptions used in the development of METRIC resulted in the development of other models aimed at addressing some of these weaknesses.

One important element not explicitly accounted for in the METRIC formulation is the relationship of parts in the hierarchical structure, that is, the relationship of an end item to its components or subassemblies (Nahmias, 1981:2). Muckstadt developed the MOD-METRIC model for the explicit consideration of the hierarchical parts structure and it was subsequently implemented by the Air Force Materiel Command (Muckstadt, 1973:472).

METRIC assumes an infinite number of servers at the repair level. This results in the application of the model under steady state conditions (Nahmias, 1981:261).

Contingency or war-time operations are not considered under the steady state assumption, leading to the development of the real time METRIC model. This model does not assume first-in-first-out repairs at the depot. The order of depot repairs is determined by base demands generated by simple Poisson processes and repair times are assumed to be independent exponential random variables (Nahmias, 1981:265). The Aircraft Sustainability model is an extension of the AAM and considers contingency operations in its formulation. (For an in-depth discussion of the entire METRIC family of models see Klinger, 1994.)

This brief discussion of METRIC and related models illustrates the importance of the underlying theory and the interest in developing extensions to it with the goal of a deeper understanding of the development of an optimal inventory of reparable items.

AAM Background

In the early 1970s the Air Force established the need for an inventory parts procurement process that could provide a specified level of availability in a time of shrinking budgets. This requirement remains at the forefront of current planning in today's environment of decreased defense spending. The AAM computes the Air Force's

worldwide peacetime requirement for reparable spare parts. "It permits the Air Force to set availability goals by aircraft type and compute a worldwide requirement for reparable spare parts which will satisfy these goals at a minimum cost" (Rexroad, July 1992:1).

The AAM Environment

The AAM is focused on those weapon systems containing items with a forecasted level of demand. This allows the computation of availability based on the percentage of aircraft that contain a full set of such parts. Issues such as scheduled or unscheduled on-aircraft maintenance, shortages of nonreparable items, shortages of other types of reparable parts, and the consolidation of reparable item shortages (aircraft cannibalization) are not considered in the model formulation (Rexroad, July 1992:2). As mentioned previously, demand activity is assumed to be steady for reparable spare parts. This is not to say demand is constant but rather it is determined in a "steady state" peacetime environment without surge levels required during wartime operations (Rexroad, July 1992:2).

The model considers a number of different types of aircraft stationed at bases in locations throughout the world. Each Mission Design (MD) or aircraft (F-15 or KC-135, for example) or its associated Mission Design Series (MDS) or subtype (F-15E or KC-135R for example) is considered the end item of concern. These aircraft are supported by an inventory of reparable spare parts that are maintained at a specified stock level. In addition, bases have a limited repair capability that is augmented by depots, which are industrial facilities with extensive repair and overhaul capabilities (Rexroad, July 1992:2).

When a failure occurs on an aircraft, the cause of the failure is isolated to a single component which is then removed and replaced with a serviceable spare from the base inventory as soon as one is available. If base supply has a serviceable unit in the current inventory of spares, aircraft downtime is limited to the time for removal and replacement of the designated LRU. The faulty unit is then either repaired at the local maintenance facility or it is shipped to a depot for extensive repair and/or overhaul. If the part is shipped to a depot, a requisition is placed with the depot for the shipment of a serviceable unit to the base (Rexroad, July 1992:2). This scenario illustrates the first level of indenture in the supply system and is identical to that modeled by the METRIC model.

Base level repair of the failed LRU may identify a failed subassembly within the unit itself. As noted earlier, these subassemblies are designated Shop Replaceable Units (SRU) and are second indenture level items. The faulty SRU is removed from the LRU and replaced by a serviceable item in base supply when possible. SRUs that are unrepairable at the base level are sent to the higher echelon for repair. The AAM definition of a down aircraft is one where no spare is available for a failed LRU; the unfilled demand (back order) causes a "hole" on the aircraft. Lack of a spare SRU delays the repair of the LRU; however, if serviceable spares of the next higher assembly are available, there is no direct SRU effect on aircraft availability (Rexroad, July 1992:3). Calculation of Expected Back Orders

The AAM utilizes a measure of an aircraft's expected back orders (EBO) to calculate its availability. An EBO is defined as the time weighted unfilled user demands and is found using the following formula (Rexroad, July 1992:5).

$$EBO = \sum_{x>s} (x-s) p(x)$$

where,

- s is the stock level
- x is the number of units in resupply for that site
- p(x) is the probability of having x units in resupply given by a negative binomial probability distribution.

The AAM derives the mean of the negative binomial probability distribution, p(x), from the following component data elements:

- a. The base pipeline: the expected number of units in base repair or in transit from the depot to the base at a random point in time.
- b. The depot pipeline: the expected number of units in depot repair or in transit from the base to the depot at a random point in time.
- c. The number of bases at which demands for the component occur.
- d. The ratio of depot demands generated at the bases to total depot demands.
- e. The expected number of units condemned over the procurement lead time (Rexroad, July 1992:6).

These factors result in the calculation of the worldwide system EBO. This value includes EBOs as a result of both echelons of repair and resupply including stock levels and pipeline values at each level (Rexroad, June 1992:5).

The Negative Binomial Probability Distribution

Sherbrooke provides an in-depth analysis of the use of the negative binomial probability distribution (Sherbrooke, 1992: 60-62). He notes some important

characteristics of the distribution which make it a powerful tool in inventory modeling. The negative binomial distribution is a discrete distribution defined by two non-negative arguments which specify the number of trials and the probability of success. This distribution is a generalization of the Poisson distribution, thus Palm's Theorem is applicable. In addition, like the Poisson distribution, the negative binomial distribution maintains independent increments, meaning the number of demands in two nonoverlapping time periods is independent. The two parameters that define the negative binomial distribution can be estimated for a specified mean and a variance to mean ratio greater than one. These characteristics make the negative binomial distribution applicable to modeling the probability of x units in resupply as demonstrated by the AAM.

Calculation of Item Availability

The EBO for each part is dependent on the number of spares for that item and the number of that item in resupply. This value is then translated to an item availability, $q_{b(k),i,n}$, by the following formula:

$$q_{h(k),i,n} = (1 - b(h(k),i)) + b(h(k),i) \cdot \left[1 - \frac{U_{h(k),i}EBO_{i,n}}{T(h(k),i)}\right]^{a(h(k),i)}$$

where,

 $q_{h(k),i,n}$ = the probability that an aircraft of MDS h(k) is not missing a unit of component i with n spare units of component i in the system.

a(h(k),i) = the quantity per application (QPA) of component i and is the number of that item present on each aircraft.

b(h(k),i) = the future application percentage (FAP) and is the proportion of aircraft containing the item.

T(h(k),i) = the number of units of component i installed on aircraft of MDS h(k).

 $U_{h(k),i}$ = the prorating factor for MDS_{h(k)} and is given by

$$U_{h(k),i} = \frac{a(h(k),i) \cdot b(h(k),i) \cdot F_{h(k)}}{IP}$$

where IP =
$$\sum_{h=1}^{H} \sum_{k=1}^{K(h)} a(h(k), i) \cdot b(h(k), i) \cdot F_{h(k)}$$

 $F_{h(k)}$ is the flying hour program for MDS h(k) and IP is the total item program which is the number of flying hours accumulated by units of component i over all MDs (Rexroad, July 1992:26,27).

This formulation of item availability takes into consideration the sharing of components by the various MDs in the inventory by prorating the worldwide EBO for each part.

Calculation of Aircraft Availability

Aircraft availability, A_b, is defined, under the independence assumption, as the product of the LRU item availabilities:

$$\mathbf{A}_{h} = \prod_{i} \mathbf{q}_{h,i,n(i)} .$$

This value provides a system level availability rate and is dependent on the stock level of the various parts (Rexroad, July 1992:13). As stock levels increase so does availability, thus the AAM determines which parts to purchase to achieve a predetermined availability rate based on a sort value, defined in the next section.

Sort Values

Optimal purchasing decisions required to meet the predetermined availability rate are constrained by the MDS budget level and are chosen from the "shopping list." The "shopping list" is generated based on those parts which provide the greatest improvement to availability per dollar spent. This type of marginal analysis is achieved through the formulation of the AAM sort value. Sort values correspond to each potential stock level of an LRU. Sort values are found using the following formula:

sort value =
$$\frac{ln(q_{h,i,n+1}) - ln(q_{h,i,n})}{V_{h,i}C_i}$$

where C_i is the cost of a unit of component i and $V_{h,i}$ is a cost prorating factor that adjusts the full cost of common components to account for the benefit of sharing the spare among several aircraft types that use the same item. $V_{h,i}$ is found using the following formula which contains values defined previously.

$$V_{h,i} = \frac{\sum_{k=1}^{K(h)} a(h(k), i) \cdot b(h(k), i) \cdot F_{h(k)}}{IP}$$

This value is the same as the prorating factor used to prorate expected back orders, $U_{h(k),i}$, except in this case it is computed for the MD rather than the MDS. Thus, a spare unit of a common component has a sort value for each aircraft type. The AAM then prorates initialization costs to each of the using aircraft types and accumulates the component's contribution to each aircraft's starting availability rate (Rexroad, July 1992:27,28).

The availability curves are not independent of each other due to the common components across the several MDs. Buy decisions for one aircraft affect the availability of those aircraft that share common components. The AAM accounts for this situation by

calculating separate sort value arrays for each shared component relative to each aircraft type. Purchasing decisions are based on the distinct sort value arrays and the final stock level for a particular item may differ for the sharing aircraft. In this case an average buy quantity is determined and the resulting cumulative cost is divided among the sharing aircraft (Rexroad, July 1992:28,29).

Levels of Indenture

The AAM is a multi-echelon (base and depot levels are taken into consideration in the calculation of EBOs), multi-indenture model. To this point SRU modeling has been only briefly mentioned. The AAM definition of availability considers only the status of LRUs, so the impact of SRU stock levels must be determined to model the multi-indentured inventory system. SRU backorders lengthen repair times for LRUs, lowering the probability of a spare LRU being serviceable when demanded (Rexroad, July 1992:32). Figure 2-2 illustrates the effect of SRU backorders.

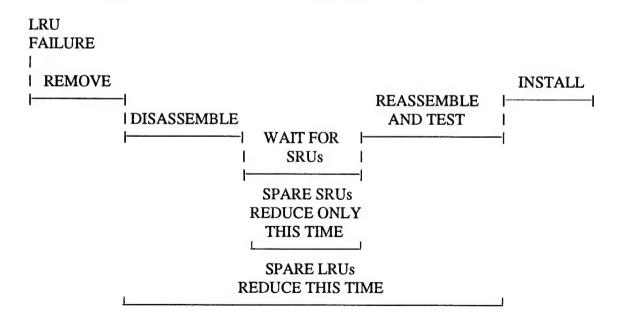


FIGURE 2-2. Levels of Indenture Repair Concept (Rexroad, July 1992:32)

Note the fact that spare LRUs have a direct impact on aircraft availability, while spare SRUs have an indirect impact measured as increased LRU repair time. SRUs are generally lower cost items so the purchase of a number of SRUs has an impact on the LRU EBO value. The impact of lower level items is measured with a recursive technique that begins at the lowest level of indenture. At each level the next higher assembly can be related in the same manner as the first indenture example between the aircraft and LRUs. The concept is to determine a number of subindentured items that are equivalent in price to the next higher assembly. Such an equivalent package of parts is termed an "Lsworth" (LRU's worth) of the component's subassemblies. It receives a sort value and is appropriately included on the optimal shopping list (Rexroad, July 1992:33). Just as the purchase of the next LRU increases aircraft availability, the purchase of an equivalent dollars worth of SRUs provides an improvement due to shorter repair time. If the SRU purchase shows a greater improvement in availability than the purchase of the next LRU, then the SRU package is purchased first.

Reparable Spares Modeling in the United States Navy and Army

The United States Navy (USN) designates items as either reparable or consumable. Consumable items are discarded when deemed no longer useful. Based on the economic value and the feasibility of repair some items are designated as reparable. Although reparable items account for only a small percentage of the total items stocked they account for more than half of the USN budget invested in spare parts. Considering this, research has been conducted to determine operating rules which will minimize the cost per unit time of operating the inventory portion of the reparable system (Schrady, 1967:392).

The USN "reparable system is comprised of three major organizations which maintain the reporting stock point, the user (non-reporting stock point), and the overhaul and repair (O&R) facility" (Schrady, 1967:391). Losses occur when failed items are discarded by the user (not returned to the O&R) and when the O&R cannot economically repair an item. These losses are replaced through the procurement of new items. An inventory of ready-for-issue (RFI) items, supplied by repair and procurement, as well as an inventory of non-ready-for-issue (NRFI) items awaiting for repair at the O&R must be managed. The system then is defined by two inventories, the primary having two input sources with different lead times and costs (Schrady, 1967:392).

The Navy model is deterministic and obtains economic order quantities for procurement and repair. Backorders are not permitted, reflecting the military objective of minimizing disservice as measured by shortages. The formulation treats the two inventories as interdependent parts of a total system, and jointly determines the optimal procurement and repair quantities (Schrady, 1967:392).

Two basic policies are investigated. One maintains the RFI inventory with items repaired in batches thus minimizing procurement activity and minimizing the NRFI inventory. O&R inducts a batch of failed items only when the NRFI inventory level reaches a defined "repair trigger." This type of deterministic system insures regularly spaced O&R inductions of fixed batch sizes resulting in an easy to implement procedure (Schrady, 1967:392). The second policy, the "substitution policy, supplies 100 percent of demand from repaired items until the supply of NRFI items decreases to a point where there are insufficient carcasses on hand to induct another batch. At this time, a

procurement quantity is received, and inductions are suspended. This second policy minimizes the RFI inventory (Schrady, 1967:393).

The United States Army (USA) approaches reparable spare inventory modeling in a manner similar to that of the USN. Hoekstra proposes two approaches to handling the problem. The first is similar to the first USN model described above. Two inventories, one of repaired items and the other of newly procured items, are managed separate from one another. Items are repaired in batches when an economic repair quantity is reached and an economic procurement quantity is purchased when the established reorder level is reached. This model is deterministic and calculates the optimal reorder level, procurement quantity, and repair quantity using traditional inventory equations (Hoekstra, 1966:378).

The second policy modeled is a look ahead policy. This model coordinates the actions of each stock manager. Each inventory position and update policy is based on a minimum repair quantity that is established to prevent a stock out position (Hoekstra, 1966:379). The proposed mathematics are not as straightforward as those for the two stock policy but the aim of this model is to more accurately portray the real system. Ultimately the USA built a computer simulation in the SIMSCRIPT simulation language to compare the performance of the proposed systems (Hoekstra, 1966:382).

Reparable Spares Modeling in Industry

The United States military is not alone in the modeling of reparable spares inventory levels. The concept of maintaining an optimal level of non-disposable, high value, repairable units is shared by other elements of industry. Extensive work in this area has been conducted by the American Airlines Decision Technologies division. American

manages its inventory of over 5,000 different types of repairable, or rotable, units supporting the operation of a fleet of over 400 aircraft with the use of a PC-based decision support system called Rotables Allocation and Planning System (RAPS). This system provides forecasts of rotable part demand, recommends least cost allocations of parts to airport locations, and calculates the availability level associated with the optimal allocation of each part (Tedone, 1989:61).

The American Airlines problem environment is very similar to that modeled by the family of METRIC models. Each operational aircraft is expected to have a complete complement of fully functional parts before departure. If a rotable part is found to be defective, the part is removed and replaced by a part in the local station stock room if possible. When a spare is issued from the local inventory, a message is sent to the repair facility or exchange base. The base maintains a supply of serviceable units available for use by the field stations. Upon receipt of the request the base ships an identical unit to the station while the station sends the faulty unit to the base for repair. Once repaired, the exchanged unit is placed in the inventory of the exchange base to begin the cycle again (Tedone, 1989:62). This scenario corresponds directly to the METRIC model's first level of supply indenture disregarding local repair capability.

American had been relying on a system developed in the late 1960s. After extensive research by the Decision Technologies and Materials Management divisions it was determined that the system needed to be updated. Their work culminated in the creation of RAPS.

The purpose of RAPS is not only to recommend allocations of spare parts, but to assist inventory managers and analysts in performing many other analyses relating to rotable part control, such as

- Determining the impact of new fleets on part allocations;
- Making surplus and purchase decisions;
- Evaluating vendor proposals and terms;
- Forecasting future demand; and
- Anticipating allocation behavior through sensitivity analyses.

The ultimate result of a RAPS run is a least-cost allocation of parts. The cost function consists of the sum of inventory ownership costs and expected shortage costs. The solution (allocation) that yields the minimum value of this function is very sensitive to many other quantities (Tedone, 1989:63,64).

The allocation of parts to the stations to satisfy expected demand at a minimum cost is the problem assigned to the American Airlines Materials Management department. One of their roles is to "distribute parts to stations in a cost-effective manner, balancing the cost of part ownership against the cost of part shortage while maintaining an acceptable level of availability. The problem is to find the allocation of least total cost" (Tedone, 1989:62).

RAPS requires a significant amount of data which is managed by a real-time computer system called the Rotable Control System (RCS). Each time a part is removed a tracking record is created that maintains the history of the broken unit from removal to repair as well as that of the serviceable part sent to replace it. Tracking data includes: transit and repair times, part removal histories, and current allocation levels. In addition, American maintains other corporate data bases containing part specific information (Tedone, 1989:62).

Calculation of part demand is critical to the model's formulation. Demand for all parts analyzed in the system is forecasted by a two step process. The first step is the calculation of total system demand across all stations. The distribution of this total demand among the stations is the second step of the process (Tedone, 1989:64).

Total expected system demand is calculated using a linear regression to establish a relationship between monthly part removals and various functions of monthly flying hours. A rolling 18-month history of removals and flying hours is updated on a monthly basis and a best fit regression is used to calculate the coefficients of the relationship. The second phase of the forecasting process distributes the system demand forecast among the individual stations. RAPS assigns a weight to each station that reflects the amount of expected station activity. Station activity is based on the numbers of departing and overnighting aircraft, the scheduled volume of maintenance checks of various levels, and each station's history of part removals (Tedone, 1989:64). At the same time a pattern of demand is established for the stations. Both the volume and this station pattern determine the level of availability, which is a major driver for the total cost of an allocation (Tedone, 1989:65).

The total cost of an allocation is defined as the sum of the inventory ownership cost and the expected shortage cost. Shortage costs are driven by the availability of parts since rotable parts are essential to the operation of the aircraft (much like LRUs are essential to the operation of an MDS). These costs are equivalent to the cost of a flight cancellation. "The cost of a flight cancellation is a highly volatile quantity which varies by fleet, time of day, passenger load, alternative flight availability, and many other factors. In extreme cases the intangible loss of goodwill is a large component of cost" (Tedone, 1989:65). The model uses a network optimization algorithm to select the least costly cycle of cancellations. Shortage costs for each fleet of aircraft are evaluated in that

manner. RAPS, like the AAM, then determines the optimal stock level of reparable parts that minimizes total system cost.

The American Airlines system illustrates a high level of capability that is not captured by current Air Force analyses. American's analysts are able to conduct extensive sensitivity analysis on a monthly basis. It is noted here that the data required for each RAPS run provides the capability to formulate those relationships that allow forecasts of the impact of current decisions. The effort and cost required for the Air Force to collect and maintain a data base similar to that maintained by American could outweigh the potential advantages of such a system. In addition, the Air Force has a larger system and serves more sights than American Airlines. A reformulation of current models such as the AAM, which is well established and understood, appears to provide a much more cost effective alternative for the conduct of effective sensitivity analyses.

Modeling Diminishing Marginal Returns

Current literature presents a series of modeling approaches for situations that demonstrate diminishing marginal returns. Diminishing marginal returns are defined as follows:

As the amount of a variable input utilized by an activity increases, with other inputs held constant, a point is reached where increases in that particular input results in a decreasing marginal increase in output. Output increases, but at an ever decreasing rate per additional unit of resource. Ultimately, the allocation of additional resources to the activity is not justified (Henderson and Quandt, 1971:57).

The AAM can be modeled to fit in this framework. The current formulation demonstrates the concept of diminishing marginal returns (as defined above) where LRUs are

considered to be resources applied to the objective of maximizing aircraft availability subject to budgetary limitations. As the number of LRUs in inventory increases, the marginal increase to aircraft availability decreases. Once viable availability functions are determined, a mathematical model can be constructed that provides the optimal level of availability and the corresponding stock level. Deckro and Hebert suggest three modeling approaches for diminishing returns in a project resource setting (1995:9).

The first, a Linear Approximation Model (LADRM), formulates a linear approximation of the nonlinear availability functions (Deckro and Hebert, 1995:9). Such a formulation could be modified so LRU availability is approximated over the possible range prescribed by the inventory upper and lower bounds. This approach requires the introduction of variables which represent the value of the availability function evaluated at its lower and upper bounds. These values indicate the maximum and minimum contributions of a given LRU to aircraft availability.

The slope of the linear approximation is defined as the value of the availability function evaluated at the upper bound (the highest availability level) minus the value of the availability function evaluated at the lower bound (the lowest availability level) divided by the difference between the lower and upper bounds. Considering the shape of a curve that demonstrates diminishing marginal increases as levels of input increase, the value of the approximated slope will be nonpositive (Deckro and Hebert, 1995:10). Alternatively, linear approximations of the LRU availability functions can be developed as a linear objective function that minimizes aircraft unavailability. The model will contain at a

minimum a budget constraint. The number of parts to purchase are variables in this model. They are continuous between the specified upper and lower bounds.

This formulation has the advantage of being a traditional linear program.

Furthermore, the model's variables are bounded. Many solvers are available to effectively solve large problems of this type. In addition, the solution lends itself to complete sensitivity analysis. Inventory levels and aircraft availability are a direct output of the model formulation and are available relative to the constrained procurement budget. This technique has drawbacks due to the linearization of the nonlinear availability functions which demonstrate diminishing returns. A level of accuracy and the impact of the effects of varying inventory levels may be lost (Deckro and Hebert, 1995:12-14).

Considering the nonlinearity of the availability functions, a viable solution technique is presented with a second approach, the Nonlinear Diminishing Returns Model (DRM). This model directly applies the LRU availability functions. If these functions are Karush-Kuhn-Tucker (KKT) regular and of the correct convexity, any number of available nonlinear programming codes can provide a solution. This model provides increased accuracy and captures the nonlinear nature of the diminishing returns thus providing a more accurate representation of the real world problem (Deckro and Hebert, 1995:14).

Deckro and Hebert point out two primary drawbacks to this solution technique outside the computational advantage of linear versus nonlinear models. First, the KKT restrictions can not always be met when generating the specific underlying functions. An example is a discontinuity within the range of variation for a resource availability for a particular activity. A second drawback is the requirement to assume a continuous

resource application (Deckro and Hebert, 1995:15,16). These drawbacks apply to the formulation of the availability curves for each LRU. The curves generated need to be strictly concave so if discontinuities exist they will need to be removed. Additionally, parts are purchased as discrete increments to the stock level so the continuity issue needs to be addressed in an AAM reformulation. (The purchase of one third of an LRU is not feasible.) This leads to a third alternative solution technique which incorporates discrete stock levels.

The Discrete Diminishing Returns Model (DDRM) discretizes the nonlinear availability functions. The intent of this model is to purchase parts in a more realistic discrete fashion while capturing the diminishing returns effect (Deckro and Hebert, 1995:16). This formulation requires the development of zero-one variables which correspond to the possible discrete stock levels of each LRU. Each variable of this type that holds a value of one in the optimal solution indicates the stock level to maintain for the corresponding LRU. Note that for each LRU included in the model only one stock level can be maintained so the sum of its corresponding binary variables will be equal to one, commonly referred to as a special ordered set of type 1 (Deckro and Hebert, 1995:20).

This model is an integer program (IP) that can be solved with available commercial solvers. One limitation of IP solution techniques is that they generally require a large number of iterations and a substantial amount of computer time based on the number of integer variables modeled. This formulation provides an element that can speed the solution process due to the limitation of only one stock level per LRU. Special ordered

set constraints limit the number of feasible solutions and can speed computer solution time. In addition, tight bounds on the possible discrete stock levels can aid in problem entry and solution time. The AAM items may exhibit such tight bounds in specific cases.

III. Methodology

Overview of Methodology

The purpose of this research is to suggest a reformulation of the AAM that provides a comparable solution while adding the capability to conduct relevant sensitivity analysis. The method of achieving this purpose involves the development of a viable mathematical programming model that can be modified to investigate the influence of various factors on the optimal solution while providing essentially the same or improved solution as the AAM. Post-optimality analysis incorporates the addition of necessary constraints as well as the analysis of those factors already in the model. This includes traditional sensitivity analysis of the right hand side (RHS) and objective function coefficients. In each case, a range of values is determined over which the respective values can vary and retain the current optimal basis. Simple sensitivity analysis varies each value independent of the other factors in the model. A parametric analysis of multiple factors provides potential for post-optimality excursions aimed at investigating the model's sensitivity to various inputs and potential trade-offs. Each element of the model is defined below.

Data

An AAM run provides the data required to formulate the mathematical model.

(Data are from the March 1995 run of the AAM.) The data include the sort values and availability rates for relevant stock levels of those LRUs used on the specified MDS. The model also requires the prorated purchase cost for each component. This study models

the AAM output data for the F-15E based on its current buy status, parts requirement, number of aircraft in the Air Force inventory, active funding level, and input received from Air Force Materiel Command Headquarters as of 7 November 1995.

Decision Variables

The decision variables are defined as the various stock levels of those LRUs used on the MDS being modeled (in this case the F-15E). Each variable name corresponds to the stock level and national stock number (NSN) associated with the LRUs. The following assumptions specify an acceptable range of NSN stock levels, as determined relative to output from an execution of the AAM. This allows the formulation of a bounded variable mathematical model.

Assumptions

The AAM is based on a marginal analysis of the improvement to availability per increment of inventory. A reformulation to a mathematical programming model requires the statement of its assumptions. First, the model assumes availability rates increase at a decreasing rate as inventory increases. This ensures the availability functions will be strictly monotonic and concave. (This will prove to be essential for the development of a tractable objective function.) Additionally, it is assumed the sort values are strictly decreasing at a decreasing rate (a monotonic and convex function). Both availability rates and sort values are bounded in the open interval from zero to one.

Objective Function

Formulation of the objective function is the most critical element of the proposed model. The ability to find an optimal solution comparable to that found by the AAM is

governed by the shape of the functions represented in the overall objective function. The following factors are taken into consideration in the formulation of a workable objective function:

- 1. Accuracy: The optimal objective function value should provide a level of availability equal to or greater than that achieved by the AAM. Given that the greedy heuristic approach used in the AAM does not guarantee optimality, an optimization approach should meet or exceed its performance. (This subject will be discussed in further detail later.)
- 2. Solution time: The approximating function should be continuous and well behaved within the inventory item's upper and lower bounds to reduce the effort of the search algorithm. A continuous formulation is preferred over an integer formulation. While items are purchased in discrete increments, integer programming models often require much more time to reach a final solution than continuous models. It has been shown that the resources required to find an optimal solution to integer models increase exponentially with problem size (Jensen, 1990:9-1).
- 3. Sensitivity analysis: Integer problems do not readily provide a sensitivity analysis capability. A continuous model, be it non-linear, linear, or piecewise linear, allows the analyst to conduct extensive sensitivity analysis much more directly and readily than an integer formulation.

This research investigates three general objective function formulations: a continuous non-linear model, a continuous linear model, and a piecewise linear discrete/continuous model.

As discussed in Chapter II, the sort value associated with each LRU's stock level contains the natural logarithm of the improvement factor due to the n(j)+1 component divided by the prorated cost of that component. The objective is to maximize the improvement to aircraft availability as a function of the LRU stock levels. The initial objective function formulation considers the exponential nature of the availability values associated to each inventory level. As inventory increases, availability approaches an upper bound of one at a decreasing rate (decreasing marginal returns). A plot of availability data shows that the following functional form approximates the shape of the data (see Appendix A, page A-1 for a plot of the test case data):

$$1 - a \cdot e^{b \cdot x_{NSN}} = q_{NSN}$$
$$a \cdot e^{b \cdot x_{NSN}} = 1 - q_{NSN}$$
$$\ln(a) + b \cdot x_{NSN} = \ln(1 - q_{NSN})$$

where x_{NSN} is the stock level for the part designated by NSN and q_{NSN} is that part's availability contribution at that stock level. Manipulation of the approximating function as shown above allows a linear least squares regression to determine the "best fit" values of a and b. Table 3-1 contains the estimates for a and b used in the continuous nonlinear and linear models. Additionally, Table 3-1 provides regression R-squared and F-statistic values to demonstrate the quality of the approximated functional form. The data tabulated here show that the exponential approximation provides an extremely high level of

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accuracy and confidence. These conditions are indicated by R-squared values near one and F-statistics that in all cases indicate the approximated coefficients are significant at an alpha level of 0.05 in the one tail F-test.

Table 3-1. Regression Analysis of Availability Data

Var. #	NSN	Fitted a	ln(Fitted a)	Fitted b	R-squared	F-Statistic
	1005012982522	0.00041062		-0.90914223	0.99943109	10540.4208
	1270013562584FX	0.00010236		-0.44313548	0.85371114	23.3432
	1560012912590FX	0.00168836		-0.58961422	0.99888776	10777.0052
NSN-4	1620012409687	0.00119007	-6.73374072	-0.32992158	0.93945539	341.3685
NSN-5	1630012251893	0.12384435	-2.08872971	-0.05228081	0.99065109	22146.5369
NSN-6	1650012511153	0.00001616	-11.03318686	-0.32485814	0.91843142	90.077
NSN-7	1650013969218	0.00011345	-9.08413158	-0.74676460	0.99419713	1027.9708
NSN-8	1650013980036	0.00111488	-6.79900823	-0.55967646	0.99899287	11903.0741
NSN-9	1660013387046BO	0.00060903	-7.40363622	-0.62058812	0.95853028	208.0258
NSN-10	1660013389649BO	0.00668540	-5.00782883	-0.60584181	0.99662356	4132.3794
NSN-11	1680012283821	0.00001393	-11.18151106	-0.76880881	0.99111472	334.6371
NSN-12	1680012283822	0.00000316	-12.66652254	-0.80471896	0.96814382	30.3911
NSN-13	2835012180143	0.00036743	-7.90897545	-0.24335330	0.99958457	57747.8156
NSN-14	2835012188080	0.00000746	-11.80569868	-0.20339569	0.95036423	210.6144
NSN-15	4810012518480HS	0.00000254	-12.86772116	-1.58266767	1.00000000	undefined
NSN-16	4810012537542	0.00614650	-5.09187294	-0.67215120	0.99757433	4935.0789
NSN-17	4810013377136TP	0.00006043	-9.71409968	-0.48985035	0.97100772	234.4436
NSN-18	5821012483022FX	0.00024518	-8.31353708	-0.53032270	0.93312518	125.5798
NSN-19	5895012913073FX	0.00005469	-9.81377565	-0.64388566	0.85437785	35.2025
NSN-20	5895013640160LN	0.00270954	-5.91097487	-1.38879930	0.99688605	1600.6788
NSN-21	5895013823225FX	0.00083508	-7.08798666	-0.39531865	0.99932578	23715.0661
NSN-22	5985013902368EW	0.00357285	-5.63439104	-0.39528303	0.99829414	11704.3072
NSN-23	5985013934820EW	0.00051209	-7.57700415	-0.70941160	0.99940425	13420.5129
NSN-24	5998013410403FX	0.00003264	-10.33011201	-0.46259325	0.87528490	42.1097
NSN-25	6110012305147	0.00000170	-13.28597119	-0.10819770	0.86785439	26.2696
NSN-26	6605012400136FX	0.00435235	-5.43703911	-0.15738695	0.99446786	9347.6202
NSN-27	6610013195039	0.02439354	-3.71343697	-0.24717362	0.98516365	2523.2766
NSN-28	6615012444251	0.00001338	-11.22168162	-1.02304883	0.89836208	17.6777
NSN-29	6615013462155	0.00002089	-10.77608277	-0.38083218	0.99964274	22384.3496
NSN-30	6615013527003	0.00097102	-6.93716278	-0.27275089	0.98771809	2010.5137

The continuous non-linear objective function uses the following derived availability function for each LRU.

$$1 - \hat{\mathbf{a}} \cdot \mathbf{e}^{\hat{\mathbf{b}} \cdot \mathbf{x}_{NSN}} = \mathbf{q}_{NSN}$$

Where x_{NSN} is defined as the stock level for the part associated with NSN and q_{NSN} is that part's availability level at stock level x_{NSN} . The first objective function value is then the sum of the natural logarithm of each LRU's inventory level contribution to overall aircraft availability. (The sum of the natural logarithms maintains a linear model as opposed to the product form of aircraft availability as discussed in Chapter II. The exponential of the optimal objective function value is MDS availability.)

A continuous linear objective function is derived using the same values of a and b found by regressing the AAM data. The functional form for each LRU is as follows:

$$\ln(a) + b x_{NSN} = \ln(1-q_{NSN})$$

(All equation elements are as defined above.) The objective in this case is to minimize the sum of the natural logarithm of one minus the availability contribution of the LRU stock levels. Note that in this case the functional form results in a minimization of "unavailability." MDS availability is simply one minus the exponential of the optimal solution.

The final objective function formulation investigated here is a piecewise linear discrete formulation. The general form is applied to both availability data and LRU sort values. The concept for this formulation is to capture the discrete nature of the problem while maintaining a continuous and linear model. In general, piecewise linear formulations of non-linear equations require a mixed integer format with binary variables used to define

each breakpoint. In the case of a concave function applied to a maximization formulation (convex in the minimization case), where the piecewise slope becomes less favorable as the value of the decision variable increases (as the stock level increases), a mixed integer formulation is unnecessary (Winston, 1994:485). Within the explicitly defined region where the function meets the conditions listed above, the formulation behaves as a piecewise mixed integer problem while maintaining continuous variables. Maintaining continuous variables allows a much more extensive sensitivity analysis capability.

(Sensitivity analysis of an integer program is much more limited than that of a continuous linear program and generally requires multiple runs of various scenarios (Nauss, 1979:24-26). See Nauss for a comprehensive discussion of parametric integer programming.) The piecewise linear formulation also requires constraints which equate the sum over each LRU to one. This type of constraint in a continuous formulation ensures a valid convex combination of the feasible stock levels. In addition, only one stock level is possible for each LRU modeled.

Constraints

The initial formulation includes only a budget constraint. The budget level is determined by current Air Force allocations relative to the MDS modeled (the F-15E in this study). Additional constraints are added once the initial formulation is shown to achieve a comparable optimal solution to that of the AAM.

Several opportunities for additional constraints fit within the framework of the basic models explained above. Some specific examples include introducing sub-budgets at the LRU level, constraining the MDS availability, limiting the number of LRUs purchased,

fixing the availability contribution of a suite of related LRUs to determine the impact on a part by part basis, and modeling subindentured items. These points will be expanded upon later in this study.

Base Model Formulation

The base model must demonstrate the capability to reproduce purchases comparable to those found using AAM methodology on a shopping list derived for a subset of data. These purchases ultimately result in the optimal stock levels for each LRU. Each model discussed above is presented in mathematical form below.

Continuous Non-linear Program (CNLP)

$$\begin{aligned} \text{Max } & \sum_{\text{NSN}} \ln(1 - \hat{\mathbf{a}} \cdot \mathbf{e}^{\hat{\mathbf{b}} \cdot \mathbf{x}_{\text{NSN}}}) \\ \text{s.t. } & \sum_{\text{NSN}} \text{PC}_{\text{NSN}} \cdot \mathbf{x}_{\text{NSN}} \leq \text{MDS (F-15E) Budget Allocation} \\ & \text{LB}_{\text{NSN}} \leq \mathbf{x}_{\text{NSN}} \leq \text{UB}_{\text{NSN}} & \forall \text{NSN} \end{aligned}$$

where x_{NSN} is defined as the stock level for the corresponding NSN, PC_{NSN} is the prorated cost of the NSN, and LB_{NSN} and UB_{NSN} are the NSN inventory lower and upper bounds respectively. The objective function maximizes the sum of the natural logarithms of the approximated availability rates at stock levels x_{NSN} which has the effect of maximizing MDS availability as a function of the NSN stock levels. The budget constraint allows parts to be purchased up to the MDS budget allocation.

Continuous Linear Program (CLP)

$$\begin{aligned} & \text{Min } \sum_{\text{NSN}} (\ln(\hat{a}) + \hat{b} \cdot x_{\text{NSN}}) \\ & \text{s.t. } \sum_{\text{NSN}} \text{PC}_{\text{NSN}} \cdot x_{\text{NSN}} \leq \text{MDS (F-15E) Budget Allocation} \\ & \text{LB}_{\text{NSN}} \leq x_{\text{NSN}} \leq \text{UB}_{\text{NSN}} & \forall \text{NSN} \end{aligned}$$

The model elements are defined as in the CNLP. The objective function minimizes the sum of the natural logarithms of the approximated aircraft unavailability at stock levels x_{NSN} which has the affect of minimizing aircraft unavailability as a function of the LRU stock levels.

Piecewise Linear Discrete/Continuous Model (using availability, q) (PLDMq)

$$\begin{aligned} \text{Max } & \sum_{\text{NSN}} \ln(q_{\text{NSN}_i}) \cdot \text{NSN}_i \\ \text{s.t. } & \sum_{\text{NSN}} \text{PC}_{\text{NSN}} \cdot i \cdot \text{NSN}_i \leq \text{MDS (F-15E) Budget Allocation} \\ & \sum_{i=\text{LB}}^{\text{UB}} \text{NSN}_i = 1 & \forall \text{NSN} \\ & 0 \leq \text{NSN}_i \leq 1 & \forall \text{NSN}_i \end{aligned}$$

where NSN_i is defined as a continuous variable in the region bound by zero and one for the corresponding NSN at stock level i. When NSN_i is equal to one, the stock level for NSN is i. The sum over i for each NSN is equal to one to ensure one feasible inventory position per part modeled. PC_{NSN} is the NSN prorated cost and is multiplied by the stock level, i, to determine the budget increment at that stock level. $q_{NSN,i}$ is the AAM availability rate for the corresponding NSN at stock level i.

The objective function is a monotonic and concave piecewise linear function defined by the discrete LRU availability rates. The objective function maximizes the sum

of the natural logarithms of the LRU availability rates at each stock level i. This model provides the maximum MDS availability level based on the discrete LRU availability rates provided by the AAM as constrained by the MDS budget allocation.

Piecewise Linear Discrete/Continuous Model (using Sort Values) (PLDMsv)

$$\begin{aligned} & \text{Min } \sum_{NSN} \text{SV}_{NSN} \cdot \text{NSN}_{i} \\ & \text{s.t. } \sum_{NSN} \text{PC}_{NSN} \cdot \mathbf{i} \cdot \text{NSN}_{i} \leq \text{MDS (F-15E) Budget Allocation} \\ & \sum_{i=LB}^{UB} \text{NSN}_{i} = 1 & \forall \text{NSN} \\ & 0 \leq \text{NSN}_{i} \leq 1 & \forall \text{NSN}_{i} \end{aligned}$$

The model elements are defined as in the PLDMq except in this case the piecewise linear objective function is monotonic and convex as defined by the AAM sort values. The objective function minimizes the sum of the LRU sort values at stock level i. This model finds the optimal budget allocation that allows each LRU the potential to move down its vector of sort values which has the affect of providing the maximum improvement to MDS availability per dollar spent. The PLDMsv provides an objective that gives each LRU stock level the same weight as that used to determine its position on the AAM shopping list.

Model Size

The AAM includes 447 different LRUs for the F-15E with 10,260 sort values and their corresponding inventory levels. A reformulation based on the entire data set is a major endeavor and was not necessary to demonstrate the viability of the approaches investigated here. Of the 447 different LRUs, 73 (1,318 sort values) are unique to the F-

15E. This is indicated by a cost proration factor of one, meaning the part is not shared. Furthermore, those LRUs in the subset of unique items that contain three or less data points (32 LRUs), are in a full stock position (indicated by a negative buy position), and/or do not meet the assumptions outlined above are not modeled. This refined subset of LRU data (30 in the non-linear and linear models and 20 in the linear piecewise models) is used in the models presented here.

IV. Results and Analysis

Formulation of Availability Function Approximations

The initial objective function formulation of the mathematical programming model focuses on determining the best functional fit to the LRU availability data. Theoretically, a quadratic function provides a simple form which non-linear solvers can easily handle. The following techniques provide insight to the determination of the correct approximating function:

- 1. Three point quadratic approximation.
- 2. Quadratic least squares approximation.
- 3. Cubic least squares approximation.
- 4. Three point exponential approximation.

Each technique was applied to data for NSN 1005012982522 as a test case. Full Mathcad software package output for each technique is provided in Appendix A.

An analysis of the results in the test case shows that polynomials of order two and three do not accurately capture the functional characteristics of AAM output data. Most notably, the polynomial functions do not maintain the monotonic assumption within the required inventory bounds. The exponential function meets the model's assumptions and provides the best fit of those techniques investigated in this study (see Appendix A, page A-6). Specifically, one minus the exponential of the given stock levels provides the most accurate approximation of the LRU availabilities. The sum of square error between the fitted and actual values for the three point exponential approximation in the test case is

2.241E-11. This value is three orders of magnitude smaller than the comparable quadratic approximation formula.

Each series of LRU availability terms, when converted to a linear form and regressed, provides the least squares estimates of the exponential parameters shown in Table 3-1 (page 3-5). Based on these tests, each LRU's availability function in the non-linear model as defined in Chapter III has the following form:

$$1 - \hat{\mathbf{a}} \cdot \mathbf{e}^{\hat{\mathbf{b}} \cdot \mathbf{x}_{NSN}} = \mathbf{q}_{NSN}.$$

Analysis of the Continuous Non-Linear Program (CNLP) Performance

The individual LRU availability functions provide the basis for determining the optimal number of additional LRUs to purchase in the CNLP. The model determines the maximum sum of the natural logarithms of the availability functions evaluated at the optimal inventory levels for each LRU. Each variable has an upper and lower bound determined by the AAM availability values that meet the model assumptions. The LRU bounds are the same for all of the models discussed in this study so the models can be readily contrasted and compared.

The optimal solution to this model, as determined by the Microsoft Excel solver on a 486 DX2 personal computer, is similar to that found by the AAM. However, for several reasons the results are not satisfactory for the purpose of this research. (See Appendix B for the Excel results for this model.) Most notably the optimal stock levels are not provided in discrete increments. Furthermore, the approximation functions do not provide an acceptable level of accuracy for the following reasons. The continuous approximations are based on least squares estimates but ultimately model accuracy is limited due to the

small marginal differences between data points. In many cases the marginal difference between availability values is on the order of 10⁻⁶. Additionally, this formulation requires the sum of the natural logarithms of the approximated availability rates. These computational steps also contribute to the model's inaccuracy. This continuous model does provide a fully capable tool to conduct sensitivity analysis but does not provide the desired discrete solution.

Analysis of the Continuous Linear Program (CLP) Performance

Linear models provide fast solution times as well as a strong sensitivity analysis capability. The LP formulation uses availability data to develop linear functions based on the parameters of the exponential functions in the CNLP formulation. The solution to this model, as determined by the Microsoft Excel Solver, is not comparable to the AAM solution. (See Appendix C for the Excel results for this model.) All but one variable is at either its upper or lower bound. The solution technique chooses an NSN based on its objective function coefficient which is simply the slope of the linear approximating function. The most favorable variables are purchased to the upper bound and the least favorable are set to the lower bound. The final LRU chosen is purchased up to the budget limit. Given the sensitivity of the data and the magnitude of the coefficients, this approximation does not meet the objectives of this research. While the CLP is quick to solve, its accuracy is not acceptable as an alternative for the AAM.

Analysis of the Discrete/Continuous Model Performance

The discrete/continuous model is ideal for the problem environment presented by the AAM. The monotonic and concave (maximization) availability piecewise linear

functions allow integer answers in a continuous formulation. (The same is true for the monotonic and convex (minimization) sort value piecewise linear functions.) The strictly increasing or decreasing at a decreasing rate assumption is necessary for this formulation to perform correctly. This requirement uncovered a problem with some of the AAM availability and sort value data.

The sort value data in all cases are strictly decreasing (this is required in the AAM formulation). Unfortunately, these same values do not decrease at a decreasing rate in all cases (they do not demonstrate diminishing marginal returns). The strictly concave assumption is violated. A like condition exists with availability data. These data inconsistencies are attributed to the AAM equal base assumption. This assumption requires additional parts to be held as part of the depot inventory until enough parts are purchased for each base to receive an additional item. The equal base assumption subsequently results in nondiminishing returns in those cases when the AAM redistributes those parts assumed to be held in the depot inventory (Rexroad, 1996).

The PLDMsv and PLDMq require monotonically decreasing and monotonically increasing at a decreasing rate break points, respectively, in order to maintain continuous variables and still offer a discrete solution. This study handles cases of nondiminishing returns by establishing a region about the original AAM optimal inventory purchases that comply with the model assumptions. Those values that do not meet the modeling assumptions are omitted from this demonstration of the approach.

This process explicitly defines the LRU upper and lower bounds that are used in both the PLDMq and PLDMsv. Acceptable ranges are determined based on sort value

data as opposed to derived AAM availability rates. Sort values are used by the AAM to rank order the proposed LRU purchases and are therefore considered reliable. When availability data violates the monotonic and strictly concave assumption within the specified sort value ranges, acceptable data points are approximated and included to maintain equivalent bounds. (Thirteen of the 102 availability values modeled are approximated.) In practice, the proposed models should be based on actual AAM output data so that there is no accuracy loss due to approximation or data smoothing.

Data preprocessing for the purpose of this study includes filtering the full set of data to obtain the subset defined in Chapter III. The remaining data are screened as discussed above using an Excel spreadsheet to obtain the final model data set. Those data are then converted to MPS format (an industry standard format for optimization programs (CPLEX, 1994:81)) and loaded into the CPLEX optimization solver. CPLEX is used due to its capability to handle very large models (unlimited variables and constraints (Sharda, 1995:52)) and because it is an efficient and effective solver with sensitivity analysis capabilities. (CPLEX provides sensitivity ranges for the objective function coefficients and constraint right hand sides. These can be expanded through the use of the CPLEX callable routine library and FORTRAN programming.)

The concepts discussed above were applied to the formulation of the PLDMq and PLDMsv. For illustrative purposes, three arbitrary budget levels are implemented in each model. The first budget level is a maximum budget allotment that allows each LRU to be purchased at its upper inventory bound. This model is used to verify the model and data accuracy. Two intermediate funding levels show the model's performance in varying

budgetary scenarios. Application of AAM methodology to the explicitly defined subset of data determines the shopping list optimal buy position and is shown in Appendix D. This solution is used as a base case to compare to the optimal solution achieved by the mathematical programming models. Model comparisons are shown in Tables 4-1 and 4-3. Appendix E contains the CPLEX solution output information.

Table 4-1. Comparison of the Shopping List and PLDMsv Optimal Solutions

	Budget=3851653.46 Budget=3185774.84		3185774.84	Budget=2700221.70		
	Shopping List	PLDMsv	Shopping List	PLDMsv	Shopping List	PLDMsv
1005012982522	5	5	4	5	3	4
1270013562584FX	2	2	1	1	0	0
1560012912590FX	5	5	5	5	2	5
1630012251893	131	131	131	131	131	125
1650013969218	2	2	0	0	0	0
1660013387046BO	6	6	4	5	3	3
1660013389649BO	13	13	11	13	9	10
2835012180143	4	4	4	1.529	1	1
2835012188080	4	4	0	0	0	0
4810012537542	13	13	12	13	10	13
4810013377136TP	5	5	5	5	5	4
5821012483022FX	6	6	6	6	4	5
5895012913073FX	11	11	11	11	9	9
5895013640160LN	6	6	4	6	4	4.401
5895013823225FX	4	4	4	3	4	3
5985013902368EW	14	14	14	14	12	13
5985013934820EW	8	8	7	8	5	8
5998013410403FX	3	3	2	3	0	0
6605012400136FX	11	11	9	9	9	8
6610013195039	42	42	42	42	42	39
Optimal Solution	1.38223E-08	1.38223E-08	1.65542E-08	1.41259E-08	2.53607E-08	1.88853E-08
System Availability	0.99831671	0.99831671	0.99804701	0.99810042	0.99763562	0.99793697

This research includes the PLDMsv to determine the impact of implementing an optimization approach as opposed to the greedy heuristic used by the AAM. The

objective function coefficients provide each variable the same weight as the AAM shopping list. Opposing solution techniques based on the same objective function vectors can easily be compared and contrasted on a decision variable level. Table 4-1 shows that the PLDMsv clearly outperforms the AAM methodology on the bottom line. The PLDMsv achieves a higher level of system availability per funds applied. The increased improvement in availability achieved by the PLDMsv at a budget level of \$2,700,221.70 results in an MDS availability of Q=0.99793697 as compared to the shopping list Q of 0.99763562. (It should be noted that while the numerical differences in the objective functions is small, in this model and in those that follow, literally hundreds of thousands of dollars may be reallocated on the basis of a difference of this magnitude.) A case by case analysis of those items that have different values in the optimal solutions provides insight to the trade-offs being made. Table 4-2 provides a summary of the trade-offs made between the shopping list and PLDMsv optimal solutions.

The PLDMsv purchases items that provide a greater improvement to availability than the AAM purchases for the same budget allocation. This is achieved through the elimination of some items and the addition of others. The additions in Table 4-2 are those items that the PLDMsv purchased below the AAM cut-off sort value. These are items the greedy heuristic could not fit under the budget limitation. The optimization approach selected these items and gave up other items above the AAM cut-off sort value to achieve a higher increase in MDS availability at the same budget level.

Table 4-2. Trade-Off Analysis of the Shopping List and the PLDMsv Optimal Solutions

Additions					
Traded NSNs	<u>Variable</u>	Sort Value	Stk lvl	Cost	Cost @ SV
1005012982522	1	0.0000000005730797	4	29716.86	118867.44
1005012982522	1	0.0000000013760097	3	29716.86	89150.58
	Net Improvement	-0.0000000008029300		Net Increase	29716.86
1560012912590FX	1	0.0000000003652814	5	3231.73	16158.65
1560012912590FX	1	0.0000000017456548	2	3231.73	6463.46
	Net Improvement	-0.0000000013803734		Net Increase	9695.19
4.60044440064070		0.0000000000000000000000000000000000000	10	15100 16	151001 60
1660013389649BO	1	0.0000000009054756	10	17408.46	174084.60
1660013389649BO	1	0.0000000016763722	- 9	17408.46	156676.14
	Net Improvement	-0.0000000007708966		Net Increase	17408.46
4810012537542	1	0.00000000002067420	13	4377.40	56906.20
4810012537542	1	0.0000000018321009	10	4377.40	43774.00
1010012331312	Net Improvement	-0.0000000016253589	-	Net Increase	13132.20
	- 100 - 111 pro 1011 on	0.0000000000000000000000000000000000000		- 100 - 110 - 100 -	
5821012483022FX	1	0.0000000009481328	5	17058.08	85290.40
5821012483022FX	1	0.000000018820221	4	17058.08	68232.32
	Net Improvement	-0.0000000009338893		Net Increase	17058.08
5895013640160LN	0.5991434	0.0000000006813538	4	33661.84	80673.08
5895013640160LN	0.4008566	0.0000000001091371	5	33661.84	67467.85
5895013640160LN	1	0.0000000011372132	- 4	33661.84	134647.36
	Net Improvement	-0.0000000003467224		Net Increase	13493.57
5985013902368EW	1	0.0000000008677973	13	13342.04	173446.52
5985013902368EW	1	0.000000000000077973	12	13342.04	160104.48
3963013902306EW	_		-		
	Net Improvement	-0.0000000004200370		Net Increase	13342.04
5985013934820EW	1	0.0000000002232926	8	8484.08	67872.64
5985013934820EW	1	0.000000019062088	5	8484.08	42420.40
	Net Improvement	-0.0000000016829162	-	Net Increase	25452.24
	Total Improvement	-0.0000000079631238	-	Total Increase	139298.64

Subtractions					
Traded NSNs	<u>Variable</u>	Sort Value	Stk lvl	Cost	Cost @ SV
1630012251893	1	0.0000000019016047	131	8795.12	1152160.72
1630012251893	1	0.0000000026855104	125	8795.12	1099390.00
	Net Loss	0.0000000007839057		Net Decrease	52770.72
4810013377136TP	1	0.0000000012087739	5	8050.00	40250.00
4810013377136TP	1	0.0000000013728717	4	8050.00	32200.00
	Net Loss	0.0000000001640978		Net Decrease	8050.00
5895013823225FX	1	0.0000000017741379	4	53030.98	212123.92
5895013823225FX	1	0.0000000017959398	3	53030.98	159092.94
	Net Loss	0.0000000000218019		Net Decrease	53030.98
6605012400136FX	1	0.0000000019291702	9	15505.66	139550.94
6605012400136FX	1	0.0000000022839261	8	15505.66	124045.28
	Net Loss	0.0000000003547559		Net Decrease	15505.66
6610013195039	1	0.000000018841562	42	3313.76	139177.92
6610013195039	1	0.00000000020472842	39	3313.76	129236.64
	Net Loss	0.0000000001631280		Net Decrease	9941.28
	Total Loss	0.000000014876893	=	Total Decrease	139298.64
	Total Change	-0.0000000064754345		Total Change	0.00

Table 4-3 shows that the optimal buy positions and the resultant optimal MDS availability levels are not the same using AAM methodology and the PLDMq. Like the PLDMsv, the PLDMq finds an optimal solution based on the objective function coefficients. A trade-off analysis in this case differs somewhat from that between the shopping list and the PLDMsv. The objective function coefficients do not apply the same weights to each variable modeled. The objective of the PLDMq is not to find the greatest per item improvement to availability but to find the maximum MDS availability level.

Table 4-4 provides an item by item analysis of those differences in the shopping list and PLDMq optimal solutions.

Table 4-3. Comparison of the Shopping List and PLDMq Optimal Solutions

	Budget=3851653.46		Budget=31	85774.84	Budget=2700221.70	
	Shopping List	PLDMq	Shopping List	PLDMq	Shopping List	PLDMq
1005012982522	5	5	4	4.065	3	3
1270013562584FX	2	2	1	2	0	0
1560012912590FX	5	5	5	5	2	5
1630012251893	131	131	131	131	131	130
1650013969218	2	2	0	0	0	0
1660013387046BO	6	6	4	4	3	3
1660013389649BO	13	13	11	12	9	10
2835012180143	4	4	4	4	1	1
2835012188080	4	4	0	0	0	0
4810012537542	13	13	12	12	10	11
4810013377136TP	5	5	5	4	5	3
5821012483022FX	6	6	6	5	4	5
5895012913073FX	11	11	11	7	9	7
5895013640160LN	6	6	4	5	4	4
5895013823225FX	4	4	4	4	4	4
5985013902368EW	14	14	14	14	12	12.084
5985013934820EW	8	8	7	7	5	6
5998013410403FX	3	3	2	2	0	0
6605012400136FX	11	11	9	9	9	9
6610013195039	42	42	42	37	42	37
Optimal Solution	-1.68471E-03	-1.68471E-03	-1.95490E-03	-1.69693E-03	-2.36718E-03	-1.88526E-03
System Availability	0.99831671	0.99831671	0.99804701	0.99830451	0.99763562	0.99811651

Table 4-4. Trade-Off Analysis of the Shopping List and PLDMq Optimal Solutions

Additions					
Traded NSNs	<u>Variable</u>	<u>ln(q)</u>	Stk lvl	Cost	Cost @ SV
1560012912590FX	1	-0.0000962446313659	5	3231.73	16158.65
1560012912590FX	1	-0.0005127214191654	2	3231.73	6463.46
	Net increase	0.0004164767877995		Net increase	9695.19
1660013389649BO	1	-0.0000173701508602	10	17408.46	174084.60
1660013389649BO	1	-0.0000331305488106	9	17408.46	156676.14
	Net increase	0.0000157603979504		Net increase	17408.46
4810012537542	1	-0.0000036000064800	11	4377.40	48151.40
4810012537542	1	-0.0000075200282754	10	4377.40	43774.00
	Net increase	0.0000039200217954		Net increase	4377.40
5821012483022FX	1	-0.0000112700635069	5	17058.08	85290.40
5821012483022FX	1	-0.0000629319801755	4	17058.08	68232.32
	Net increase	0.0000516619166686		Net increase	17058.08
5985013902368EW	0.9161545	-0.0000315529043241	12	13342.04	146680.44
5985013902368EW	0.0838455	-0.0000019175685125	13	13342.04	14542.71
5985013902368EW	1	-0.0000344405930704	12	13342.04	160104.48
	Net increase	0.0000009701202338		Net increase	1118.67
5985013934820EW	1	-0.0000075200282754	6	8484.08	50904.48
5985013934820EW	1	-0.0000155401207471	5	8484.08	42420.40
	Net increase	0.0000080200924717		Net increase	8484.08
	Total Increase	0.0004968093369194		Total Increase	58141.88

Subtractions					
Traded NSNs	<u>Variable</u>	<u>ln(q)</u>	Stk lvl	Cost	Cost @ SV
1630012251893	1	-0.0002135728050480	131	8795.12	1152160.72
1630012251893	1	-0.0002207743688676	130	8795.12	1143365.60
	Net Decrease	0.0000072015638196		Net Decrease	8795.12
4810013377136TP	1	-0.0000049000120050	5	8050.00	40250.00
4810013377136TP	1	-0.0000111500621617	3	8050.00	24150.00
	Net Decrease	0.0000062500501567		Net Decrease	16100.00
5895012913073FX	1	-0.0000001400000098	9	8338.98	75050.82
5895012913073FX	1	-0.0000006300001984	7	8338.98	58372.86
	Net Decrease	0.0000004900001886		Net Decrease	16677.96
6610013195039	1	-0.0000003900000760	42	3313.76	139177.92
6610013195039	1	-0.0000013400008978	37	3313.76	122609.12
	Net Decrease	0.0000009500008218		Net Decrease	16568.80
	Total Decrease	0.0000148916149867		Total Decrease	58141.88
	Total Difference	0.0004819177219327		Total Difference	0.00

This analysis shows that the PLDMq purchases items that provide a higher level of MDS availability than the AAM optimal purchases for the same budget allocation. This is achieved through the elimination of some items and the addition of others. The additions in Table 4-4 are those items that the PLDMq purchased below the AAM cut-off sort value. These are items that the greedy heuristic could not fit under the budget limitation. The optimization routine selected these items and gave up other items above the AAM cut-off sort value to achieve a higher level of MDS availability. The greatest advantage provided by the PLDMq is that it does not search for specific items that provide the greatest improvement for each dollar spent. Rather, the PLDMq provides the highest achievable MDS availability level for a given budget allocation.

The above analysis shows that the objective of the PLDMsv is equivalent to that of the AAM. Each technique provides the greatest improvement in availability per dollar spent (constrained by the MDS budget allocation) toward the goal of achieving the highest level of MDS availability. The objective of the PLDMq formulation is to maximize MDS availability subject to the same MDS budget allocation. A comparison of the PLDMsv and PLDMq optimal solutions and resultant MDS availability rates provides insight to which model provides the highest level of MDS availability. The PLDMsv optimal inventory position results in an MDS availability of Q=0.99793697 (exp(-0.002065158)). The PLDMq provides a Q of 0.99811651 (exp(-0.001885264)). It is noted here that thirteen of those availability rates included in the PLDMq are estimated to ensure a monotonic piecewise function, but the success of this formulation remains clear.

Analysis of the Model Solution Techniques

The solution differences noted here are attributed to the nature of the separate solution techniques and objectives. As discussed previously, AAM methodology is a greedy heuristic that selects those items that provide the greatest improvement to availability in descending order until the budget limit is reached. The AAM shopping list approach is similar to a greedy heuristic used to provide an initial solution to Binary Knapsack problems. Like the AAM shopping procedure, the greedy heuristic considers potential items that have been sorted by "increasing indices and insert[s] each new item into the Knapsack if it fits" (Martello and Toth, 1990:28). Martello and Toth show that the greedy heuristic obtains a feasible solution but provides a worst case performance ratio (defined as the optimal continuous solution divided by the heuristic solution) of one half

(Martello and Toth, 1990:29). The greedy heuristic can not guarantee an optimal solution, illustrating a common characteristic of heuristic problem solving known as satisficing. "Heuristic problem-solving methods are strongly associated with satisficing, as opposed to optimizing, behavior. Heuristic methods do not normally guarantee optimal solutions" (Daellenbach, et. al., 1978:650). Optimality is traded for speed.

CPLEX implements the dual simplex algorithm to achieve an optimal solution.

This type of algorithm systematically searches the region of feasible solutions to determine the most profitable tradeoffs between budget levels and objective function improvement.

Each model's output is the "true" continuous optimal solution, to the degree of accuracy of the data, for the given set of data.

Data Scaling

The CPLEX data found in Appendix E differs from the values in Tables 4-1 and 4-3 by a factor of 1E+16. CPLEX operates with a maximum optimality tolerance of nine decimal places. AAM sort value data is provided in sixteen decimal digit format. Model formulation using this type of raw data results in an extremely sensitive model that is affected by round off error. The natural logarithm of availability rates experiences the same condition as the LRU availability rates approach one. Therefore, the PLDMq is also scaled by a factor of 1E+16. Scaling is required to maintain the AAM's implied significant digits. Given the incremental difference in the AAM's data, the CPLEX routine does not always converge to the same optimal solution when solving a problem that has not been scaled to account for values beyond the ninth decimal place. All post optimality analysis is conducted on output data that has been re-scaled to the original AAM decimal accuracy.

Explanation of the Optimal Basic Feasible Solution

The model output data in Tables 4-1 and 4-3 and Appendix E shows that all model variables are set to discrete inventory positions except for one NSN in all cases. This condition exists due to the model formulation and solution algorithm. The simplex solution algorithm defines each feasible solution as a linear combination of the linearly independent columns of the problem matrix. By definition every feasible solution is a basis of m variables, where the problem matrix contains m rows (constraints) and n columns (variables) (Hillier and Lieberman, 1986:108). The models discussed here have 21 constraints (20 constraints summing to one to ensure a valid convex combination of feasible stock levels, one for each NSN, and the budget constraint) and 102 variables (the 102 data points which define the concave/convex piecewise linear functions). This combination of model parameters results in one more basic variable than NSN modeled and results in one non-integer inventory level.

An acceptable all integer solution is achieved by rounding the non-discrete variable down. The resulting solution may be integer sub-optimal but still exceeds the availability level provided by the AAM optimal buy position. For example, the PLDMq base case requires rounding NSN 5985013902368EW down to a stock level of 12. This results in an objective function decrease of 9.701171634E-7 and a decrease in MDS availability from 0.99811651 to 0.99811555. This example is provided for illustrative purposes only but it shows a negligible decrease in MDS availability to obtain an all integer solution. The resulting solution, however, still exceeds the AAM's results for the same case.

Traditional Sensitivity Analysis

Linear programming provides sensitivity data for the right hand side of the constraints and the objective function coefficients as a post-optimality analysis tool. Data for the PLDMq at a budget level of 2,700,221.70 dollars is provided in Appendix F. This data shows that the budget can decrease to a level of \$2,699,103.03 and increase to a level of \$2,712,445.07 and retain the current optimal basis. (The current mix and values of purchases remains the same except that the fractional amount of the non-discrete stock level varies until a less or more favorable purchasing option is reached.) The availability rate provided by NSN 1005012982522 at a stock level of four can be decreased from the current value of 0.99998862 to 0.99998224 or increased to a value of 0.99999736 and still remain in the optimal basis. This type of analysis is valuable in assessing the impact of such factors as technological improvements or part degradation due to extended shelf life, for example.

Modeling Additional Constraints

Those models proposed here provide an analysis capability beyond the traditional sensitivity tools discussed above with the addition of properly formulated constraints. The additional constraints offered here are examples of the potential of these models. Each constraint is formulated and then applied in the PLDMq to indicate possible impacts on the current optimal solution.

The first proposed constraint models a suite of items that are required to obtain a minimum level of availability. A constraint of this type can be applied in the example of subindentured items that contribute to the availability of a major component such as an

engine. Those items that make up the end item of concern are included in a single constraint with the natural logarithm of the availability rate at the associated stock level as a constraint coefficient. The sum of these availability rates is greater than or equal to the natural logarithm of the desired major component availability level. This constraint has the following form:

$$\sum_{NSN \in S} \sum_{i} \ln(q_{NSN_{i}}) \cdot NSN_{i} \ge \ln(availability)$$

where S is defined as the set of parts that make up the next higher assembly and availability is the required availability rate of the next higher assembly.

For illustrative purposes, four arbitrary NSNs were chosen to formulate a constraint as defined above and applied in the PLDMq. The current optimal availability level provided by these NSNs is 0.99972854 (exp(-0.002715)). The additional constraint requires an availability level of no less than 0.999777 (ln(availability) = -0.00223025). The CPLEX output of the PLDMq with this additional constraint is in Appendix G, page G-1. The additional availability requirement for this small subset of NSNs results in a reallocation of the MDS budget resource. The optimal inventory position in this case results in an MDS availability slightly lower than the original optimal value (from 0.99811651 to 0.99798229). This example shows that by requiring a higher level of availability for a major subassembly on the aircraft a portion of MDS availability is sacrificed. While the current AAM formulation would require multiple runs to analyze such a scenario, the proposed model allows these types of trade-offs to be considered directly.

Other possible constraints are based on the concept of sub-budgets within an MDS budget allocation. Those LRUs that are included as part of a sub-budget are summed as in the MDS budget constraint and are further limited at the sub-budget level. The formulation of this type of constraint is as follows:

$$\sum_{NSN \in S} \sum_{i} PC_{NSN} \cdot i \cdot NSN_{i} \leq Sbudget$$

where S is defined as the set of parts that make up the specified sub-budget, Sbudget.

Four arbitrary NSNs were chosen to illustrate the implementation of a sub-budget constraint in the PLDMq. The NSNs chosen require \$422,032.54 of the MDS budget allocation in the current optimal solution. The additional constraint limits these parts to an allocation of \$350,000.00. (CPLEX output of the PLDMq with the addition of this constraint is in Appendix G, page G-4.) The sub-budget restriction results in a redistribution of the MDS budget and a subsequent decrease in the optimal MDS availability rate from 0.9981165 to 0.99809438.

A similar constraint requires a subset of parts to meet a minimum budget allocation.

$$\sum_{NSN \in S} \sum_{i} PC_{NSN} \cdot i \cdot NSN_{i} \ge Sbudget$$

where S is defined as the set of parts that make up the specified sub-budget, Sbudget.

The same NSNs modeled in the first sub-budget constraint are modeled here. In this case the budget allocation to these parts is required to meet or exceed \$500,000.00. (CPLEX output for this model is found in Appendix G, page G-8.) Once again the

optimal budget allocation is adjusted to meet the conditions of the new constraint. The impact is a decrease in MDS availability from 0.99811651 to 0.99806890.

The number of parts purchased can be managed beyond the LRU upper and lower bounds through the formulation of constraints of the following type.

$$\sum_{NSN \in S} \sum_{i} i \cdot NSN_{i} \leq Stock Level$$

where S is defined as the set of parts subject to the specified stock level. Constraints of this type apply in various scenarios including the modeling of storage limitations and inventory control programs.

Those NSNs used to demonstrate the sub-budget constraints are used in the formulation of an example inventory control constraint. The total number of parts purchased for this subset of NSNs in the original optimal solution is 20. The additional constraint restricts the total inventory of these part to an upper bound of 15. The optimal MDS availability for this model is 0.99807595 a decrease of 0.00004056 from the basic model (see Appendix G, page G-11 for the CPLEX output for this model).

The above constraint examples demonstrate the versatility and strength of the post-optimality analysis capability of the PLDMq formulation. Note that with the inclusion of new constraints, the optimal basis requires an additional basic variable. This results in one more non-integer stock level. (The conditions of the new constraint are met at equality and the budget is expended to its upper bound.) This condition can be successfully handled by rounding those variables that are non-integer to the nearest integer that satisfies the corresponding constraint. The resulting solution may be integer

suboptimal but the additional insight provided outweighs the small decrease in MDS availability.

Parametric Analysis of the RHS and Objective Function

Parametric analysis allows a model parameter to vary over a wide range of values and computes changes to the optimal basis and the resultant effect on the optimal objective function value. Advanced parametric analysis allows the specification of a direction to vary the right hand side or objective function vector and then computes changes to the optimal basis and objective function value over a specified range. In the case of multiple changes to the right hand side, a parametric analysis also determines when constraints become binding, non-binding or infeasible. The CPLEX optimization package does not provide a parametric analysis routine as part of the basic package. The Linear, INteractive, and Discrete Optimizer (LINDO) system does offer the capability to conduct a parametric analysis of both the objective function coefficients and the values of the constraint right hand sides (Schrage, 41-46:1991). The MPS format of the model data developed for use with CPLEX was translated to an acceptable format for the LINDO package and loaded there.

Parametric analysis of the budget constraint provides the decision maker with a powerful tool to investigate the impact of budget changes. For example, the Department of Defense regularly conducts budget "what-if" drills where Air Force funding is subject to a certain level of cutbacks. (There are not many drills to determine how to spend excess defense funding.) Decision makers are then tasked with a determination of what impact a certain percentage cut in funds will have on current programs. Figure 4-1 provides a

graph of output from a parametric analysis of the budget constraint in the PLDMq (for parametric output data see Appendix H, page H-1). This graph simulates a thirty percent decrease in the original \$2,700,221.70 budget.

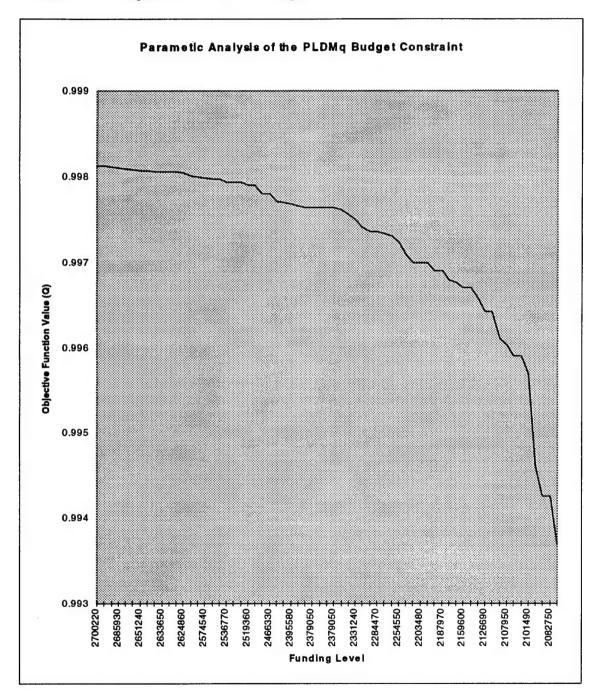


Figure 4-1. Graph of the Parametric Analysis of the PLDMq Budget Constraint

The range of budget values specified in LINDO is from the current funding level to a lower bound of \$1,900,200.00 (an approximate thirty percent decrease). The parametric output data and Figure 4-1 show that the model becomes infeasible below a funding level of \$2,079,520.00. The current formulation forces the purchase of at least the current lower bound stock level of those parts that have sort values greater than the cutoff sort value determined by the original funding allocation and the AAM shopping list. This example parametric analysis shows that a thirty percent cut results in an unacceptable level of availability. To reach this level of reduction, a decrease in the acceptable minimum availability will be required. (If such drastic cuts were to be considered the bounds could be changed to determine the impact.) A review of Figure 4-1 clearly indicates where the drop off in availability accelerates as funding levels decrease, a critical piece of information in a down-sizing agency or company. Additionally, it is possible to determine the cost of achieving a specified level of MDS availability from that data provided by a parametric analysis. The optimal purchases for each LRU at the specified MDS availability are obtained by noting those variables that have left and entered the original optimal basis.

A parametric analysis of more than one element of the RHS vector indicates the impact of potential resource trade offs. For example, the impact of reallocating funds among those certain groups of LRUs that are constrained to a specified sub-budget level can be investigated with a parametric analysis. The direction vector is defined in such a manner that each dollar decrease to one LRU sub-budget is added to another LRU sub-budget.

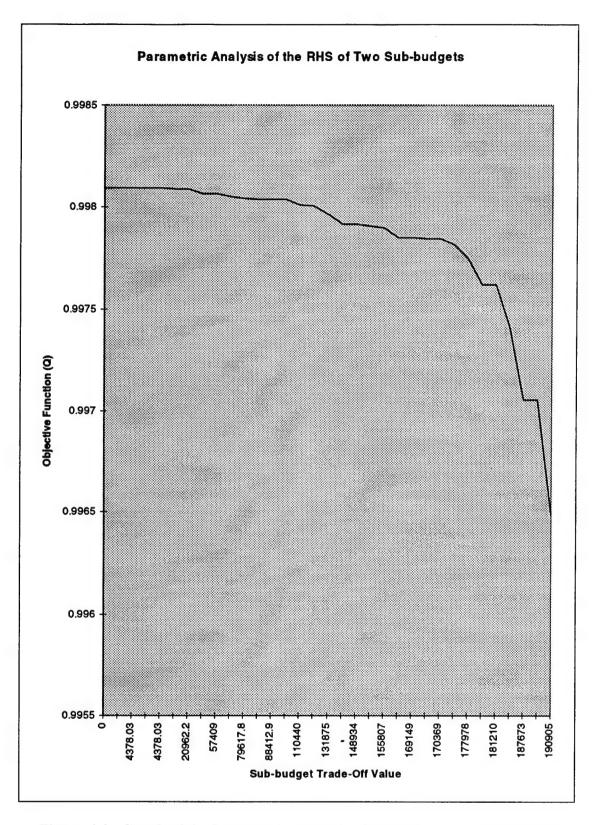


Figure 4-2. Graph of the Parametric Analysis of the RHS of Two Sub-budgets

LINDO output for the parametric analysis of the RHS of two sub-budget constraints is used to construct the graph in Figure 4-2 and can be found in appendix H, page H-2. This type of analysis provides insight to the impact of the allocation of resources. A parametric analysis of multiple constraint right hand sides determines the optimal allocation of program resources. Figure 4-3 is the graph of a specific region of parametric data for the trade-offs in sub-budget allocations. This figure focuses on the region of data that indicates the optimal resource allocation. A reallocation of resources

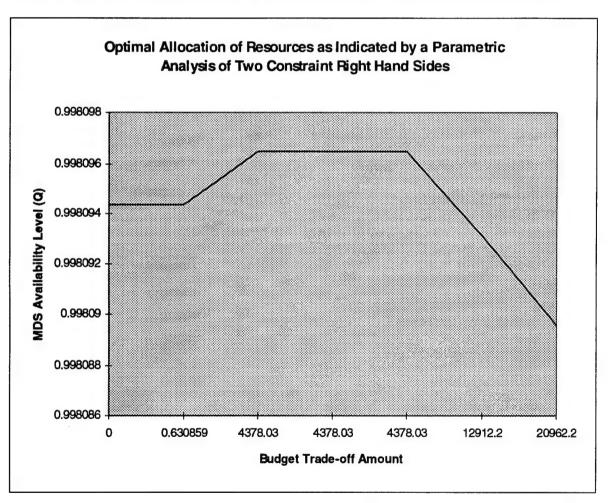


Figure 4-3. The Optimal Allocation of Resources as Indicated by a Parametric Analysis of Two Constraint Right Hand Sides.

between sub-budgets from the initial proposed levels results in an improved overall availability level. The optimal MDS availability level of 0.99809648 is obtained at a budget reallocation of \$4,378.03. This budget reallocation actually results in three alternate optimal inventory positions. A practical analysis similar to this provides the decision maker with a great deal of flexibility and insight that does not currently exist in the AAM.

In addition to budgetary trade-offs, multiple inventory control constraints can be compared to determine the optimal allocation of warehouse storage space. Applications in the parametric modeling arena are limited only by the operational setting and the ability of the analyst to model that setting. The output data includes those variables that have left and entered the optimal basis at each step along the specified direction. Noting the changes at each step provides the analyst with the optimal basic solution and objective function value. A well designed parametric analysis provides the optimal allocation of resources over a specified range of values and eliminates the need for several model runs with various constraint right hand side values.

This reformulation of the AAM, subject to its limiting assumptions, provides the ability to extend the analysis of aircraft availability beyond what is currently available to the Air Force. Given the large funding levels necessary to maintain a mission ready airfleet, building upon the already tested models in METRIC and the AAM appears to be a fruitful area for further research.

<u>V. Summary, Conclusions and Recommendations</u>

Summary of Research Effort

The Aircraft Availability Model provides the Air Force with a worldwide peacetime requirement for reparable spare parts. The Air Force reparable spares program operates on an average annual budget of one billion dollars. This research investigates the environment for reparable spares modeling through an in-depth review of METRIC theory and its applications. A review of modeling techniques used in the U. S. Armed forces and related commercial applications provides insight to the methodology being used in the reparable spares arena.

AAM methodology is modeled as it relates to the concept of diminishing marginal returns in resource application. This research applies three separate modeling techniques toward the goal of a reformulation of the AAM as a mathematical programming model that is a capable tool for the conduct of relevant sensitivity analysis.

The general formulations presented here are continuous non-linear, continuous linear, and piecewise linear discrete/continuous models. The continuous non-linear and linear formulations do not meet the objectives of this research effort for reasons discussed in Chapter IV. Two formulations of the piecewise linear discrete/continuous model are presented. The piecewise linear model based on AAM sort values shows the dominance of an optimization routine relative to the AAM shopping list, a greedy heuristic. Research shows that the optimization approach provides the greatest improvement to MDS availability per dollar spent. The piecewise linear model based on LRU availability rates

provides the capability to maximize not the improvement to availability but the actual MDS availability rate. It has the potential to obtain the highest possible MDS availability from the reparable spares inventory. This mathematical model is discussed in complete detail as a robust platform for conducting extensive post-optimality analysis.

Conclusions

Current AAM methodology provides the Air Force with a good technique to establish reparable spares inventory levels. The AAM and the METRIC family of models are based on sound principles and have provided excellent results since introduced in the 1970s. This research demonstrates the capabilities of mathematical programming models that are based on valid AAM output data. The goal of this study was to provide a mathematical programming model that provides an optimization based inventory position comparable to that found by the AAM that is capable of a robust sensitivity analysis. Research shows that the proposed reformulation of the AAM provides a higher level of MDS availability while adding a full complement of post-optimality analysis tools.

The suggested reformulation is based entirely on AAM output data. The implementation of the proposed mathematical model requires valid LRU availability rates as calculated by the AAM. Considering the sensitive nature of the model and the solution technique, data accuracy is of the utmost importance. In addition, the data must provide monotonic and concave breakpoints in the piecewise linear model. The strongest attribute of the piecewise linear models investigated here is the capability to provide a discrete solution with continuous variables. Large continuous variable models can be solved with relative speed and ease and provide the capability for post-optimality analysis.

Implementation of a piecewise linear discrete/continuous reformulation of the AAM will provide the Air Force with the highest level of MDS availability per dollar spent on reparable spares inventory levels while adding the capability to conduct extensive sensitivity analysis.

Recommendations for Future Research

Data preprocessing is the main area of concern with respect to implementing the proposed model. Generation of accurate data that meet the model assumptions is a critical requirement for successful results with the piecewise linear formulation. An automated system that can handle the sorting, filtering, and marginal analysis of the AAM output data would be a valuable asset in the implementation of a full scale model. Furthermore, an automated tool that translates the resultant data set to MPS format would be highly advantageous. This translation can be achieved either directly from a text file of data or from a spreadsheet application.

Recall from Chapter IV that the AAM assumes equal bases. Air Force Materiel

Command has expressed interest in developing a formulation that models unequal bases.

The modeling techniques presented in this study provide a sound framework upon which a model of that nature can be based.

The CPLEX optimization package is a powerful tool that solves extremely large models with relative speed and ease. The current package does not provide a parametric programming capability. The CPLEX callable library and FORTRAN or C programming languages can support a parametric analysis routine. (The CPLEX Optimization, Inc. manual, <u>Using the CPLEX Callable Library</u>, provides a tutorial on the use of CPLEX

(pp.3-23) and shows examples of using the CPLEX Callable Library with FORTRAN and C (pp.287-309).) CPLEX is a widely accepted optimization package so research in this area would be widely applicable.

Appendix A. Functional Approximation of A AM LRU Availability data .

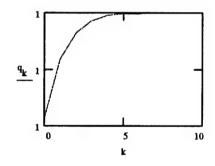
Technique 1. Three point quadratic approximation.

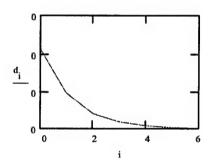
All analysis is based on AAM output data for NSN 1005012982522.

The three points used for the quadratic approximation technique are the LRU lower bound, the AAM optimal buy position, and the LRU upper bound.

$$\mathbf{q} := \begin{bmatrix} .99962185 \\ .99983549 \\ .99993070 \\ .99997159 \\ .99998862 \\ .99999553 \\ .99999827 \\ .99999934 \end{bmatrix} \qquad \begin{aligned} \mathbf{k} &:= 0... 7 \\ \mathbf{i} &:= 0... 6 \\ \mathbf{d_i} &:= \mathbf{q_{i+1}} - \mathbf{q_i} \end{aligned} \qquad \mathbf{d} = \begin{bmatrix} 2.136400000000149^{\bullet} 10^{-4} \\ 9.5209999999999121^{\bullet} 10^{-5} \\ 4.089000000007115^{\bullet} 10^{-5} \\ 1.70299999999997346^{\bullet} 10^{-5} \\ 6.9099999999971106^{\circ} 10^{-6} \\ 2.740000000001075^{\bullet} 10^{-6} \\ 1.0700000000047422^{\bullet} 10^{-6} \end{bmatrix}$$

d is a vector indicating the region of test data is increasing at a decreasing rate.





These graphs confirm the fact that the values are strictly decreasing at a decreasing rate and smooth (monotonic and concave).

$$\mathbf{q_0} = 0.999962185$$
 $\mathbf{q_3} = 0.99997159$
 $\mathbf{q_7} = 0.99999934$

$$Q := \begin{bmatrix} \left(x_{0}\right)^{2} & x_{0} & 1 \\ \left(x_{3}\right)^{2} & x_{3} & 1 \\ \left(x_{7}\right)^{2} & x_{7} & 1 \end{bmatrix} \qquad q2 := \begin{bmatrix} q_{0} \\ q_{3} \\ q_{7} \end{bmatrix} \qquad \begin{pmatrix} a \\ b \\ c \end{pmatrix} := Q^{-1} \cdot q2 \qquad \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{bmatrix} -1.566321428572715 \cdot 10^{-5} \\ 1.635696428571865 \cdot 10^{-4} \\ 0.99962185 \end{bmatrix}$$

The matrix manipulation shown here determines the parameters of the quadratic: a, b, and c.

$$qfit_{k} := a \cdot (x_{k})^{2} + b \cdot x_{k} + c$$

error
$$_{\mathbf{k}} := \mathbf{qfit}_{\mathbf{k}} - \mathbf{q}_{\mathbf{k}}$$

$$error_k := qfit_k - q_k$$
 $sqerr_k := (error_k)^2$

qfit k
0.99962185
0.999769756428571
0.999886336428572
0.99997159
1.000025517142857
1.000048117857143
1.000039392142857
0.9999934

$q_{\mathbf{k}}$
0.99962185
0.99983549
0.9999307
0.99997159
0.99998862
0.99999553
0.99999827
0.99999934

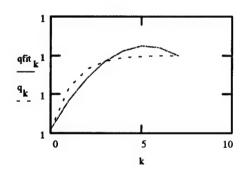
error k
0
$-6.573357142858338 \cdot 10^{-5}$
-4.436357142845182 ·10 ⁻⁵
0
$3.689714285715073 \cdot 10^{-5}$
5.258785714279401 ·10 ⁻⁵
$4.112214285700855 \cdot 10^{-5}$
0

sqerr k
0
0.000000004320902
0.000000001968126
0
0.000000001361399
0.000000002765483
0.000000001691031
0

sse :=
$$\sum_{k=1}^{6} sqerr_{k}$$

sse = 1.210694138568814 •10⁻⁸

The error analysis of the quadratic fit indicates a strong relationship between the derived function and the actual data. Notice the error of the fitted points is zero and intermediate points are within 10⁻⁵ accuracy.



This graph of the fitted and actual data shows a violation of the strictly increasing assumption by the three point quadratic fit.

Technique 2. Quadratic least squares approximation.

The three point quadratic is not monotonic so a least squares technique is applied in an attempt to remedy this condition.

$$q := \begin{bmatrix} .99962185 \\ .99983549 \\ .99993070 \\ .99997159 \\ .99998862 \\ .999998553 \\ .999999827 \\ .99999934 \end{bmatrix}$$

$$k := 0... 7$$

$$x_k := k$$

$$\mathbf{x} = \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{bmatrix} \qquad \mathbf{x} := \begin{bmatrix} 1 & \mathbf{x}_{0} & (\mathbf{x}_{0})^{2} \\ 1 & \mathbf{x}_{1} & (\mathbf{x}_{1})^{2} \\ 1 & \mathbf{x}_{2} & (\mathbf{x}_{2})^{2} \\ 1 & \mathbf{x}_{3} & (\mathbf{x}_{3})^{2} \\ 1 & \mathbf{x}_{4} & (\mathbf{x}_{4})^{2} \\ 1 & \mathbf{x}_{5} & (\mathbf{x}_{5})^{2} \\ 1 & \mathbf{x}_{6} & (\mathbf{x}_{6})^{2} \\ 1 & \mathbf{x}_{7} & (\mathbf{x}_{7})^{2} \end{bmatrix} \qquad \mathbf{X} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 1 \\ 1 & 2 & 4 \\ 1 & 3 & 9 \\ 1 & 4 & 16 \\ 1 & 5 & 25 \\ 1 & 6 & 36 \\ 1 & 7 & 49 \end{bmatrix}$$

$$\mathbf{a} := (\mathbf{X}^{T} \cdot \mathbf{X})^{-1} \cdot \mathbf{X}^{T} \cdot \mathbf{q} \qquad \mathbf{a} = \begin{bmatrix} 0.999664944583336 \\ 1.435669642855242 \cdot 10^{-4} \\ 1 & 1 & 1 & 1 \\ 1 & 2 & 4 \\ 1 & 3 & 9 \\ 1 & 4 & 16 \\ 1 & 5 & 25 \\ 1 & 6 & 36 \\ 1 & 7 & 49 \end{bmatrix} \qquad \mathbf{a} \text{ is a estim param}$$

$$\mathbf{X} = \begin{bmatrix} 1 & 0 & 0 \\ 1 & 1 & 1 \\ 1 & 2 & 4 \\ 1 & 3 & 9 \\ 1 & 4 & 16 \\ 1 & 5 & 25 \\ 1 & 6 & 36 \\ 1 & 7 & 49 \end{bmatrix}$$

$$a := (\mathbf{X}^{T} \cdot \mathbf{X})^{-1} \cdot \mathbf{X}^{T} \cdot \mathbf{q}$$

$$a = \begin{bmatrix} 0.999664944583336 \\ 1.435669642855242 \cdot 10^{-4} \\ -1.427172619052064 \cdot 10^{-5} \end{bmatrix}$$

a is a vector of the least squares estimates of the quadratic parameters.

$$qfit_k := a_0 + a_1 \cdot x_k + a_2 \cdot (x_k)^2$$

$$\operatorname{error}_{\mathbf{k}} := \operatorname{qfit}_{\mathbf{k}} - \operatorname{q}_{\mathbf{k}}$$

$$\operatorname{error}_{k} := \operatorname{qfit}_{k} - \operatorname{q}_{k} \qquad \operatorname{sqerr}_{k} := (\operatorname{error}_{k})^{2}$$

qfit k
0.999664944583336
0.999794239821431
0.999894991607145
0.999967199940478
1.00001086482143
1.000025986250001
1.000012564226191
0.999970598749999

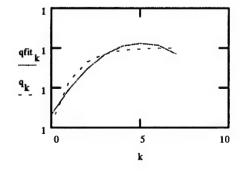
q_k
0.99962185
0.99983549
0.9999307
0.99997159
0.99998862
0.99999553
0.99999827
0.99999934

error k
$4.309458333606742 \cdot 10^{-5}$
$-4.12501785689301 \cdot 10^{-5}$
$-3.570839285482741 \cdot 10^{-5}$
$-4.390059522019207 \cdot 10^{-6}$
$2.224482142987316 \cdot 10^{-5}$
$3.045625000075436 \cdot 10^{-5}$
$1.429422619059206 \cdot 10^{-5}$
$-2.874125000074113 \cdot 10^{-5}$

sqerr k
0.000000001857143
0.000000001701577
0.000000001275089
0.000000000019273
0.000000000494832
0.000000000927583
0.000000000204325
0.000000000826059

$$sse := \sum_{k=0}^{5} sqerr_{k}$$

sse =
$$6.275497532314834 \cdot 10^{-9}$$



The quadratic fit in this case provides a lower sum of squared errors than the three point approximation but is still not monotonic in the modeling region.

Technique 3. Cubic least squares approximation.

$$\mathbf{x} = \begin{bmatrix} 0 \\ 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{bmatrix} \qquad \mathbf{X} := \begin{bmatrix} 1 & \mathbf{x}_0 & (\mathbf{x}_0)^2 & (\mathbf{x}_0)^3 \\ 1 & \mathbf{x}_1 & (\mathbf{x}_1)^2 & (\mathbf{x}_1)^3 \\ 1 & \mathbf{x}_2 & (\mathbf{x}_2)^2 & (\mathbf{x}_2)^3 \\ 1 & \mathbf{x}_3 & (\mathbf{x}_3)^2 & (\mathbf{x}_3)^3 \\ 1 & \mathbf{x}_4 & (\mathbf{x}_4)^2 & (\mathbf{x}_4)^3 \\ 1 & \mathbf{x}_5 & (\mathbf{x}_5)^2 & (\mathbf{x}_5)^3 \\ 1 & \mathbf{x}_6 & (\mathbf{x}_6)^2 & (\mathbf{x}_6)^3 \\ 1 & \mathbf{x}_7 & (\mathbf{x}_7)^2 & (\mathbf{x}_7)^3 \end{bmatrix} \qquad \mathbf{X} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \\ 1 & 2 & 4 & 8 \\ 1 & 3 & 9 & 27 \\ 1 & 4 & 16 & 64 \\ 1 & 5 & 25 & 125 \\ 1 & 6 & 36 & 216 \\ 1 & 7 & 49 & 343 \end{bmatrix}$$

$$\mathbf{a} := \left(\mathbf{X}^{\mathsf{T}} \cdot \mathbf{X}\right)^{-1} \cdot \mathbf{X}^{\mathsf{T}} \cdot \mathbf{q} \qquad \mathbf{a} = \begin{bmatrix} 0.999629848333403 \\ 2.354857142551903 & {}^{\bullet}10^{-4} \\ -4.936797618843025 & {}^{\bullet}10^{-5} \\ 3.342499999899051 & {}^{\bullet}10^{-6} \end{bmatrix}$$

$$qfit_{k} := a_{0} + a_{1} \cdot x_{k} + a_{2} \cdot \left(x_{k}\right)^{2} + a_{3} \cdot \left(x_{k}\right)^{3} \qquad \qquad error_{k} := qfit_{k} - q_{k} \qquad \qquad sqerr_{k} := \left(error_{k}\right)^{2}$$

qtit k
0.999629848333403
0.99981930857147
0.999930087857159
0.99998224119047
0.999995823571402
0.999990889999955
0.999987495476129
1.000005694999921

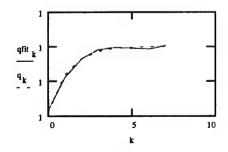
q_k
0.99962185
0.99983549
0.9999307
0.99997159
0.99998862
0.99999553
0.99999827
0.99999934

error k	
$7.998333402703395 \cdot 10^{-6}$	
- 1.618142853054838	·10 ⁻⁵
- 6.121428413052854	·10 ⁻⁷
$1.065119046972374 \cdot 10^{-5}$	
$7.203571402158993 \cdot 10^{-6}$	
-4.640000044520143	·10 ⁻⁶
- 1.07745238714374	·10 ⁻⁵
$6.354999921409643 \cdot 10^{-6}$	

0.000	000000063973
0.000	000000261839
0.000	000000000375
0.000	0000000113448
0.000	000000051891
0.000	000000002153
0.000	000000011609
	000000040386

sse :=
$$\sum_{k=0}^{5} sqerr_{k}$$

sse = 5.130555851496908 •10⁻¹⁰



The cubic approximation provides a lower sum of squared errors than the quadratic. This graph shows that the cubic is neither concave nor monotonic.

Technique 4. Three point exponential approximation.

The exponential approximation is derived using the same points as the initial quadratic fit. The form of the exponential is c-ae bx;=q;.

$$q := \begin{bmatrix} .99962185 \\ .99983549 \\ .99993070 \\ .99997159 \\ .99998862 \\ .99999827 \\ .99999934 \end{bmatrix}$$

$$k := 0...7$$

$$x_k := 5 + k$$

Note: The current Air Force inventory of 5 parts is included here to scale the problem to an acceptable level for the Mathcad symbolic processor.

$$\frac{e^{x_6 \cdot b} - e^{x_0 \cdot b}}{e^{x_6 \cdot b} - e^{x_3 \cdot b}} \frac{q_0 - q_6}{q_3 - q_6}$$

$$\frac{e^{x_6 \cdot b} - e^{x_0 \cdot b}}{e^{x_6 \cdot b} - e^{x_3 \cdot b}} = \frac{q_0 - q_6}{q_3 - q_6}$$

$$\frac{q_0 - q_6}{q_3 - q_6} = 14.10869565220015$$

$$\frac{e^{11 \cdot b} - e^{5 \cdot b}}{e^{11 \cdot b} - e^{8 \cdot b}} = 14.10869565220015$$

The Mathcad symbolic processor solves the equality shown here for the values of b which satisfy the equation.

b :=-.85775860008003064492

$$a := \frac{q_3 - q_6}{e^{11 \cdot b} - e^{8 \cdot b}}$$

$$a = 0.027593485148153$$

$$c := q_6 + a \cdot e^{b \cdot x_6}$$

$$c = 1.000000473375224$$

The values for a and c are found here. The value for c is assumed to be one for all exponential approximations used in this study.

$$qfit_k := c - a \cdot e^{b \cdot x_k}$$

qfit _k
0.99962185
0.99983989480161
0.999932370135986
0.99997159
0.999988223600123
0.999995278103243
0.99999827
0.999999538898185

0.99962185 0.99997159 0.99998862 0.99999553 0.9999982 0.99999934

$$error_k := qfit_k - q_k$$

error _k
0
4.404801610236042·10 ⁻⁶
1.670135986509003·10 ⁻⁶
0
- 3.96399877145015·10 ⁻⁷
-2.518967572306963·10 ⁻⁷
0
1.988981850331584·10 ⁻⁷

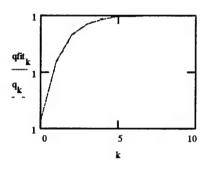
sqerr	_k := (error k)2
squi	k'-\	k.	1

sqerr k
0
0.000000000019402
0.0000000000002789
0
0.0000000000000157
0.0000000000000063
0
0.000000000000004

$$sse := \sum_{k=1}^{6} sqerr_{k}$$

 $sse = 2.241221627787435 \cdot 10^{-11}$

The fit for the exponential function is the best of those attempted in this study. The sum of squared error is three orders of magnitude better than that of the quadratic fit. The least squares exponential fit is determined using Microsoft EXCEL for each LRU included in those models in this study.



Appendix B. The Continuous Non-Linear Program

of the form $\ln(a) + b^*x = \ln(1-q)$ and translated to the non-linear form. The objective function is the maximum of the sum of the natural logarithm of q for each LRU, constrained by the budget and each LRU's acceptable range of stock levels. The functions for each LRU are based on output data for the F-15E MDS and are of the form 1-a*exp(b*x)=q. This Microsoft EXCEL workbook provides a nonlinear reformulation of the Aircraft Availability Model. The parameters of the exponential (a and b) are derived using a linear least squares regression technique

יו חור וומנח		o linear		Variables	Vorights Citted arms Drive C. t. Dude	Drive Or su	ot Dudget			Oh: Ean
NCN.1	1005012082522	0.00041062	0.00014223	7	2	16.96	76778 3323	LOWCI DIIG		4E 05
CNI O	1000012502222	0.00041002	-0.50514223	2.2021344	0.999900132	12074 62	70055 0455	I	0	-4E-03
NSN-7	12/0013362384FA	0.00010236	-0.44313548	7.208/201	0.999961536	139/4.63	30866.0466	I	3	-3.8E-05
NSN-3	1560012912590FX	0.00168836	-0.58961422	5	0.999911461	3231.73	16158.65	0	5	-8.9E-05
NSN-4	1620012409687	0.00119007	-0.32992158	0	0.998809927	75403.35	0	0	0	-0.00119
NSN-5	1630012251893	0.12384435	-0.05228081	125	0.99982023	8795.12	1099390	125	131	-0.00018
9-NSN	1650012511153	0.00001616	-0.32485814	0	0.999983844	82240	0	0	0	-1.6E-05
NSN-7	1650013969218	0.00011345	-0.74676460	1	0.999946235	46000	46000	1	2	-5.4E-05
NSN-8	1650013980036	0.00111488	-0.55967646	0	0.99888512	36000	0	0	0	-0.00112
NSN-9	1660013387046BO	0.00060903	-0.62058812	3	0.999905357	57681.59	173044.77	3	9	-9.5E-05
NSN-10	1660013389649BO	0.00668540	-0.60584181	8.6671774	0.999964951	17408.46	150882.211	5	13	-3.5E-05
NSN-11	1680012283821	0.00001393	-0.76880881	0	0.999986071	19672.91	0	0	0	-1.4E-05
NSN-12	1680012283822	0.00000316	-0.80471896	0	0.999996845	20131.4	0	0	0	-3.2E-06
NSN-13	2835012180143	0.00036743	-0.24335330	1	0.999711936	67393.87	67393.87	1	4	-0.00029
NSN-14	2835012188080	0.00000746	-0.20339569	1	0.999993911	70669.82	70669.82	1	4	-6.1E-06
NSN-15	4810012518480HS	0.00000254	-1.58266767	0	0.99999746	13986	0	0	0	-2.5E-06
NSN-16	4810012537542	0.00614650	-0.67215120	9.8954387	0.999992056	4377.4	43316.2936	7	13	-7.9E-06
NSN-17	4810013377136TP	0.00006043	-0.48985035	2.2529203	0.999979958	8050	18136.0084	1	5	-2E-05
NSN-18	5821012483022FX	0.00024518	-0.53032270	3.4553707	0.999960767	17058.08	58941.9907	2	9	-3.9E-05
NSN-19	5895012913073FX	0.00005469	-0.64388566	7	0.999999397	8338.98	58372.86	7	11	-6E-07
NSN-20	5895013640160LN	0.00270954	-1.38879930	3.2531185	0.999970435	33661.84	109505.956	2	9	-3E-05
NSN-21	5895013823225FX	0.00083508	-0.39531865	4	0.999828214	53030.98	212123.92	2	4	-0.00017
NSN-22	5985013902368EW	0.00357285	-0.39528303	11.291135	0.999958821	13342.04	150646.78	6	14	-4.1E-05
NSN-23	5985013934820EW	0.00051209	-0.70941160	5.0159004	0.999985412	8484.08	42555.3003	2	8	-1.5E-05
NSN-24	5998013410403FX	0.00003264	-0.46259325	1	0.999979451	17142.59	17142.59	1	3	-2.1E-05
NSN-25	6110012305147	0.00000170	-0.10819770	0	0.999998302	11429.91	0	0	0	-1.7E-06
NSN-26	6605012400136FX	0.00435235	-0.15738695	6	0.998944269	15505.66	139550.94	4	6	-0.00106
NSN-27	6610013195039	0.02439354	-0.24717362	36	0.999996667	3313.76	119295.36	36	42	-3.3E-06
NSN-28	6615012444251	0.00001338	-1.02304883	0	0.999986619	44301.56	0	0	0	-1.3E-05
NSN-29	6615013462155	0.00002089	-0.38083218	0	0.999979107	13861	0	0	0	-2.1E-05
NSN-30	6615013527003	0.00097102	-0.27275089	0	0.999028979	32725.3	0	0	0	-0.00097
					0.994436557		2700221.7			-0.00558

Appendix C. The Continuous Linear Program

The functions for each LRU are based on output data for the F-15E MDS and are of the form ln(a)+bx=ln(1-q). of the form $\ln(a) + b^*x = \ln(1-q)$. The objective function here is the minimum of the sum of natural log of 1-q The parameters of the linear approximation were derived using a linear least squares regression technique This Microsoft EXCEL workbook provides a linear reformulation of the Aircraft Availability Model. for each LRU, constrained by the budget and each LRU's acceptable range of stock levels.

		In(a)	h	Variables	Variables Objective Fcn	Price	st. Budget	I ower bud	I Inner hnd
NSN-1	1005012982522	-7.79785021	-0.90914223	1	2	29716.86		I	5
NSN-2	1270013562584FX	-9.18703138	-0.44313548	2.447969	-10.27181326	13974.63	34209.46	-	3
NSN-3	1560012912590FX	-6.38399507	-0.58961422	5	-9.332066153	3231.73	16158.65	0	5
NSN-4	1620012409687	-6.73374072	-0.32992158	0	-6.733740716	75403.35	0	0	0
NSN-5	1630012251893	-2.08872971	-0.05228081	125	-8.623830471	8795.12	1099390	125	131
9-NSN	1650012511153	-11.03318686	-0.32485814	0	-11.03318686	82240	0	0	0
NSN-7	1650013969218	-9.08413158	-0.74676460	1	-9.830896176	46000	46000	-	2
NSN-8	1650013980036	-6.79900823	-0.55967646	0	-6.799008228	36000	0	0	0
6-NSN	1660013387046BO	-7.40363622	-0.62058812	3	-9.265400582	57681.59	173044.77	3	9
NSN-10	1660013389649BO	-5.00782883	-0.60584181	13	-12.88377239	17408.46	226309.98	5	13
NSN-11	1680012283821	-11.18151106	-0.76880881	0	-11.18151106	19672.91	0	0	0
NSN-12	1680012283822	-12.66652254	-0.80471896	0	-12.66652254	20131.4	0	0	0
NSN-13	2835012180143	-7.90897545	-0.24335330	1	-8.152328748	67393.87	67393.87		4
NSN-14	2835012188080	-11.80569868	-0.20339569	1	-12.00909437	70669.82	70669.82		4
NSN-15	4810012518480HS	-12.86772116	-1.58266767	0	-12.86772116	13986	0	0	0
NSN-16	4810012537542	-5.09187294	-0.67215120	13	-13.82983848	4377.4	290695	7	13
NSN-17	4810013377136TP	-9.71409968	-0.48985035	5	-12.16335141	8050	40250	-	5
NSN-18	5821012483022FX	-8.31353708	-0.53032270	2	-9.374182471	17058.08	34116.16	2	9
NSN-19	5895012913073FX	-9.81377565	-0.64388566	11	-16.89651786	8338.98	91728.78	L	11
NSN-20	5895013640160LN	-5.91097487	-1.38879930	9	-14.24377065	33661.84	201971.04	2	9
NSN-21	5895013823225FX	-7.08798666	-0.39531865	2	-7.878623958	53030.98	106061.96	7	4
NSN-22	5985013902368EW	-5.63439104	-0.39528303	6	-9.191938305	13342.04	120078.36	6	14
NSN-23	5985013934820EW	-7.57700415	-0.70941160	8	-13.25229698	8484.08	67872.64	2	∞
NSN-24	5998013410403FX	-10.33011201	-0.46259325	1	-10.79270527	17142.59	17142.59	I	3
NSN-25		-13.28597119	-0.10819770	0	-13.28597119	11429.91	0	0	0
NSN-26	6605012400136FX	-5.43703911	-0.15738695	4	-6.066586908	15505.66	62022.64	7	6
NSN-27	6610013195039	-3.71343697	-0.24717362	42	-14.0947289	3313.76	139177.92	98	42
NSN-28		-11.22168162	-1.02304883	0	-11.22168162	44301.56	0	0	0
NSN-29	6615013462155	-10.77608277	-0.38083218	0	-10.77608277	13861	0	0	0
NSN-30	NSN-30 6615013527003	-6.93716278	-0.27275089	0	-6.937162776	32725.3	0	0	0

-320.3633247

Appendix D. Applic	cation of A	AM Methodology to a	Subset of Data-The Sh	opping	List	
This workbook uses	an explicitly	defined subset of F-15	E AAM output data			
and applies AAM me	thodology t	o determine the optimal	buy postition.			
An alternate formulat	ion of the n	nodel is then compared t	o those items			
selected from the "sh	opping list"	of this subset of data.				
The AAM Shopping	List					
The cut-off sort value	for the firs	t arbitrary budget level	is indicated by this shad	ing:		
The cut-off sort value	for the 2nd	l arbitrary budget level i	s indicated by this shadi	ng:		
NSN	Pro. Cost	Sort Value	ln(q)	stk lvl	Budget at SV	Accum. Bud.
1660013389649BO	17408.46	0.0000000161834380	-0.0003755004914860	5	87042.3	87042.3
5895013640160LN	33661.84	0.0000000147218310	-0.0001960792222744	2	67323.68	154365.98
4810012537542	4377.4	0.0000000142968630	-0.0000638120359447	7	30641.8	185007.78
5985013934820EW	8484.08	0.0000000140849990	-0.0001263979878891	2	16968.16	201975.94
1660013389649BO	17408.46	0.0000000094993569	-0.0002101320761984	6	17408.46	219384.4
5895012913073FX	8338.98	0.0000000086909139	-0.0000006300001984	7	58372.86	277757.26
5985013934820EW	8484.08	0.0000000073765321	-0.0000638120359447	3	8484.08	286241.34
4810012537542	4377.4	0.0000000073335550	-0.0000317105027727	8	4377.4	290618.74
1005012982522	29716.86	0.0000000071909388	-0.0001645235332543	1	29716.86	320335.6
5821012483022FX	17058.08	0.0000000070057637	-0.0001869974829395	2	34116.16	354451.76
1660013389649BO	17408.46	0.0000000054413007	-0.0001154066590923	7	17408.46	371860.22
4810013377136TP	8050	0.0000000052874417	-0.0000393507742316	1	8050	379910.22
6610013195039	3313.76	0.0000000048854066	-0.0000052200136243	36	119295.36	499205.58
5895012913073FX	8338.98	0.0000000045907435	-0.0000002500000313	8	8338.98	507544.56
1560012912590FX	3231.73	0.0000000044178821	-0.0014396958649220	0	0	507544.56
6605012400136FX	15505.66	0.0000000043742659	-0.0026404930354171	4	62022.64	569567.2
5895013640160LN	33661.84	0.0000000043388930	-0.0000500212510419	3	33661.84	603229.04
5985013902368EW	13342.04	0.00000000040514446	-0.0001141165110413	9	120078.36	723307.4
5985013934820EW	8484.08	0.0000000037837814	-0.0000317105027727	4	8484.08	731791.48
6605012400136FX	15505.66	0.0000000037567421	-0.0015530153042349	5	15505.66	747297.14
4810012537542	4377.4	0.0000000036945283	-0.0000155401207471	9	4377.4	751674.54
6610013195039	3313.76	0.0000000036715338	-0.0000013400008978	37	3313.76	754988.3
5821012483022FX	17058.08	0.0000000036690270	-0.0001187470501519	3	17058.08	772046.38
5895013823225FX	53030.98	0.0000000032711363	-0.0003607950787175	2	106061.96	878108.34
6605012400136FX	15505.66	0.0000000032124378	-0.0012395479222008	6	15505.66	893614
1005012982522	29716.86	0.0000000032043008	-0.0000693024013560	2	29716.86	923330.86
1660013389649BO	17408.46	0.0000000030497431	-0.0000623219419718	8	17408.46	940739.32
4810013377136TP	8050	0.0000000029897004	-0.0000219302404659	2	8050	
1560012912590FX	3231.73		-0.0008674961660170	1	3231.73	
5985013902368EW	13342.04		-0.0000769729623424	10	13342.04	

6610013195039 6605012400136FX	3313.76	0.0000000027473313 -0.0000010500005512	38	3313.76	968676.85
6605012400136FX				3313170	700070.03
	15505.66	0.0000000026931256 -0.0011200670409569	7	15505.66	984182.51
1630012251893	8795.12	0.0000000026855104 -0.0002642249043258	125	1099390	2083572.51
1630012251893	8795.12	0.0000000025371144 -0.0002544423677140	126	8795.12	2092367.63
1630012251893	8795.12	0.000000023962592 -0.0002452400688876	127	8795.12	2101162.75
6605012400136FX	15505.66	0.000000022839261 -0.0010140840094248	8	15505.66	2116668.41
1630012251893	8795.12	0.0000000022626032 -0.0002365779823642	128	8795.12	2125463.53
1630012251893	8795.12	0.0000000021358174 -0.0002284260872523	129	8795.12	2134258.65
6610013195039	3313.76	0.000000020472842 -0.0000008400003528	39	3313.76	2137572.41
1630012251893	8795.12	0.0000000020155859 -0.0002207743688676	130	8795.12	2146367.53
6610013195039	3313.76	0.000000019755079 -0.0000006600002178	40	3313.76	2149681.29
6610013195039	3313.76	0.000000019298320 -0.0000005100001301	41	3313.76	2152995.05
6605012400136FX	15505.66	0.000000019291702 -0.0009153788313963	9	15505.66	2168500.71
5985013934820EW	8484.08	0.000000019062088 -0.0000155401207471	5	8484.08	2176984.79
1630012251893	8795.12	0.000000019016047 -0.0002135728050480	131	8795.12	2185779.91
5985013902368EW	13342.04	0.000000018996085 -0.0000516213323581	11	13342.04	2199121.95
6610013195039	3313.76	0.000000018841562 -0.0000003900000760	42	3313.76	2202435.71
5821012483022FX	17058.08	0.000000018820221 -0.0000629319801755	4	17058.08	2219493.79
4810012537542	4377.4	0.000000018321009 -0.0000075200282754	10	4377.4	2223871.19
5895013823225FX	53030.98	0.000000017959398 -0.0002655552566763	3	53030.98	2276902.17
5895013823225FX	53030.98	0.000000017741379 -0.0001714747009463	4	53030.98	2329933.15
1560012912590FX	3231.73	0.000000017456548 -0.0005127214191654	2	3231.73	2333164.88
1660013389649BO	17408.46	0.000000016763722 -0.0000331305488106	9	17408.46	2350573.34
4810013377136TP	8050	0.000000016693150 -0.0000111500621617	3	8050	2358623.34
1660013387046BO	57681.59	0.000000016509086 -0.0000838235130925	3	173044.77	2531668.11
1005012982522	29716.86	0.000000013760097 -0.0000284104035717	3	29716.86	2561384.97
4810013377136TP	8050	0.000000013728717 -0.0000070900251342	4	8050	2569434.97
5985013902368EW	13342.04	0.000000012878343 -0.0000344405930704	12	13342.04	2582777.01
4810013377136TP	8050	0.000000012087739 -0.0000049000120050	5	8050	2590827.01
5895013640160LN	33661.84	0.000000011372132 -0.0000117400689144	4	33661.84	2624488.85
5895012913073FX	8338.98	0.000000010990673 -0.0000001400000098	9	8338.98	2632827.83
2835012180143	67393.87	0.000000010694991 -0.0002710667352681	1	67393.87	2700221.7
1560012912590FX	3231.73	0.000000010569970 -0.0002979043691005	3	3231.73	2703453.43
5895012913073FX	8338.98	0.000000009866293 -0.000000600000018	10	8338.98	2711792.41
5821012483022FX	17058.08	0.0000000009481328 -0.0000112700635069	5	17058.08	2728850.49
5985013934820EW	8484.08	0.0000000009452809 -0.0000075200282754	6	8484.08	2737334.57
5895012913073FX	8338.98	0.0000000009163556 -0.000000100000001	11	8338.98	2745673.55
1660013389649BO	17408.46	0.0000000009054756 -0.0000173701508602	10	17408.46	2763082.01
4810012537542	4377.4	0.000000008959681 -0.0000036000064800	11	4377.4	2767459.41
5985013902368EW	13342.04	0.0000000008677973 -0.0000228702615224	13	13342.04	2780801.45
5821012483022FX	17058.08	0.000000008488365 -0.0000073500270113	6	17058.08	2797859.53
2835012180143	67393.87	0.000000008328215 -0.0002149330964632	2	67393.87	2865253.4
		0.0000000007534311 -0.0000192901860544	1	17142.59	2882395.99

1660013387046BO	57681.59	0.00000000007089429	-0.0000667922305514	4	57681.59	2940077.58
1560012912590FX	3231.73	0.0000000006269877	-0.0001704845316620	4	3231.73	2943309.31
2835012180143	67393.87	0.00000000006059478	-0.0001740951536818	3	67393.87	3010703.18
5985013902368EW	13342.04	0.0000000005814403	-0.0000151101141572	14	13342.04	3024045.22
1005012982522	29716.86	0.0000000005730797	-0.0000113800647527	4	29716.86	3053762.08
2835012180143	67393.87	0.0000000005450212	-0.0001373694347488	4	67393.87	3121155.95
1660013389649BO	17408.46	0.0000000004814117	-0.0000089900404103	11	17408.46	3138564.41
5998013410403FX	17142.59	0.0000000004678330	-0.0000112700635069	2	17142.59	3155707
5985013934820EW	8484.08	0.0000000004622789	-0.0000036000064800	7	8484.08	3164191.08
4810012537542	4377.4	0.0000000004327756	-0.0000017100014621	12	4377.4	3168568.48
1270013562584FX	13974.63	0.0000000003722626	-0.0000664422072346	1	13974.63	3182543.11
1560012912590FX	3231.73	0.000000003652814	-0.0000962446313659	5	3231.73	3185774.84
1270013562584FX	13974.63	0.0000000003590310	-0.0000281603965003	2	13974.63	3199749.47
1660013387046BO	57681.59	0.0000000002952601	-0.0000598817928788	5	57681.59	3257431.06
5895013640160LN	33661.84	0.0000000002722596	-0.0000025800033282	5	33661.84	3291092.9
1660013387046BO	57681.59	0.0000000002581623	-0.0000510113010543	6	57681.59	3348774.49
1660013389649BO	17408.46	0.0000000002523052	-0.0000046000105801	12	17408.46	3366182.95
1005012982522	29716.86	0.0000000002326117	-0.0000044700099905	5	29716.86	3395899.81
5998013410403FX	17142.59	0.0000000002287884	-0.0000073500270113	3	17142.59	3413042.4
5985013934820EW	8484.08	0.0000000002232926	-0.0000017100014621	8	8484.08	3421526.48
4810012537542	4377.4	0.00000000002067420	-0.0000008000003200	13	4377.4	3425903.88
1650013969218	46000	0.0000000001556203	-0.0000617619072273	1	46000	3471903.88
1650013969218	46000	0.0000000001556144	-0.0000234802756595	2	46000	3517903.88
1660013389649BO	17408.46	0.0000000001305148	-0.0000023300027145	13	17408.46	3535312.34
5895013640160LN	33661.84	0.00000000000606521	-0.0000005300001404	6	33661.84	3568974.18
2835012188080	70669.82	0.0000000000357204	-0.0000069300240125	1	70669.82	3639644
2835012188080	70669.82	0.0000000000250328	-0.0000051600133128	2	70669.82	3710313.82
2835012188080	70669.82	0.0000000000174683	-0.0000039300077225	3	70669.82	3780983.64
2835012188080	70669.82	0.0000000000121404	-0.0000030700047125	4	70669.82	3851653.46

Appendix E. CPLEX Solution Output for the PLDMsv and PLDMq

B=\$3,851,653									
Level:									
Budget)								
Maximum									
the						(MIM)			
PLDMsv at									
put for the	tminsv.mps	scaledsv.mps	1.382233E+08	OPTIMAL SOLN	0	obj	rhs		BOUND
CPLEX Solution Out	PROBLEM NAME tminsv.mps	DATA NAME	OBJECTIVE VALUE	STATUS	ITERATION	OBJECTIVE	RHS	RANGES	BOUNDS

0200	
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.DUAL ACTIVITY	10-	-2326117	-3590310	-3652814	-1.901605E+07	-1556144	-2581623	-1305148	-5450212	-121404.3	-2067420	-1.208774E+07	-8488365	-9163556	-606521.1	-1.774138E+07	-5814403	-2232926	-2287884	-1.92917E+07	-1.884156E+07
UPPER LIMIT.	NONE 3851653	\leftarrow	\leftarrow	\vdash	⊣	П	-	-	1	+	Т	7	-	1	1	П	-1	€	++	-	1
LOWER LIMIT.	NONE	1	4	1	Н	(-1	Н	П	1	Н	1	1	1	Н	٦	Н	Н	1	1	Н	1
SLACK ACTIVITY	-1.382233E+08 -3.19788BE-10	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
ACTIVITY	1.382233E+08 3851653	\leftarrow		7	⊣	7		\leftarrow 1		ਜ	Н	Н	-		н	Н	Н	1	Н	-	 1
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ROW	obj budget	order1	order2	order3	order4	order5	order6	order7	order8	order9	order10	order11	order12	order13	order14	order15	order16	order17	order18	order19	order20
NUMBER	7 7	3	4	2	9	7	80	Q	10	11	12	13	14	15	16	17	18	19	20	21	22

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	.KEDOCED COST.	.958327E+0	.971689E+0	143398E+0	40468	,	132316	i)]	.052601E+0	50243E+0	.380373E+0	691715	90		83905	35509	94654	86609	2342127	13981		59		46E+0	450780	37097		.605292E+0	42E+0	.310786E+0	.919228E+0	.545857E+0	774960	50896	90		24477	2878003	60926		235799.7
mtwr 1 daddii		1	τ	1				l (-	+	\leftarrow	-	П	1	Н	-	-	Н	Н	1	1	7	1	1	7	Н	H	+	Н	1	Н	1	1	7	Н	۳	-	+	↔	\vdash	\leftarrow
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TOOD FIIGHT		7.190939E+07	.204301E+0	.37601E+0	73079	32611	72262	59031	.417882E+0	15524E+0	.745655E+0	.056997E+0	26987	65281	2.68551E+0	.537114E+0	.396259E+0	.262603E+0	17E+0	.015586E+0	.901605E+0	55620	55614	09E+0	08942	95260	2	.618344E+0	499357E+0	.441301E+0	.049743E+0	.676372E+0	05475	81411	52305	30514	99E+0	2821	05947	4502	5720
ひかてひてゆる		0	0	0	0	7	0	-	0	0	0	0	0	-	0	0	0	0	0	0	H	0	H	0	0	0	\vdash	0	0	0	0	0	0	0	0	Н	0	0	0	\leftarrow I	0
COLUMN AT	•	0501298252	05012982522-2	05012982522-3	05012982522-4	05012982522-5	70013562584FX1	70013562584FX2	60012912590FX0	60012912590FX1	60012912590FX2	60012912590FX3	60012912590FX4	60012912590FX5	30012251893125	30012251893126	30012251893127	30012251893128	30012251893129	30012251893130	30012251893131	50013969218-1	50013969218-2	60013387046BO3	60013387046BO4	60013387046BO5	60013387046BO6	60013389649B5	60013389649B6	60013389649B7	60013389649BB	60013389649B9	60013389649B10	60013389649B11	60013389649B12	60013389649B13	35012180143-1	35012180143-2	35012180143-3	35012180143-4	35012188080-1
MIMBER	· Andrion	23 10	4 1	5 1	6 1	7 1	8 1	9 1	0 1	1 1	2 1	3 1	4 1	5	6 1	7 1	8 1	9 1	0 1	1	2 1	3 1	4 1	5 1	6 1	7 1	8	9 1	0 1	1 1	2 1	3 1	4	5 1	6 1	7 1	8	9	0 2	61 28	2

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5246427 2390446 2390446 0 2.445096E+07 1.283268E+07 7639554 3547559 3.00125E+07 1.787378E+07 1.787378E+07 1.787378E+07 456758		.DUAL ACTIVITY	1 35.11856 -7544184 -4571848 -4220283 -5.947828E+07 -1.473579E+07
ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ		UPPER LIMIT.	NONE 3185775 1 1 1 1
185,775		LOWER LIMIT.	NONE NONE 1 1 1 NONE
2232926 7534311 4678330 2287884 4.3742687884 3.756742E+07 3.212438E+07 2.693126E+07 2.283926E+07 4.885407E+07 3.671534E+07 1.92917E+07 3.671534E+07 1.929832E+07 1.929832E+07 1.929832E+07 1.929832E+07 1.929832E+07		SLACK ACTIVITY	-1.412592E+08 0 0 0 0 0 0 0 0 0
1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	(MIN)	ACTIVITY	1.412592E+08 3185775 1 1 1 1 1 1 1
013934820EW8 BS 013410403FX1 LL 013410403FX2 LL 012400136FX4 LL 012400136FX5 LL 012400136FX5 LL 012400136FX6 LL 012400136FX9 LL 012400136FX9 LL 012400136FX9 LL 012400136FX9 LL 013195039-36 LL 013195039-37 LL 013195039-39 LL 013195039-41 LL 013195039-42 LL	obj rhs BOUND ROWS	ROW AT	et UL UL L.2 L.3 L.3 L.5 L.5 L.5 L.2 L.5 L.5 L.5 L.7
108 598501 100 598801 110 599801 111 660501 113 660501 114 660501 115 660501 115 660501 117 660501 119 661001 120 661001 121 661001 121 661001 122 661001 123 661001 124 661001 124 661001 125 651001 127 661001 127 661001 128 651001 128 651001 129 651001 121 651001 122 651001 123 651001 124 651001 124 651001	OBJECTIVE RHS RANGES BOUNDS SECTION 1 - R	NUMBER	1 obj 2 budget 3 order1 4 order2 5 order4 7 order5 8 order5 9 order5

-1.306177E+07 -0.306177E+07 -1.350126E+07 -1.238494E+07 -1.238494E+07 -2.519087E+07 -1.237415E+07 -1.237415E+07 -4616516 -4093953 -2.419253E+07		REDUCED COST.	6.540882E+07	.0586U5E+U	36106		-358453	1	.995854E+0	45E+0	.346325E+U	0690169 250356		98582	4810737	71105	68336	72438	3094	0	17165	78705	85037	56416.	5471		1.556384E+08
ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ		UPPER LIMIT.	₩.	⊣ ←	~	\vdash	₩.		⊷,	- 1	⊣ ←	-1 ←	1 ←1	-		\vdash	-	ᆏ	Н	-	-	1	н	H	-	. →	-
NONE 1 1 1 1 1 1		LOWER LIMIT.	00	0	0	0	0	0	0	0			0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
010000000000		INPUT COST	190939E+	.204301E+0 1.37601E+0	573079	32611	72262	359031	.417882E+0	24E+0	0143633E+0	626987	65281	2.68551E+0	14E+0	.396259E+0	.262603E+0	.135817E+0	.015586E+0	.901605E+0	55620	55614	09E+0	08942	95260	258162	44E+0
		ACTIVITY	00	00	0	\leftarrow I	с - (D (0 (0 0		00	• ←1	0	0	0	0	0	0	\leftarrow 1	0	0	0	0	Н	0	0
		. AT	12.																								
order8 order9 order11 order12 order13 order14 order15 order16 order18 order19	2 - COLUMNS	COLUMN	1005012982522-1	00501298252 00501298252	00501298252	00501298252	270013562584	270013562584	560012912590	560012912590	560012912590	560012912590	5600129125	630012251893	630012251893	630012251893	630012251893	630012251893	630012251893	630012251893	650013969218	650013969218	660013387046	660013387046	660013387046	6600133870	660013389649
11 11 11 11 11 11 11 11 11 11 11 11 11	SECTION	NUMBER	23	25	26	27	28	29	30	31	7 6	3.0	32	36	37	38	39	40	41	42	43	44	45	46		48	49

8.94089E+07 4.94397E+07 2.613548E+07 1.301313E+07 2.286249 6.06543.9 6.06543.9 6.06543.9 7.049949E+07 7.049949E+07 1.39978EE+07 7.049949E+07 1.57924E+07 1.57924E+07 1.57924E+07 2.640474E+07 2.640474E+07 2.640474E+07 3.965586E+07 1.57924E+07 1.57924E+07 3.426295E+07 1.57924E+07 2.640474E+07 3.965586E+07 1.657417E+07 3.965586E+07 1.696115E+07 2.640474E+07 3.965586E+07 1.696115E+07 3.965586E+07 1.696115E+07 3.965586E+07	1.124524E+07 -1644353
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<u>0190</u> 0 01110040 00000000 000 000 000 000 000	6E+0 4E+0
0.44 0.5292688 0.5292688 0.5292688 0.00 0.00 0.00 0.00 0.00 0.00 0.00 0	0 1
1660013389649B6 LL 1660013389649B7 LL 1660013389649B9 LL 1660013389649B10 LL 1660013389649B10 LL 1660013389649B10 LL 1660013389649B11 LL 1660013389649B11 LL 1660013389649B12 LL 1680013389649B13 BS 2835012180143-1 BS 2835012180143-2 LL 2835012180143-4 LL 283501218080-1 LL 283501218080-1 LL 283501218080-1 LL 283501218080-1 LL 283501218080-1 LL 4810012537542-9 LL 4810012537542-10 LL 4810012537542-11 LL 5835012188080-3 LL 582501218080-3 LL 582501224830225KX LL 5825012913073F9 LL 5895012913073F1 LL 5895013640160LN3 LL 5895013640160LN3 LL	89501382322 89501382322
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0	.235728E+	2.015001E+07	.177602E+0	12683	39501	0	.368294E+0	.004265E+0	09E+0	.593532E+0	62398	09191	0	04238	8842	0	.172827E+0	57E+0	.119907E+0	55048	00302	0	931426E+0	72919E+0	8166253	28215	8076	383.	0
	1	Н	1	1	\leftarrow		← 1	□		₽	1	Н	-	₩.	Н	Н	←-1	←1	←1	←1	~	~ 1	€-4	eI	-	1	кH	~	~
0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
.774138E+0	0	.783863E+	.899608E+0	.287834E+0	67797	81440	.4085E+0	.376532E+0	81E+0	.906209E+0	45280	62278	23292	5343	67833	28788	.374266E+0	.756742E+0	212438E+0	.693126E+0	.283926E+0	1.92917E+	.885407E+0	.671534E+0	.747331E+	.047284E+0	.975508E+0	832E+0	.884156E+
0	0	0	0	0	0	ᆏ	0	0	0	0	0	0	Н	0	0	Н	0	0	0	0	0	П	0	0	0	0	0	0	1
	LL (14 LL			17 LL		71 LL					7T 91	7			19 PT			19 LL		41 LL	12 BS
8950138232	5985013902368E9	9850139023	9850139023	9850139023	9850139023	9850139023	9850139348	9850139348	9850139348	9850139348	9850139348	9850139348	9850139348	9980134104	9980134104	9980134104	6050124001	6050124001	6050124	605012400136F	605012400136F	605012400136F	610013195039-	610013195039-	610013195039-	610013195039-	610013195039-	610013195039-	610013195039-
95	96	97	86	66	0	0	0	0	0	0	0	0	0	109	Н	\leftarrow	\leftarrow	Н	\vdash	\vdash	\vdash	\vdash	\vdash	Н	\sim	\sim	\sim	\sim	124

CPLEX Solution Output for the PLDMsv at a Budget Level of 2,700,022									
Level									
Budget						MAX)			
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<u>ra</u>									
PLDMsv				_					
the	sdw.n.	sdm.vs	3E+08	SOLN					
put for	tsvscaln.mps	scaledsv.mps	-1.88853E+08	OPTIMAL SOLN	49	obj	rhs		GINITAG
ution Out	NAME	NAME	OBJECTIVE VALUE		No	Æ			
CPLEX Sol	PROBLEM NAME	DATA	OBJECTIV	STATUS	ITERATION	OBJECTIVE	RHS	RANGES	POLINIDO

ROWS	
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SECTION	

.DUAL ACTIVITY	1 -256.9537 3.627423E+07	0	35E+0		6.637543E+07	.401898E+0	.296243E+0		ט פ סעכ	478719	.129361E+0	.597028E+0	.883893	.381042E+0	967306		482092E+0	5.38144E+		REDUCED COST.	.327	1 104049E+0	-393441		117	34	.077198E+0	37398E+0	2.118081E+0	.131252E+0	534	-1786658	0-	775979.1
UPPER LIMIT.	NONE 2700222	e-1 e-	·1 ·1	-		1		٦,	⊣ ←) (-	-	-		H	1	∺		UPPER LIMIT.	•	-	۱ ۲	1			-	ι —	1	Н	+		 1	Н
LOWER LIMIT.	NONE NONE	NONE	4 4-4	NONE	₩.	. Н	1	NON	→ ←	-	· ←	+		H	-	NONE	4	П		LOWER LIMIT.	0	C	0	0	0	0	0	0	0	0	0	0	0	0
SLACK ACTIVITY	1.88853E+08 0 0	H C	0	1	0	0	0,	40	o c	0	0	0	0	0	0	-	0	0		INPUT COST	.190939	430	1.37601E	-573	2326	722	3590	.417882E	2.815524E	.745655E	.056997	26987	-3652	51
ACTIVITY	-1,88853E+08 2700222	0 -	ii	0	 1 ,	⊶,		> F	-1 e	v~	Н	1	1	₽	1	0	Н	н		ACTIVITY	0	0	0	\vdash	0	0	0	0	0	0	0	0	7	1
. AT	BS	BS EO	ы О	BS	O (O (E C	2 6	i ic	(C)	G G	Ğ	Ö	Ğ	ğ	BS	S S	EQ		AT	LL	LL	ĽĽ	BS	LL	TI.	LL	Trr o	LL.	I.	디	J	BS	ď
ROW	obj budget order1	order2 order3	order4	order5	order6	order/	order8	order 10	order11	order12	order13	order14	order15	order16	order17	order18			2 - COLUMNS	COLUMN	1005012982522-1	1005012982522-2	1005012982522-3	1005012982522-4	1005012982522-5	1270013562584FX1	1270013562584FX2	1560012912590FX0	1560012912590FX1	1560012912590FX2	1560012912590FX3	1560012912590FX4	1560012912590FX5	1630012251893125
NUMBER	426.	4n ru	9	7	ω (, כ	10	17	13	14	15	16	17	18		20			SECTION	NUMBER	c	4	S	26	7	00	σ	0	\vdash	0	m	~ !!	Ω,	و

37	1630012251893126 BS	00	-2.537114E+07	0 0	1207	
9 6	630012251893128	0	2.262603E+0		-177476	
40	630012251893129	0	2.135817E+0		-276684	
41	630012251893130	0	2.015586E+0		-382447	
42	630012251893131	0	1.901605E+0		-494459	
43	650013969218-1	0	155620		-1.337608E+0	
4 4	650013969218-2	0	-155614		-2.519589E+0	
45	660013387046B03	1	909E+0		540184	
46	660013387046BO4	0	708942			
47	660013387046B05	0	295260		-1.068467E+0	
48	66001338704	0	-258162		-2.51352E+0	
49	660013389649B5	0	1.618344E+0		-1.301812E+0	
20	660013389649B6	0	499357E+0		-6.781361E+0	
51	660013389649B7	0	5.441301E+0		-3.170621E+0	
52	660013389649B8	0	3.049743E+0		-1.226381E+0	
23	660013389649B9	0	1.676372E+0		-300326	
54	660013389649B10	П	905475		232530.	
55	660013389649B11	0	481411		1	
26	660013389649B12	0	252305		-218210	
57	660013389649B13	0	130514		-543736	
28	835012180143-1	-	499E+0		1.495033E+0	
29	835012180143-2	0	832821		•	
09	835012180143-3	0	605947		-1.504837E+0	
61	835012180143-4	0	545021		-3.175621E+0	
62	835012188080-1	0	-35720		-1.851608E+0	
63	835012188080-2	0	250328.		-3.656808E+0	
64	835012188080-3	0	174683.		-5.465131E+0	
9	835012188080-4	0	-121404.		-7.275691E+0	
99	810012537542-7	0	.429686E+0		-1.341525E+0	
29	810012537542-8	0	3555E+0		-6.564418E+0	
89	810012537542-9	0	3.694528E+0		-3.037871E+0	
69	810012537542-10	0	.832101E+0		-1.287922E+0	
70	810012537542-11	0	895968		-464268	
71	810012537542-12	0	432775		-113554	
72	810012537542-13	П	-206742		•	
73	810013377136TP1	0	287442E+0		-3.251277E+0	
74	810013377136T	0	.9897E+0		-1.160383E+0	
75	810013377136TP3	0	1.669315E+0		-468455.	
9/	810013377136TP4	.→	1.372872E+0		427499.	
77	810013377136TP5	0	.208774E+0		1	
78	821012483022	0	7.005764E+0		-4.403672E+0	
79	821012483022FX3	0	.669027E+0		-1.505249E+0	
0 1	821012483022FX4	0	.882022E+0		-156558	
81	821012483022F	T	48132		339017	

CPLEX Solution Output for the PLDMq at the Maximum Budget Level: B=\$3,851,653

PROBLEM NAME tqscale.mps
DATA NAME scaledq.mps
OBJECTIVE VALUE -1.684713E+13
STATUS
OPTIMAL SOLN
ITERATION 0 (MAX) BOUND obj rhs OBJECTIVE RHS RANGES BOUNDS

NUMBER	ROW AT	ATACTIVITY	SLACK ACTIVITY	LOWER LIMIT.	UPPER LIMIT.	.DUAL ACTI
ᆏ	obj BS	-1.684		NONE	NONE	
2	budget BS	3851653	-5.116621E-10	NONE	3851653	
m	order1 EQ	Н	0	Т	1	4.47001
•	(•		•	•	

SECTION 1 - ROWS

NUMBER	ROW	AT	ACTIVITY	SLACK ACTIVITY	LOWER LIMIT.	UPPER LIMIT.	.DUAL ACTIVITY
Н	obj	BS	-1.684713E+13	1.684713E+13	NONE	NONE	₽
2	budget	BS	3851653	-5.116621E-10	NONE	3851653	0
m	order1	ВQ	\leftarrow	0	Ч	1	4.47001E+10
4	order2	E	\leftarrow	0	Н	Н	2.81604E+11
2	order3	EQ	Н	0	Н	Н	9.624463E+11
9	order4	EQ	Н	0	Н	1	2.135728E+12
7	order5	EQ	\leftarrow	0	\leftarrow	Н	2.348028E+11
00	order6	EQ	⊣	0	Н	1	5.10113E+11
9	order7 '	EQ	7	0	Н	T	2.330003E+10
10	order8	EQ	Н	0	-	Н	1.373694E+12
11	order9	EQ	Н	0	\leftarrow	-	3.070005E+10
12	order10	EQ	⊣	0	7	-	8.000003E+09
13	order11	EQ	⊣	0	\vdash	Н	4.900012E+10
14	order12	EQ	~	0	Н		7.350027E+10
15	order13	EQ	7	0	Н	7	1E+08
16	order14	EQ	Н	0	~	Н	5.300001E+09
17	order15	BO	\leftarrow	0	Н	Н	1.714747E+12
18	order16	ВO	\leftarrow	0	Н	+	1.511011E+11
19	order17	ВO		0	Н	1	1.710001E+10
20	order18	O O	Н	0		1	7.350027E+10
21	order19	EQ	Н	0	Н	1	9.153788E+12
22	order20	ĔŎ		0	1	τ	3.900001E+09
SECTION	SECTION 2 - COLUMNS						

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-1.474012E+11
-6.720028E+10
-2.800006E+10
-9.100011E+09
                                                                       -6.200002E+09
-2.4E+09
-1.3E+09
-5E+08
                                                                                                                                          -6.186285E+11
-3.651122E+11
-1.933048E+11
-7.760147E+10
                        -3.445076E+11
-1.703023E+11
-6.25005E+10
                                                                                               -1.955492E+12
-4.949125E+11
-1.121007E+11
                                                        -5.558195E+11
-3.920036E+10
                                                                                                             -2.050003E+10
                                                                                                                                                                  -1.24688E+12
-6.210203E+11
                                                                                                                                                                                     -5.810027E+10
-1.890005E+10
                                                                                                                                                                                                        3.920036E+10
                                      .190013E+10
                                                -1.796475E+12
-1.11397E+12
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-9.408056E+11
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 -1.5540126-1.
-7.520028E+10
                                                                                -1.4E+09
-6E+08
-1E+08
         .600006E+10
              .710001E+10
                                      .090025E+10
                                                                   .350027E+10
                                                                                                             .580003E+10
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                                           900012E+10
                                                                       300002E+09
                                                                           -2.5E+09
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                        .935077E+11
                                 .115006E+11
                                               .869975E+12
                                                     .187471E+12
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                             .193024E+11
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5895012913073F7 I
5895012913073F8 I
5895012913073F9 I
5895012913073F10 I
5895012913073F11 E
                                                         5821012483022FX4
5821012483022FX5
810012537542-9
810012537542-10
             4810012537542-12
4810012537542-13
                            |810013377136TP2
|810013377136TP3
                                      810013377136TP4
                                          4810013377136TP5
5821012483022FX2
                                                    5821012483022FX3
                                                                  5821012483022FX6
                                                                                                        895013640160LN4
                                                                                                                                          5985013902368E10
                                                                                                                                                   5985013902368E12
                                                                                                                                                        5985013902368E13
                                                                                                                                                                                5985013934820EW5
                                                                                                                                                                                              5985013934B20EW8
                       810013377136TP1
                                                                                               895013640160LN2
                                                                                                    5895013640160LN3
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                                                                                                                       895013823225FX2
                                                                                                                                 5895013823225FX4
                                                                                                                                               5985013902368E11
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         810012537542-11
                                                                                                                            5895013823225FX3
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                                                                                                                                                                                                                  6605012400136FX4
                                                                                                                                     5985013902368E9
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-6.376365E+12 -3.241691E+12 -2.046882E+12 -9.870518E+11 -4.830014E+10 -9.500008E+09 -6.600005E+09 -2.700001E+09 -1.200001E+09		.DUAL ACTIVITY -2325298 3.902028E+11 3.465943E+11 1.00002E+12 4.814845E+12 0 1.20443E+12 5.351788E+11 2.000538E+11 2.1403239E+11 3.11491E+11
ਜਜਜਜਜਜਜਜਜ		UPPER LIMIT. NONE 3185775 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0		LOWER LIMIT. NONE NONE 1 NONE 1 NONE 1 1 1 1 1 1 1 1 1 1 1 1 1
-1.553015E+13 -1.239548E+13 -1.120067E+13 -1.014084E+13 -9.153788E+10 -1.340001E+10 -1.050001E+10 -8.400004E+09 -6.60002E+09 -5.100001E+09 -5.100001E+09		SLACK ACTIVITY 1.696933E+13 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0
0 0 1 1 0 0 0 0 1 1 PLDMq at a Budget	(MAX)	ACTIVITY1.696933E+13 3185775 1 1 1 1 1 1 1 1 1 1 1 1
012400136FX5 LL 012400136FX6 LL 012400136FX7 LL 012400136FX8 LL 013195039-36 LL 013195039-37 LL 013195039-39 LL 013195039-40 LL 013195039-41 LL 013195039-41 LL 013195039-42 LL	tqscalel.mps scaledq.mps -1.696933E+13 OPTIMAL SOLN 26 obj rhs	- ROWS obj budget order1 order3 order4 order5 order6 order6 order7 order8 corder8 order8 order10 EQ order10 EQ order11 EQ order11 EQ
113 6605 114 6605 115 6605 116 6605 117 6605 118 6610 120 6610 121 6610 122 6610 123 6610 124 6610	PROBLEM NAME DATA NAME OBJECTIVE VALUE STATUS ITERATION OBJECTIVE RHS RANGES BOUNDS	NUMBER 1 obj 2 budget 3 order1 4 order2 5 order3 6 order4 7 order5 8 order6 10 order6 11 order8 11 order1 12 order1 13 order1

1.576249E+11 4.17169E+11 2.20799BE+12 5.854402E+11 1.749241E+11 1.930851E+11 9.478286E+12 3.033082E+11		REDUCED COST.	1.324133E+1			0-	-3.503229E+11	•	1.339694E+1	7.682456E+1	\rightarrow	2.001568E+1	7.348843E+1	•	3.838134E+1	.064393E+1	2.348675E+1	1.68698E+1	-	5.156437E+1	'	7.245828E+1	-4.487301E+11	3.618595E+1	0-	4.502132E+1	1.104444E+1	3.422225E+1	+	9.022468E+1	4.118795E+1	1.604454E+1	4.332125E+1
ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ		UPPER LIMIT.	↔ ,	-1 ←	i —	-	Н	 1	, - 1	Н	⊷ ,	Н.	⊷ ,	Н.	н .	1	1	Н	н	Н	н	Н	Н	Н	Н	1	ч		П	7	T	П	Н
нннннн		LOWER LIMIT.	0 0		0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
0000000		INPUT COST	-1.645235E+12	6.93024E+1 2.84104E+1	.138006E+1	4.47001E+1	.644221E+1	Z.81604E+1	1.439696E+1	8.6/4962E+1	.127214E+1	2.979044E+1	1.704845E+1	9.624463E+1	2.642249E+1	2.544424E+1	2.452401E+1	2.36578E+1	2.284261E+1	2.207744E+1	.135728E+1	6.176191E+1	2.348028E+1	8.382351E+1	6.679223E+1	5.788168E+1	5.10113E+1	3.755005E+1	.101321E+1	1.154067E+1	6.232194E+1	3.313055E+1	.737015E+1
ਜਜਜਜਜਜਜ		ACTIVITY	00	00	934788	0652111	0 1	.	0	0 (0	o (0,	·	0 (0	0	0	0	0		0	0	0	⊣	0	0	0	0	0	0	0	0
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115 116 118 220 221	SECTION 2	NUMBER	23	25	26	27	28	57	30	31	32	L. (λ. 4.14	35	3.6	37	38	39	40	41	42	43	44	45	46	47	48	49	20	51	52	53	54

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-0
3.420445E+09
-1.435933E+10
-8.668406E+11
                                                                                           -1.141463E+11
-2.506321E+10
-3.181484E+09
                                  -2.336286E+11
-3.802569E+11
-5.322852E+11
                                                                                                               -1.637814E+12
-9.949749E+11
-4.764893E+11
                                                                                                                                                 -1.829061E+10
-3.688122E+10
-5.577183E+10
                                                                                                                                                               -1.700171E+12
-3.178649E+11
-1.332686E+10
                                                -6.880135E+11
-5.690478E+11
-2.582112E+11
                                                                                                                                             0-
                                                                                                                                                                                   -5.777377E+10
-1.646578E+12
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-2.105464E+11
                                                                   -3.6664E+10
                                                                        -7.642545E+09
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                                                                                                                                        1.559061E+10
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-2.720395E+11
                                                               -1.066862E+11
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-1.174007E+11
-2.580003E+10
-5.300001E+09
-3.607951E+12
         -2.330003E+10
-2.710667E+12
-2.149331E+12
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-1.4E+09
                                                                                                                                                          E+08
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-8.99004E+10
     .600011E+10
                        -1.740952E+12
                             -1.373694E+12
-6.930024E+10
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                                                          -3.17105E+11
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5821012483022FX5 U
5821012483022FX6 E
5895012913073F7 U
             2835012180143-1
2835012180143-3
2835012180143-3
2835012180143-4
2835012188080-1
2835012188080-2
2835012188080-3
2835012188080-4
4810012537542-7
4810012537542-8
                                                                                                                                                     5895012913073F10
    1660013389649B12
1660013389649B13
                                                                   4810012537542-10
4810012537542-11
                                                                             4810012537542-12
                                                                                  4810012537542-13
4810013377136TP1
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4810013377136TP4
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5821012483022FX3
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5895013640160LNZ
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5895013640160LN5
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5895013823225FX3
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5985013902368E10
                                                                                                                                                                                                               5985013902368E11
5985013902368E12
                                                                                                                                           5895012913073F8
5895012913073F9
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0 -1.26398E+12 0		0 11	-2.287026E+11 -1.511011E+11	0	1 -4.657726E+10 1 -0
0 -6.381204B+11 0	5985013934820EW2	0	1.26398E+1	0	-1.128512E+1
0 -3.17105B+11 0 1 1.554012B+11 0 0	5985013934820EW3	0	.381204E+1	0	-5.223803E+1
0 -1.554012E+11 0 0	5985013934820EW4	0	ω,	0	-2.21093
0 -7.520028E+10 0	5985013934820EW5	0	•	0	-7.911716
1 -3.600006E+10 0 1 1 -3.600006E+10 0 1 1 -3.600006E+10 0 0 1 1 -1.229019E+11 0 0 1 1 -1.229019E+11 0 0 0 1 1 -1.229019E+13 0 0 0 -2.640027E+13 0 0 0 -1.239548E+13 0 0 0 -1.239548E+13 0 0 0 -1.239548E+13 0 0 0 -1.239548E+13 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	5985013934820EW6	0	7	0	-1.864424
0 -1.710001E+10 0 1 1	5985013934820EW7	-	ω.	0	8.279619E+0
0 -1.929019E+11 0 1 1 -1.127006E+11 0 0	5985013934820EWB	0	Ή.	0	1
1 -1.127006E+11 0 0	5998013410403FX1	0	ä	0	-3.967834E+1
0 -7.350027E+10 0 1 1	5998013410403FX2	⊣	H	0	6.61261E+0
0 -2.640493E+13 0 1 -1.553015E+13 0 1 1 -1.553015E+13 0 0	5998013410403FX3	0	~	0	,
0 -1.553015E+13 0 1 1	6605012400136FX4	0	2	0	-1.707087E+1
0 -1.239548E+13 0 1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2	6605012400136FX5	0	H	0	-6.232144E+1
0 -1.120067E+13 0 1 1	6605012400136FX6	0	ί.	0	-3.1
0 -1.014084E+13 0 1 -9.153788E+12 0 0 1 -9.153788E+12 0 0 0 -5.220014E+10 0 0 1 1 -1.340001E+10 0 0 1 1 -1.340001E+10 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	6605012400136FX7	0	÷.	0	-1.974772E+1
1 -9.153788E+12 0 1 1	6605012400136FX8	0	1.014084E+1	0	-9.509965E+1
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1 -1.340001E+10 0 1 0 -1.05001E+10 0 1 0 -8.400004E+09 0 1 1 0 -6.60002E+09 0 1 1 -1 0 -5.100001E+09 0 1 1 -1 PLDMq at a Budget Level of \$2,700,222	6610013195039-36	0	5.220014E+1	0	-2.62
0 -1.050001E+10 0 1	6610013195039-37		1.340001E+1	0	4.805475E+0
0 -8.400004E+09 0 1 -9.400002E+09 0 0 -6.600002E+09 0 0 1 -9.100001E+09 0 0 1 -9.200001E+09 0 0 0 1 -9.200001E+09 0 0 0 1 -9.200001E+09 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	6610013195039-38	0	.050001E+1	0	
0 -6.600002E+09 0 1 -: 0 -5.100001E+09 0 1 -: 0 -3.900001E+09 0 1 -: PLDMq at a Budget Level of \$2,700,222 s	6610013195039-39	0	.400004E+0	0	-5.605477E+0
0 -5.100001E+09 0 1 -: 0 -3.900001E+09 0 1 -: PLDMq at a Budget Level of \$2,700,222 S	6610013195039-40	0	6.600002E+0	0	ï
0 -3.900001E+09 0 1 -: PLDMq at a Budget Level of \$2,700,222 S	6610013195039-41	0	5.100001E+0	0	-1.771643E+1
PLDMq at a Budget Level of \$2,700,22 s	6610013195039-42	0	3.900001E+0	0	1
scaledq.mps -1.885264E+1	Ū	a t a	Level of \$2,700,22		
-1.885264E+1					
MICO TENTENCO					

	(MAX)
cqscaren.mps scaledq.mps -1.885264E+13 OPTIMAL SOLN 54	obj rhs BOUND
FROBLEM NAME DATA NAME OBJECTIVE VALUE STATUS ITERATION	OBJECTIVE RHS RANGES BOUNDS

07:10	200
	1
INC PECOL	יון
-	4

.DUAL ACTIVITY	-
UPPER LIMIT.	NONE
LOWER LIMIT.	NONE
SLACK ACTIVITY	1.885264E+13
ACTIVITY	-1.885264E+13
AT	BS
NUMBERADW AT	1 obj

-8672086 1.144629E+12 0 1.102576E+12 1.212335E+13 2.668801E+12 3.318222E+12 3.318222E+11 3.209315E+11 3.209315E+11 3.209315E+11 3.209315E+11 3.209315E+11 3.209315E+11 3.203316E+12 5.125145E+11 5.125146E+12 1.375968E+12 1.375968E+12 1.375968E+12 1.375968E+12 1.375968E+12 1.37596E+12 1.036399E+13 1.08674E+12	REDUCED COST.	-7.583132E+11 -6.380905E+10 8.740377E+10 -1.886066E+11 -7.856113E+11 -5.239823E+11 -1.329438E+13 -7.600412E+12 -4.08069E+12 -7.143732E+11 -7.143732E+10 -5.290003E+10 -5.290003E+10 -5.290003E+10 -5.246916E+09 -7.1559575E+10 -5.246916E+09
2700222	UPPER LIMIT.	ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ ਜ
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001001000000000000000000000000000000000	INPUT COST	-1.645235E+12 -6.93024E+11 -2.84104E+11 -4.47001E+10 -6.644221E+11 -2.81604E+11 -1.439696E+13 -1.43969E+12 -2.979044E+12
270022 22 0 0 1 1 1 1 1 1 1 1 1 1 1 1 1 1	ACTIVITY	H000000000000000
0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	COLUMNS AT	2982522-1 LL 2982522-2 LL 2982522-3 UL 2982522-4 BS 2982522-5 LL 3562584FX1 LL 3562584FX2 LL 2912590FX1 LL 2912590FX2 LL 2912590FX3 LL 2912590FX3 LL 2912590FX4 LL 2912590FX4 LL 2912590FX3 LL 2912590FX4 LL 2912590FX4 LL 2912590FX4 LL 2912590FX5 LL 2912590
budget order1 order3 order4 order6 order10 order110 order110 order110 order110 order110 order110 order110 order110 order110	2 - 60	1005011 1005011 1005011 1270011 1560011 1560011 1560011 1630011 1630011 1630011
28 4 2 2 8 4 2 8 8 7 6 5 4 3 2 8 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	SECTION	22 2 2 2 2 2 2 2 2 2 2 2 3 3 3 3 3 3 3

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6.636321E+09
-6.053023E+10
-1.675976E+11
-2.958652E+11
2.310903E+10
                            -4.111141E+11
-8.426301E+11
-2.819829E+12
-1.317112E+12
-5.208258E+11
-1.409463E+11
                                                                                                                                                                              -4.792232E+10
-1.423865E+11
-3.799149E+10
                                                                                                                                                                                                                                                    -6.851635E+10
-1.397327E+11
-2.11249E+11
     -1.016535E+12
-1.032635E+12
3.299069E+11
                                                                                                        -1.76066E+11
-3.932542E+11
-6.82155E+11
-1.27731E+12
                                                                                                                                                                        -1.906114E+10
                                                                                                                                                                                                      -2.920992E+10
-7.712008E+10
-4.011248E+09
                                                                                                                               -1.877864E+12
-2.482119E+12
                                                                                                                                           -4.502755E+11
                                                                                                                                                  -1.672214E+11
-4.347877E+10
                                                                                                                                                              -1.23903E+09
                                                                                                                                                                                                                 -1.204758E+12
                                                                                                                                                                                                                            -2.599613E+11
1.087288E+11
                                                                                                                                                                                                                        -6.701828E+11
E+10
                                                   -1.154067E+12
-6.232194E+11
                                                                                       -2.330003E+10
                                                                                                                    .930024E+10
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                                                                            .99004E+10
                                                                                  -4.600011E+10
                                                                                                        -1.740952E+12
                                                                                                                          .160013E+10
                                                                                                                                .930008E+10
                                                                                                                                                             .520028E+10
                                                                                                                                                                   .600006E+10
                                                                                                                                                                                                      .090025E+10
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-2.135728E+12
-6.176191E+11
           .348028E+11
                 .382351E+11
                            .788168E+11
                                              .101321E+12
                                                                     -1.737015E+11
                                                                                             .710667E+12
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                       .679223E+11
                                   .10113E+11
                                         .755005E+12
                                                                -3.313055E+11
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1660013389649B10
                 1660013387046BO3
                       1660013387046BO4
1660013387046BO5
                                  1660013387046B06
                                                                           1660013389649B11
1660013389649B12
                                                                                       1660013389649B13
                                                                                                                                                       4810012537542-9
4810012537542-10
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4810012537542-13
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4810013377136TP3
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5821012483022FX2
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5821012483022FX5
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5895012913073F8
5895012913073F9
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1630012251893131
     1650013969218-1
1650013969218-2
                                        1660013389649B5
1660013389649B6
                                                   1660013389649B7
                                                          1660013389649B8
1660013389649B9
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2835012180143-2
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2835012180143-4
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                                                                                                                   2835012188080-1
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-2.830654E+11
-1.168661E+12
-0
               9.089346E+10
-1.094243E+11
-3.808426E+11
-9.734254E+11
                                                                         -3.810184E+10
-8.878547E+11
-3.355698E+11
-8.812915E+10
                                                                                                   6.626255E+09
-2.77482E+10
-8.242282E+10
-3.415639E+11
-4.100247E+11
                                                    -1.939171E+11
-5.610408E+10
                                                                                                                                                                       1.006292E+10
                                                                                                                                                                                      -6.934871E+10
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                                                                                                                                                  -1.777949E+12
-8.525854E+11
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-5.162133E+11
-3.444059E+11
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-5.30001E+09
-3.607951E+12
                                                                                            -1.554012E+11
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-3.60006E+10
-1.710001E+10
     -1.960792E+12
-5.002125E+11
-1.174007E+11
                                    .655553E+12
                                                                                                                                                                .220014E+10
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                                                                                        -3.17105E+11
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5895013640160LN5 I
5895013640160LN6 I
5895013823225FX2 I
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5895013823225FX4 I
5985013902368E9 I
    5895013640160LN2
5895013640160LN3
               5895013640160LN4
                                                   5985013902368E10
5985013902368E11
                                                              5985013902368E12
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5985013902368E14
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5985013934820EW4
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5985013934820EW7
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6605012400136FX8
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5895012913073F11
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5998013410403FX2
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                                                                                                                                                                                      6610013195039-40
                                                                                                                                                                                                6610013195039-42
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		1	S Sensitivity Range	1
Constraint Name	Dual Price	Down	Current	Up
budget	8672085.79	2699103.03	2700221.70	2712445.07
		OR	 J Sensitivity Range	
Variable Name	Reduced Cost	Down	Current	Up
1005012982522-1	0.99992417	-infinity	0.99983549	0.99991131
1005012982522-2	0.99999362	-infinity	0.99993070	0.99993708
1005012982522-3	1.00000874	0.99996285	0.99997159	+infinity
1005012982522-4	1.00000000	0.99998224	0.99998862	0.99999736
1005012982522-5	0.99998114	-infinity	0.99999553	1.00001439
1270013562584FX1	0.99992144	-infinity	0.99993356	1.00001432
1270013562584FX2	0.99994760	-infinity	0.99997184	1.00001212
1560012912590FX0	0.99867144	-infinity	0.99856134	0.99988975
1560012912590FX1	0.99924025	-infinity	0.99913288	0.99989255
1560012912590FX2	0.99959201	-infinity	0.99948741	0.99989535
1560012912590FX3	0.99980396	-infinity	0.99970214	0.99989816
1560012912590FX4	0.99992857	-infinity	0.99982953	0.99990096
1560012912590FX5	1.00000000	0.99983233	0.99990376	+infinity
1630012251893125	0.99999471	-infinity	0.99973581	0.99974110
1630012251893126	0.99999687	-infinity	0.99974559	0.99974872
1630012251893127	0.99999844	-infinity	0.99975479	0.99975635
1630012251893128	0.99999948	-infinity	0.99976345	0.99976397
1630012251893129	1.00000000	0.99977120	0.99977160	0.99977162
1630012251893130	1.00000002	0.99977923	0.99977925	+infinity
1630012251893131	0.99999960	-infinity	0.99978645	0.99978685
1650013969218-1	0.99989835	-infinity	0.99993824	1.00003989
1650013969218-2	0.99989674	-infinity	0.99997652	1.00007979
1660013387046BO3	1.00003299	0.99988319	0.99991618	+infinity
1660013387046BO4	1.00000000	0.99989210	0.99993321	0.99996620
1660013387046BO5	0.99995889	-infinity	0.99994212	0.99998323
1660013387046BO6	0.99991574	-infinity	0.99994899	1.00003325
1660013389649B5	0.99971806	-infinity	0.99962457	0.99990649
1660013389649B6	0.99986830	-infinity	0.99978989	0.99992158
1660013389649B7	0.99994792	-infinity	0.99988460	0.99993668
1660013389649B8	0.99998591	-infinity	0.99993768	0.99995177
1660013389649B9	1.00000000	0.99996082	0.99996687	0.99996753
1660013389649B10	1.00000066	0.99998197	0.99998263	+infinity
1660013389649B11	0.99999395	-infinity	0.99999101	0.99999706
1660013389649B12	0.99998324	-infinity	0.99999540	1.00001216
1660013389649B13	0.99997041	-infinity	0.99999767	1.00002726

2835012180143-2	2835012180143-1	1 00000221	0.00073666	0.00073907	.!
2835012180143-3		1.00000231	0.99972666	0.99972897	+infinity
2835012180143-4 0.99996068 -infinity 0.99986264 0.99990196 2835012188080-1 0.99981728 -infinity 0.9999307 1.00006129 2835012188080-2 0.99987228 -infinity 0.99999484 1.00012238 2835012188080-3 0.99981223 -infinity 0.9999607 1.00018387 2835012188080-4 0.99987182 -infinity 0.9999607 1.00018387 2835012188080-4 0.999975182 -infinity 0.9999609 1.00024517 4810012537542-7 0.99995497 -infinity 0.9999619 0.99998122 4810012537542-8 0.999998328 -infinity 0.99998629 0.99998801 4810012537542-10 0.9999988 -infinity 0.99998446 0.99998881 4810012537542-11 1.0000000 0.99999628 0.9999248 0.99999240 4810012537542-12 0.99999809 -infinity 0.99999249 1.00000020 4810012537542-13 0.99999521 -infinity 0.9999929 1.00000020 4810013377136TP2 0.99998576 -infinity 0.9999665 0.99997807 4810013377136TP2 0.99999620 -infinity 0.9999885 +infinity 4810013377136TP3 1.0000000 0.99998593 0.9999885 +infinity 4810013377136TP4 0.99999708 -infinity 0.9999921 0.99999187 4810013377136TP5 0.99999798 -infinity 0.9999910 0.99999885 5821012483022FX2 0.99987953 -infinity 0.9999910 0.99999885 5821012483022FX4 0.99997939 -infinity 0.99998102 0.9999348 5821012483022FX4 0.9999790 -infinity 0.99998873 +infinity 5821012483022FX4 0.9999790 -infinity 0.99998873 +infinity 5821012483022FX4 0.9999790 -infinity 0.99998873 +infinity 5821012483022FX4 0.9999790 -infinity 0.999999999999999999999999999999999999					
2835012188080-1 0.99993179 -infinity 0.9999307 1.00006129 2835012188080-2 0.99987228 -infinity 0.99999484 1.00012258 2835012188080-3 0.99981223 -infinity 0.99999607 1.00018387 2835012188080-4 0.99975182 -infinity 0.99999607 1.00018387 4810012537542-7 0.99995497 -infinity 0.99993619 0.99998122 4810012537542-8 0.99998328 -infinity 0.99996829 0.99998501 4810012537542-9 0.99999565 -infinity 0.99998446 0.9999881 4810012537542-10 0.99999988 -infinity 0.99999248 0.99999881 4810012537542-11 1.0000000 0.9999628 0.99999640 +infinity 4810012537542-12 0.99999809 -infinity 0.99999829 1.0000020 4810012537542-13 0.99999521 -infinity 0.99999829 1.0000039 4810012537542-13 0.99999520 -infinity 0.99999809 1.0000039 4810013377136TP1 0.99998576 -infinity 0.99999805 0.99998881 4810013377136TP2 0.99999600 -infinity 0.99999885 +infinity 4810013377136TP2 0.99999708 -infinity 0.9999885 +infinity 4810013377136TP2 0.99999708 -infinity 0.9999885 +infinity 4810013377136TP2 0.99999708 -infinity 0.9999885 +infinity 5821012483022FX2 0.99987953 -infinity 0.99998130 0.9999885 5821012483022FX2 0.99987953 -infinity 0.9999810 1.0000281 5821012483022FX3 0.99997400 -infinity 0.99993707 0.99993488 5821012483022FX3 0.99997400 -infinity 0.99999707 0.99996306 5821012483022FX3 1.00001087 0.9999786 0.99999887 +infinity 5821012483022FX3 1.00001087 0.9999786 0.9999887 +infinity 5821012483022FX4 0.99997400 -infinity 0.999999999999999999999999999999999999			-		
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2835012188080-3					
2835012188080-4					
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4810012537542-11 1.0000000 0.99999628 0.99999640 +infinity 4810012537542-12 0.99999809 -infinity 0.99999829 1.0000020 4810012537542-13 0.99999521 -infinity 0.99999920 1.0000039 4810013377136TP1 0.99998576 -infinity 0.99997807 0.9999788 4810013377136TP2 0.99999708 -infinity 0.99998855 +infinity 4810013377136TP4 0.99999708 -infinity 0.99999291 0.99999583 4810013377136TP5 0.99999708 -infinity 0.99999510 1.00000281 5821012483022FX2 0.999987953 -infinity 0.999981302 0.9999314 5821012483022FX3 0.999993298 -infinity 0.99981202 0.99998120 5821012483022FX4 0.99997786 0.99998873 +infinity 5821012483022FX5 1.00001087 0.99997786 0.99998873 +infinity 5821012483022FX6 1.0000000 0.99997786 0.99999873 +infinity 5821012483022FX6 1.00000000 0.99999778 <	4810012537542-9		-infinity	0.99998446	0.99998881
4810012537542-12 0.99999809 -infinity 0.99999829 1.00000020 4810012537542-13 0.99999521 -infinity 0.99999920 1.00000399 4810013377136TP1 0.99998576 -infinity 0.99996065 0.99997489 4810013377136TP2 0.99999620 -infinity 0.99997807 0.99998187 4810013377136TP3 1.00000000 0.99998593 0.99998885 +infinity 4810013377136TP5 0.999999229 -infinity 0.99999510 1.00000281 5821012483022FX2 0.99997533 -infinity 0.999981302 0.99993348 5821012483022FX3 0.99997533 -infinity 0.99988126 0.9999934827 5821012483022FX4 0.99997400 -infinity 0.99998873 +infinity 5821012483022FX5 1.00001087 0.99997786 0.99998873 +infinity 5821012483022FX6 1.00001087 0.999997866 0.99999873 +infinity 582012913073F7 1.0000000 0.999999999999999999999999999999999999	4810012537542-10	0.9999988	-infinity	0.99999248	0.99999260
4810012537542-13 0.99999521 -infinity 0.99999920 1.00000399 4810013377136TP1 0.99998576 -infinity 0.99996065 0.99997489 4810013377136TP2 0.99999620 -infinity 0.99997807 0.99998187 4810013377136TP3 1.00000000 0.99998593 0.99998885 +infinity 4810013377136TP4 0.99999708 -infinity 0.99999291 0.99999583 4810013377136TP5 0.99999229 -infinity 0.9999910 1.00000281 5821012483022FX2 0.99987953 -infinity 0.99981302 0.99993348 5821012483022FX3 0.99993298 -infinity 0.999988126 0.999994827 5821012483022FX4 0.99997400 -infinity 0.99998873 +infinity 5821012483022FX5 1.00001087 0.99997786 0.99999873 +infinity 5825012913073F7 1.00000000 0.99999252 0.999999997 +infinity 5895012913073F1 0.99998603 -infinity 0.99999999 1.0000383 5895012913073F10 0.9999788	4810012537542-11	1.00000000	0.99999628	0.99999640	+infinity
4810013377136TP1 0.99998576 -infinity 0.99996065 0.99997489 4810013377136TP2 0.99999620 -infinity 0.99997807 0.99998187 4810013377136TP3 1.0000000 0.99998593 0.99998885 +infinity 4810013377136TP4 0.99999708 -infinity 0.999999291 0.99999583 4810013377136TP5 0.99999729 -infinity 0.99999510 1.00000281 5821012483022FX2 0.99987953 -infinity 0.99981302 0.99993348 5821012483022FX3 0.99993298 -infinity 0.99998126 0.999994827 5821012483022FX4 0.99997400 -infinity 0.99998873 +infinity 5821012483022FX5 1.00001087 0.99997786 0.999998873 +infinity 5821012483022FX6 1.0000000 0.99999252 0.99999937 +infinity 5825012913073F7 1.0000000 0.99999252 0.99999937 +infinity 5895012913073F1 0.99998603 -infinity 0.99999994 1.00001383 5895012913073F10 0.9999888 <	4810012537542-12	0.99999809	-infinity	0.99999829	1.00000020
4810013377136TP2 0.99999620 -infinity 0.99997807 0.99998187 4810013377136TP3 1.0000000 0.99998593 0.99998885 +infinity 4810013377136TP4 0.99999708 -infinity 0.99999291 0.99999583 4810013377136TP5 0.99999229 -infinity 0.99999510 1.00000281 5821012483022FX2 0.99987953 -infinity 0.99988126 0.99993348 5821012483022FX3 0.99997400 -infinity 0.999988126 0.99994827 5821012483022FX4 0.99997786 0.999998873 +infinity 5821012483022FX5 1.0000000 0.99996665 0.999998873 +infinity 5821012483022FX6 1.0000000 0.99999665 1.0000352 1.00000352 5895012913073F7 1.0000000 0.999999252 0.9999999975 1.00000660 5895012913073F1 0.9999888 -infinity 0.99999999 1.00001383 5895012913073F10 0.99997888 -infinity 0.99999999 1.00002107 5895013640160LN2 0.99988314 -infinity	4810012537542-13	0.99999521	-infinity	0.99999920	1.00000399
4810013377136TP3 1.00000000 0.99998593 0.99998885 +infinity 4810013377136TP4 0.99999708 -infinity 0.99999291 0.99999583 4810013377136TP5 0.99999229 -infinity 0.99999510 1.00000281 5821012483022FX2 0.99987953 -infinity 0.99981302 0.99993348 5821012483022FX3 0.99993298 -infinity 0.99988126 0.99994827 5821012483022FX4 0.99997400 -infinity 0.99993707 0.99996306 5821012483022FX5 1.00001087 0.99997786 0.99998873 +infinity 5821012483022FX6 1.00000000 0.99999252 0.99999997 +infinity 5895012913073F7 1.00000000 0.999999252 0.999999997 1.00000660 5895012913073F9 0.99998803 -infinity 0.99999996 1.00001383 5895012913073F10 0.99997169 -infinity 0.99999999 1.00002107 5895013640160LN2 0.99988314 -infinity 0.99998094 0.99999079 5895013640160LN4 1.00000000	4810013377136TP1	0.99998576	-infinity	0.99996065	0.99997489
4810013377136TP4 0.99999708 -infinity 0.99999291 0.99999583 4810013377136TP5 0.99999229 -infinity 0.99999510 1.00000281 5821012483022FX2 0.99987953 -infinity 0.99981302 0.99993348 5821012483022FX3 0.99993298 -infinity 0.99988126 0.99994827 5821012483022FX4 0.99997400 -infinity 0.99993707 0.99996306 5821012483022FX5 1.00001087 0.9999786 0.999998873 +infinity 5821012483022FX6 1.00000000 0.999996665 0.99999937 +infinity 5895012913073F7 1.00000000 0.999999252 0.99999997 1.00000660 5895012913073F8 0.99999315 -infinity 0.99999999 1.00001383 5895012913073F10 0.99997888 -infinity 0.99999999 1.00002107 5895013640160LN2 0.99988314 -infinity 0.99998094 0.99992079 5895013640160LN3 1.00000000 0.99997917 0.99998826 +infinity 5895013823225FX2 0.99990266	4810013377136TP2	0.99999620	-infinity	0.99997807	0.99998187
4810013377136TP5 0.99999229 -infinity 0.99999510 1.00000281 5821012483022FX2 0.99987953 -infinity 0.99981302 0.99993348 5821012483022FX3 0.99993298 -infinity 0.99988126 0.99994827 5821012483022FX4 0.99997400 -infinity 0.99993707 0.99996306 5821012483022FX5 1.00001087 0.99997786 0.99998873 +infinity 5821012483022FX6 1.00000000 0.999996665 0.99999265 1.00000352 5895012913073F7 1.00000000 0.99999252 0.999999997 +infinity 5895012913073F8 0.999998603 -infinity 0.99999996 1.00001383 5895012913073F10 0.99997888 -infinity 0.99999999 1.00002107 5895013640160LN2 0.99988314 -infinity 0.999980394 0.999992079 5895013640160LN3 1.00000000 0.99993904 0.99999498 0.999995907 5895013640160LN6 0.9999806 -infinity 0.99999942 1.00000375 5895013823225FX2 0.999990266	4810013377136TP3	1.00000000	0.99998593	0.99998885	+infinity
5821012483022FX2 0.99987953 -infinity 0.99981302 0.99993348 5821012483022FX3 0.99993298 -infinity 0.99998126 0.99994827 5821012483022FX4 0.99997400 -infinity 0.99993707 0.99996306 5821012483022FX5 1.00001087 0.99997786 0.99998873 +infinity 5821012483022FX6 1.00000000 0.99996665 0.99999265 1.00000352 5895012913073F7 1.00000000 0.99999252 0.99999997 +infinity 5895012913073F8 0.999998603 -infinity 0.99999986 1.00001383 5895012913073F10 0.99997888 -infinity 0.99999999 1.00002107 5895012913073F11 0.99997169 -infinity 0.99999999 1.00002830 5895013640160LN2 0.99988314 -infinity 0.999980394 0.999992079 5895013640160LN3 1.00000000 0.99993904 0.99998826 +infinity 5895013823225FX2 0.99996192 -infinity 0.99999947 1.00003755 5895013823225FX3 0.99995191	4810013377136TP4	0.99999708	-infinity	0.99999291	0.99999583
5821012483022FX3 0.99993298 -infinity 0.99988126 0.99994827 5821012483022FX4 0.99997400 -infinity 0.99993707 0.99996306 5821012483022FX5 1.00001087 0.99997786 0.99998873 +infinity 5821012483022FX6 1.00000000 0.999996665 0.99999265 1.00000352 5895012913073F7 1.00000000 0.99999252 0.99999937 +infinity 5895012913073F8 0.999998603 -infinity 0.999999986 1.00001383 5895012913073F10 0.99997169 -infinity 0.99999999 1.00002107 5895012913073F11 0.99997169 -infinity 0.999980394 0.999992079 5895013640160LN2 0.99988314 -infinity 0.99980394 0.999992079 5895013640160LN3 1.00000000 0.99993904 0.99999498 0.99995907 5895013640160LN4 1.00000000 0.9999717 0.99998826 +infinity 5895013823225FX2 0.99996192 -infinity 0.999963927 0.99973658 5895013823225FX3 0.99995504	4810013377136TP5	0.99999229	-infinity	0.99999510	1.00000281
5821012483022FX4 0.99997400 -infinity 0.99993707 0.99996306 5821012483022FX5 1.00001087 0.99997786 0.99998873 +infinity 5821012483022FX6 1.00000000 0.99996665 0.99999265 1.00000352 5895012913073F7 1.00000000 0.99999252 0.99999937 +infinity 5895012913073F8 0.99999315 -infinity 0.999999975 1.00000660 5895012913073F9 0.99998603 -infinity 0.999999986 1.00001383 5895012913073F10 0.99997169 -infinity 0.999999999 1.00002107 5895013640160LN2 0.99988314 -infinity 0.999980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013823225FX2 0.999990266 -infinity 0.99993947 1.00003755 5895013823225FX3 0.99995504 -infinity 0.99973448 0.99978256 5895013902368E9 0.99995504	5821012483022FX2	0.99987953	-infinity	0.99981302	0.99993348
5821012483022FX5 1.00001087 0.999997786 0.99998873 +infinity 5821012483022FX6 1.00000000 0.99996665 0.99999265 1.00000352 5895012913073F7 1.00000000 0.99999252 0.99999937 +infinity 5895012913073F8 0.999998603 -infinity 0.99999986 1.00001383 5895012913073F10 0.999997888 -infinity 0.99999999 1.00002107 5895012913073F11 0.99997169 -infinity 0.999980394 0.99992079 5895013640160LN2 0.99988314 -infinity 0.99980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000000 0.99997917 0.99998826 +infinity 5895013640160LN6 0.9999806 -infinity 0.99999947 1.00003755 5895013823225FX2 0.99990266 -infinity 0.99993248 0.99973658 5895013823225FX4 1.0000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504	5821012483022FX3	0.99993298	-infinity	0.99988126	0.99994827
5821012483022FX6 1.00000000 0.99996665 0.99999265 1.00000352 5895012913073F7 1.00000000 0.99999252 0.99999937 +infinity 5895012913073F8 0.99999315 -infinity 0.999999975 1.00000660 5895012913073F9 0.99998603 -infinity 0.999999986 1.00001383 5895012913073F10 0.99997169 -infinity 0.99999999 1.00002107 5895012913073F11 0.99998314 -infinity 0.999980394 0.99992079 5895013640160LN2 0.99988314 -infinity 0.99994998 0.99995907 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000000 0.99997917 0.99998826 +infinity 5895013640160LN6 0.99996192 -infinity 0.999999947 1.00003755 5895013823225FX2 0.999995191 -infinity 0.999973448 0.999978256 5895013823225FX4 1.00000000 0.99978046 0.99998859 0.99993085 5985013902368E9 0.99998061	5821012483022FX4	0.99997400	-infinity	0.99993707	0.99996306
5821012483022FX6 1.00000000 0.99996665 0.99999265 1.00000352 5895012913073F7 1.00000000 0.99999252 0.99999937 +infinity 5895012913073F8 0.999998603 -infinity 0.99999986 1.00001383 5895012913073F10 0.99997169 -infinity 0.99999999 1.00002107 5895012913073F11 0.99997169 -infinity 0.99999999 1.00002830 5895013640160LN2 0.99988314 -infinity 0.999980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013640160LN6 0.99998906 -infinity 0.999999742 1.00000836 5895013823225FX2 0.99990266 -infinity 0.99993944 0.99973658 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.999982854 +infinity 5985013902368E10 0.99998061	5821012483022FX5	1.00001087	0.99997786	0.99998873	+infinity
5895012913073F8 0.99999315 -infinity 0.99999975 1.00000660 5895012913073F9 0.99998603 -infinity 0.99999986 1.00001383 5895012913073F10 0.99997888 -infinity 0.999999994 1.00002107 5895012913073F11 0.99997169 -infinity 0.999999999 1.00002830 5895013640160LN2 0.99988314 -infinity 0.999980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013640160LN5 0.99998906 -infinity 0.99999942 1.00000836 5895013823225FX2 0.99990266 -infinity 0.999963927 0.99973658 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.999993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.999994242	5821012483022FX6	1.00000000	0.99996665	0.99999265	
5895012913073F8 0.99999315 -infinity 0.99999975 1.00000660 5895012913073F9 0.99998603 -infinity 0.99999986 1.00001383 5895012913073F10 0.99997888 -infinity 0.99999999 1.00002107 5895012913073F11 0.99997169 -infinity 0.999999999 1.00002830 5895013640160LN2 0.99988314 -infinity 0.999980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000909 0.9999717 0.99998826 +infinity 5895013640160LN5 0.99998906 -infinity 0.99999742 1.00000836 5895013823225FX2 0.999996192 -infinity 0.999963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242	5895012913073F7	1.00000000	0.99999252	0.99999937	+infinity
5895012913073F10 0.99997888 -infinity 0.99999994 1.00002107 5895012913073F11 0.99997169 -infinity 0.99999999 1.00002830 5895013640160LN2 0.99988314 -infinity 0.99980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013640160LN5 0.99998906 -infinity 0.99999947 1.00000836 5895013823225FX2 0.999990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99988584 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242	5895012913073F8	0.99999315	-infinity	0.99999975	
5895012913073F10 0.99997888 -infinity 0.99999994 1.00002107 5895012913073F11 0.99997169 -infinity 0.99999999 1.00002830 5895013640160LN2 0.99988314 -infinity 0.99980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013640160LN5 0.99998906 -infinity 0.99999947 1.00000836 5895013823225FX2 0.999990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99988584 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242	5895012913073F9	0.99998603	-infinity	0.99999986	1.00001383
5895013640160LN2 0.99988314 -infinity 0.99980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013640160LN5 0.99998906 -infinity 0.99999742 1.00000836 5895013840160LN6 0.99996192 -infinity 0.99999947 1.00003755 58950138232225FX2 0.999990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.999992303 0.99994242	5895012913073F10	0.99997888		0.99999994	1.00002107
5895013640160LN2 0.99988314 -infinity 0.99980394 0.99992079 5895013640160LN3 1.00000000 0.99993904 0.99994998 0.99995907 5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013640160LN5 0.99998906 -infinity 0.99999742 1.00000836 5895013640160LN6 0.99996192 -infinity 0.99999947 1.00003755 5895013823225FX2 0.999990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.999992303 0.99994242	5895012913073F11	0.99997169	-infinity	0.99999999	1.00002830
5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013640160LN5 0.99998906 -infinity 0.99999742 1.00000836 5895013640160LN6 0.99996192 -infinity 0.99999947 1.00003755 5895013823225FX2 0.99990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.999992303 0.99994242	5895013640160LN2	0.99988314		0.99980394	0.99992079
5895013640160LN4 1.00000909 0.99997917 0.99998826 +infinity 5895013640160LN5 0.99998906 -infinity 0.99999742 1.00000836 5895013640160LN6 0.99996192 -infinity 0.99999947 1.00003755 5895013823225FX2 0.99990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242	5895013640160LN3	1.00000000	0.99993904	0.99994998	0.99995907
5895013640160LN5 0.99998906 -infinity 0.99999742 1.00000836 5895013640160LN6 0.99996192 -infinity 0.99999947 1.00003755 5895013823225FX2 0.99990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.999988589 0.999993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242	5895013640160LN4	1.00000909	0.99997917	0.99998826	
5895013640160LN6 0.99996192 -infinity 0.99999947 1.00003755 5895013823225FX2 0.99990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.999992303 0.99994242	5895013640160LN5				
5895013823225FX2 0.99990266 -infinity 0.99963927 0.99973658 5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.999988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242	5895013640160LN6				
5895013823225FX3 0.99995191 -infinity 0.99973448 0.99978256 5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.999993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242			-		
5895013823225FX4 1.00000000 0.99978046 0.99982854 +infinity 5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242		*****			
5985013902368E9 0.99995504 -infinity 0.99988589 0.99993085 5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242					
5985013902368E10 0.99998061 -infinity 0.99992303 0.99994242					
5985013902368E12 1.00000000 0.99996552 0.99996556 0.99996586					

5985013902368E13	1.00000000	0.99997683	0.99997713	0.99997717
5985013902368E14	0.99999619	-infinity	0.99998489	0.99998870
5985013934820EW2	0.99991122	-infinity	0.99987361	0.99996239
5985013934820EW3	0.99996644	-infinity	0.99993619	0.99996975
5985013934820EW4	0.99999119	-infinity	0.99996829	0.99997710
5985013934820EW5	1.00000000	0.99998169	0.99998446	0.99998512
5985013934820EW6	1.00000066	0.99999182	0.99999248	+infinity
5985013934820EW7	0.99999723	-infinity	0.99999640	0.99999917
5985013934820EW8	0.99999176	-infinity	0.99999829	1.00000653
5998013410403FX1	0.99996584	-infinity	0.99998071	1.00001487
5998013410403FX2	0.99995900	-infinity	0.99998873	1.00002973
5998013410403FX3	0.99994805	-infinity	0.99999265	1.00004460
6605012400136FX4	0.99834349	-infinity	0.99736299	0.99901787
6605012400136FX5	0.99941632	-infinity	0.99844819	0.99903130
6605012400136FX6	0.99971621	-infinity	0.99876122	0.99904474
6605012400136FX7	0.99982222	-infinity	0.99888056	0.99905817
6605012400136FX8	0.99991475	-infinity	0.99898643	0.99907161
6605012400136FX9	1.00000000	0.99899986	0.99908504	+infinity
6610013195039-36	1.00000000	0.99999320	0.99999478	0.99999579
6610013195039-37	1.00000101	0.99999765	0.99999866	+infinity
6610013195039-38	0.99999842	-infinity	0.99999895	1.00000053
6610013195039-39	0.99999576	-infinity	0.99999916	1.00000340
6610013195039-40	0.99999307	-infinity	0.99999934	1.00000627
6610013195039-41	0.99999034	-infinity	0.99999949	1.00000915
6610013195039-42	0.99998759	-infinity	0.99999961	1.00001202

Appendix G. CPLEX Solution Output for Models with Additional Constraints

						MAX)			
						_			
tgavail.mps	scaledg.mbs	-2.019744E+13	OPTIMAL SOLN	49		obj	rhs		BOUND
		OBJECTIVE VALUE	STATUS	ITERATION		OBJECTIVE	RHS	RANGES	BOUNDS
		PROBLEM NAME tgavail.mps DATA NAME scaledg.mps	PROBLEM NAME tgavail.mps DATA NAME scaledg.mps OBJECTIVE VALUE -2.019744E+13	UE	UE	UE	tqavail.mps scaledq.mps .UE -2.019744E+13 OPTIMAL SOLN 49 obj (tqavail.mps scaledq.mps .UE -2.019744E+13 OPTIMAL SOLN 49 obj (tqavail.mps scaledq.mps -2.019744E+13 OPTIMAL SOLN 49 obj (

SECTION 1 - ROWS

. DUAL ACTIVITY	1 -1.795928E+07	3.702126E+12	0	1.252644E+12	5.010691E+13	0	4.811602E+12	4.385271E+12	3.921013E+12	0	1.132177E+12	5.084468E+11	1.854723E+12	1.200597E+12	2.31384E+12	5.512747E+12	3.165864E+12	9.265769E+11	0	1.166002E+13	2.406099E+12	12.77279
UPPER LIMIT.	NONE 2700222	⊣	Н	-	Н	H	Н	Н	H	Н	Н	H	Н	Н	H	Н	Н	Н	П	н	Н	NONE
LOWER LIMIT.	NONE	7	NONE	₽	Н	NONE	Н	H	Н	NONE	Н	Н	-1	Н	Н	Н	Н	Н	NONE	Н	Н	-2.23025E+12
SLACK ACTIVITY	2.019744E+13	0	Н	0	0	⊣	0	0	0	⊢ 1	0	0	0	0	0	0	0	0	\leftarrow 1	0	0	0
ACTIVITY	-2.019744E+13 2700222		0	-	₽	0	-	Н	€=1	0	7	ਜ	1	1	1	7	1	Н	0	T	1	-2.23025E+12
. AT	BS	EQ	BS	E E	S S	BS	EQ	EQ	Ŏ G	BS	Ğ	Ŏ E	EQ	O E	Ğ H	E E	Ğ	EQ	BS	Ğ H	OH E	ΓΓ
Row	obj budget	order1	order2	order3	order4	order5	order6	order7			order10							·	•	Ŭ	Ū	avail
NUMBER	7	3	4	2	9	7	8	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23

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ATACTIVITYINPUT COS 1. LL 2. LL 3. LL 4. BS 4. BS 5. UL 7. 118006 2.841046 4. BS 5. UL 7. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 121806 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 1218066 5. 121806 5. 121	. LOWER LIMIT.	TINDER LIMIT	שייים השיוותשם
012982522-1 LL 012982522-2 LL 012982522-3 LL 012982522-3 LL 012982522-4 BS 012982522-4 BS 012982522-4 BS 012982522-4 BS 012982522-4 BS 013982522-4 BS 012912590FX3 LL 0		· · OFFEN DIMIT.	
5012982522-3 LL 0 -6.930248+1 5012982522-3 LL 0 -6.930248+1 5012982522-3 LL 0 -1.136008+1 5012982522-5 UL 0 -1.136008+1 5012982522-5 UL 0 -6.644221E+1 0013562584FX2 LL 0 -6.644221E+1 001312590FX3 LL 0 -7.439696E+1 0012912590FX3 LL 0 -7.439696E+1 0012912590FX3 LL 0 -7.439696E+1 0012912590FX3 LL 0 -2.979044E+1 001251893126 LL 0 -2.979044E+1 001251893129 LL 0 -2.97904E+1 001251893129 LL 0 -2.97904E+1 001251893129 LL 0 -2.348028E+1 0013387046B05 LL 0 -2.348028E+1 0013387046B05 LL 0 -2.348028E+1 0013389649B9 LL 0 -2.101321E+1 0013389649B1 LL 0 -2.101331E+1 0013389649B1 LL 0 -2.1013389649B1 LL 0 -2.1013389888888888888888888888888888888888		Н	1.949105E+1
001251893125 LL 0 0 1.380068+1 0.013562584FX1 LL 0 0 1.380068+1 0.013562584FX1 LL 0 0 1.439696E+1 0.013562584FX1 LL 0 0 1.439696E+1 0.013562584FX1 LL 0 0 1.439696E+1 0.012912590FX1 LL 0 1.439696E+1 0.012912590FX1 LL 0 1.439696E+1 0.012912590FX1 LL 0 1.439696E+1 0.012912590FX2 LL 0 1.2912590FX2 LL 0 1.2912590FX3 LL 0 1.2912590FX4 LL 0 1.704845E+1 0.012912590FX4 LL 0 1.704845E+1 0.012912590FX4 LL 0 1.704845E+1 0.012912590FX4 LL 0 1.704845E+1 0.012912590FX3 LL 0 1.704845E+1 0.01251893126 LL 0 1.704845E+1 0.01251893129 LL 0 1.704845E+1 0.01251893129 LL 0 1.704845E+1 0.01251893129 LL 0 1.704845E+1 0.01251893129 LL 0 1.704845E+1 0.01387046B0A BS			6.910135E+1
5012982522-5 UL 0013562584FX1 LL 0013562584FX1 LL 0013562584FX2 LL 0013562584FX2 LL 0012912590FX3 LL 001251893126 LL 001251893129 LL 001251893129 LL 00125189313 LS 0013387046BO3 UL 0013387046BO5 LL 0013387046BO5 LL 0013387046BO5 LL 0013389649BS LL 0013389649BS LL 0013389649BB LL 0013389649B	O C	-1 	.811859E+
0013562584FX1 LL 0013562584FX2 LL 0012912590FX2 LL 0012912590FX2 LL 0012912590FX2 LL 0012912590FX3 LL 0012912590FX3 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX4 LL 0012251893125 LL 0012251893125 LL 0012251893125 LL 0012251893129 LL 0012251893129 LL 0012251893131 BS 0012251893131 BS 0012251893131 BS 0012251893131 BS 0012351893131 BS 0012351893131 BS 0012351893131 BS 0013387046BO3 UL 0013387046BO3 LL 0013387046BO4 LL 0013387046BO5 LL 0013387046BO5 LL 0013389649B5 LL 0013389649B6 LL 0013389649B6 LL 0013389649B1 LL		1 -	.180139E+1
0012562584FX2 LL 0012912590FX0 LL 0012912590FX1 LL 0012912590FX1 LL 0012912590FX2 LL 0012912590FX3 LL 0012912590FX3 LL 0012912590FX3 LL 0012912590FX3 LL 0012912590FX3 LL 0012051893125 LL 0012051893126 LL 0012051893127 LL 0012051893129 LL 0012051893129 LL 0012051893129 LL 0012051893129 LL 0012051893129 LL 0012051893130 LL 001308069218-1 LL 001308069218-1 LL 0013387046B06 LL 0013387046B06 LL 0013387046B06 LL 0013389649B0 LL 0013389649B0 LL 0013389649B1 L		1 7	9.153964E+1
0012912590FX0 LL 0012912590FX1 LL 0012912590FX1 LL 0012912590FX1 LL 0012912590FX2 LL 0012912590FX3 LL 0012912590FX3 LL 0012912590FX4 LL 0012912590FX4 LL 001291893125 LL 0012251893126 LL 0012251893127 LL 0012251893127 LL 0012251893129 LL 0012251893130 LL 0012251893131 BS 0013251893131 BS 0013251893131 BS 0013251893131 LL 0013387046BO4 BS 0013387046BO4 BS 0013389649BS LL 001		-	.835526E+1
0012912590FX1 LL 0012912590FX2 LL 0012912590FX3 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX4 LL 001251893125 LL 0012251893125 LL 0012251893127 LL 0012251893129 LL 0012251893129 LL 0012251893130 LL 0013251893130 LL 0013251893131 BS 0013251893130 LL 0013251893130 LL 0013251893130 LL 0013387046BO5 LL 0013387046BO5 LL 0013387046BO5 LL 0013389649B5 LL 0013389649B6 LL 0013389649B6 LL 0013389649B1 BS 001743704 -2.330003E+1 0013389649B1 LL 0013389649B1 LL 0013389649B1 BS 001743704 -2.330003E+1 0013389649B1 LL 0013389649B1 LL 0013389649B1 BS 001743704 -2.330003E+1 0013389649B1 LL 0013		+	1.314431E+1
0012912590FX2 LL 0012912590FX3 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX5 BS 001251893125 LL 0012251893126 LL 0012251893127 LL 0012251893130 LL 0012251893130 LL 0012251893130 LL 0012251893130 LL 0012251893130 LL 0012251893130 LL 0013251893130 LL 0013251893130 LL 0013251893130 LL 0013251893130 LL 0013387046B04 BS 0013387046B05 LL 0013387046B05 LL 0013389649B5 LL 0013389649B6 LL 0013389649B7 LL 0013389649B9 LL 0013389649B1 LL 001338964		H	7.480357E+1
0012912590FX3 LL 0012912590FX4 LL 0012912590FX4 LL 0012912590FX5 BS 001251893125 LL 001251893126 LL 0012251893127 LL 0012251893130 LL 0012251893130 LL 0012251893130 LL 0012251893130 LL 0012251893130 LL 0012251893130 LL 0013251893130 LL 0013251893130 LL 0013251893130 LL 0013251893130 LL 0013251893130 LL 0013387046B03 UL 0013387046B04 BS 0013387046B05 LL 0013389649B5 LL 0013389649B7 LL 0013389649B7 LL 0013389649B1 LL 0013389649B		1	3.990649E+1
0012912590FX4 LL 0012912590FX5 BS 0012912590FX5 BS 0012251893125 LL 0012251893126 LL 0012251893127 LL 0012251893138 LL 0012251893139 LL 001225189313 BS 001225189313 BS 001225189313 BS 001236969218-2 LL 0013367046B03 UL 0013387046B04 BS 0013387046B05 LL 0013387046B05 LL 0013389649B5 LL 0013389649B6 LL 0013389649B7 LL 0013389649B1 LL		1	1.900518E+1
001251893125 LL 001251893125 LL 001251893126 LL 001251893126 LL 001251893127 LL 001251893128 LL 001251893139 LL 001251893139 LL 001251893131 BS 0012551893131 BS 0012551893131 BS 0012551893131 BS 0012551893131 BS 0013869218-2 LL 0013869218-2 LL 001387046BO3 UL 0013387046BO4 BS 0013387046BO5 LL 0013389649B5 LL 0013389649B6 LL 0013389649B9 LL 0013389649B9 LL 0013389649B1 LL 00133896		1	6.843595E+1
0012251893125 LL 0012251893126 LL 0012251893126 LL 0012251893127 LL 0012251893128 LL 0012251893130 LL 0012251893131 BS 0012251893131 BS 0012251893131 BS 0012251893131 BS 001236969218-1 0013369649B8 LL 0013389649B9 LL 0013389649B9 LL 0013389649B1 LL 0013489649B1 LL 0013489B1 LL 0013489B1 LL 0013489B1 L		7	1
001251893126 LL 001251893127 LL 001251893127 LL 001251893128 LL 001251893129 LL 001251893130 LL 001251893131 BS 001251893131 BS 001251893131 BS 0012369218-1 LL 0013369218-2 LL 0013387046BO3 UL 0013387046BO5 LL 0013387046BO5 LL 0013389649BS LL 0013389649B		-	.028483E+1
0012251893127 LL 0012251893128 LL 0012251893128 LL 0012251893129 LL 0012251893130 LL 0012251893131 BS 0012251893131 BS 0012369218-1 LL 0013369218-2 LL 0013387046BO3 UL 0013387046BO5 LL 0013387046BO5 LL 0013389649BS LL 0013		ı 	4.839109E+1
0012251893128 LL 0012251893129 LL 0012251893130 LL 0012251893131 BS 0012251893131 BS 0013269218-1 LL 0013969218-2 LL 0013387046BO3 UL 0013387046BO5 LL 0013387046BO5 LL 0013389649B5 LL 0013389649B6 LL 0013389649B7 LL 0013389649B9 LL 0013389649B9 LL 0013389649B9 LL 0013389649B9 LL 0013389649B1 LL 0013389649B13 BS 001743704 -2.333003E+1		I (-3.72965E+1
0012251893129 LL 0012251893130 LL 0012251893131 BS 0012251893131 BS 0013969218-1 LL 0013969218-2 LL 0013387046BO3 UL 0013387046BO5 LL 0013387046BO5 LL 0013389649B5 LL 0013389649B6 LL 0013389649B7 LL 0013389649B9 LL 0013389649B9 LL 0013389649B9 LL 0013389649B1 LL 0013389649B13 BS 001743704 -2.333003E+1		I (2.694593E+1
0012251893130 LL 0012251893131 BS 0013269218-1 LL 0013969218-2 LL 0013369218-2 LL 0013387046BO3 UL 0013387046BO5 LL 0013387046BO5 LL 0013389649B5 LL 0013389649B7 LL 0013389649B9 LL 0013389649B9 LL 0013389649B1 LL 0013389649B13 BS 0013489649B13 BS		-	.729803E+1
0012251893131 BS 0013969218-1 LL 0013969218-2 LL 0013387046BO3 UL 0013387046BO5 LL 0013387046BO5 LL 0013389649B5 LL 0013389649B6 LL 0013389649B9 LL 0013389649B9 LL 0013389649B9 LL 0013389649B9 LL 0013389649B1 LL 0013389649B13 BS 0017743704 -2.330003E+1 0013389649B13 BS 0017743704 -2.330003E+1 001389649B13 BS 0017743704 -2.330003E+1 001389649B13 BS 0017743704 -2.330003E+1 001389649B13 BS 0017743704 -2.330003E+1 001389649B13 BS 0017743704 -2.330003E+1		-	8.339022E+1
0013969218-1 LL 0013969218-2 LL 0013387046BO3 UL 0013387046BO5 LL 0013387046BO5 LL 0013387046BO5 LL 0013389649B5 LL 0013389649B6 LL 0013389649B9 LL 0013389649B9 LL 0013389649B1 LL 0013389649B13 BS 00013389649B13 BS		-	1
0013969218-2 LL 0013387046BO3 UL 013387046BO3 UL 013387046BO5 LL 0013387046BO5 LL 0013389649B5 LL 0013389649B6 LL 0013389649B9 LL 0013389649B1 LL 0013389649B13 BS 0017743704 -2.330003E+1 001389649B13 BS 0017743704 -2.330003E+1			1.443746E+1
0013387046B03 UL 0013387046B04 BS 0013387046B05 LL 0013389649B5 LL 0013389649B6 LL 0013389649B6 LL 0013389649B6 LL 0013389649B9 LL 0013389649B9 LL 0013389649B1 LL 0013389649B1 LL 0013389649B1 LL 0013389649B1 LL 0013389649B1 LL 0013389649B1 LL 0013389649B1 LL 0013389649B1 LL 0013389649B13 BS 001743704 -2010667E+1 001389649B13 BS 001743704 -2010667E+1 001389649B13 BS 001743704 -2010667E+1 001389649B13 BS 001743704 -2010667E+1 001389649B13 BS 001743704 -2010667E+1 001389649B13 BS 001743704 -2010667E+1		Н	↵
0013387046B04 BS 0013387046B05 LL 0013387046B05 LL 0013389649B5 LL 0013389649B6 LL 0013389649B7 LL 0013389649B9 LL 0013389649B1 LL 0013389649B13 BS 001743704 -2.330003E+1 5012180143-4 LL 0013389649B13 BS 001743704 -2.330003E+1		-	8.65607E+1
0013387046B05 LL 0013387046B06 LL 0013389649B5 LL 0013389649B6 LL 0013389649B8 LL 0013389649B9 LL 0013389649B1 LL 001338964B1 LL		#	
0013387046B06 LL 0013389649B5 LL 0013389649B6 LL 0013389649B7 LL 0013389649B9 LL 0013389649B1		П	.468143E+1
0013389649B5 LL 0013389649B6 LL 0013389649B6 LL 0013389649B7 LL 0013389649B8 LL 0013389649B9 LL 0013389649B1 L		Н	1.91403E+1
0013389649B6 LL 0013389649B7 LL 0013389649B7 LL 0013389649B8 LL 0013389649B9 LL 0013389649B10 LL 0013389649B11 LL 0013389649B12 BS 0013389649B13 BS 0013389649B13 BS 00134389649B13 BS 00134344 LL 001389649B13 BS 00134344 LL 00134344 LL 00134344 LL 0013444 LL 001344 LL 0013444 LL 001344 LL 0013444 LL 001344		Н	4.889484E+1
0013389649B7 LL 0013389649B8 LL 0013389649B8 LL 0013389649B9 LL 0013389649B10 LL 0013389649B11 LL 0013389649B12 BS 0013389649B13 BS 0013389649B13 BS 00134389649B13 BS 00134389649B13 BS 00134389649B13 BS 00134389649B13 BS 00134389649B13 BS 00134389649B13 BS 0013439649B13 BS 001343964B13 BS		+	.643164E+1
0013389649B8 LL 0013389649B9 LL 0013389649B9 LL 0013389649B10 LL 0013389649B11 LL 0013389649B12 BS 0013389649B13 BS 0013389649B13 BS 0013439649B13 BS 0013439649B13 BS 0013439649B13 BS 001343704 -2.330003E+1 001389649B13 BS 001343704 -2.330003E+1 001389649B13 BS 001343704 -2.33003E+1 001343736744 LL 001343736744 LL 001343736744 LL		Н	1.369795E+1
0013389649B9 LL 0013389649B10 LL 0013389649B11 LL 0013389649B12 LL 0013389649B13 LL 0013389649B13 LL 0013389649B13 LL 0013180143-1 LL 0013180143-2 LL 0013180143-3 LL 0013180143-4 LL 0013180143-4 LL 0013180143-4 LL 0013389649B13 LL 0013389649B13 LL 013389649B13 LL 013389649B1 LL 013389649B1 LL 013389649B1 LL 01338964B1 LL 013389649B1 LL 013389648B1 LL 013389649B1 LL 013389648B1 LL 013389649B1 LL 01338		Н	6.699347E+1
0013389649B10 LL 0013389649B11 LL 0013389649B12 BS 0013389649B13 BS 0013389649B13 BS 0013389649B13 BS 0013389649B13 BS 0013389649B13 BS 0013389649B13 BS 0013389649B13 BS 0013389649B13 BS 001343704 -2.330003E+1 0013380143-2 LL 0013380143-4 LL 0013380143-4 LL		Н	2.991521E+1
0013389649B11 LL 0.2256296 -4.600011E+1 0.13389649B12 BS 0.7743704 -2.330003E+1 0.13389649B13 BS 0.7743704 -2.330003E+1 0.12180143-2 LL 0.2256296 -1.740952E+1 0.12180143-3 LL 0.2149331E+1 0.12180143-4 LL 0.1373694E+1		Н	1.133518E+1
0013389649B12 BS		4	2.919862E+1
0013389649B13 BS		1	ı
5012180143-1 BS 1 -2.710667E+1 5012180143-2 LL 0 -2.149331E+1 5012180143-3 LL 0 -1.740952E+1 5012180143-4 LL 0 -1.373694E+1		7	
5012180143-2 LL 0 -2.149331E+1 5012180143-3 LL 0 -1.740952E+1 5012180143-4 LL 0 -1.373694E+1		1	
5012180143-3 LL 0 -1.740952E+1 5012180143-4 LL 0 -1.373694E+1		-	6.49009E+1
5012180143-4 LL 0 -1.373694E+1		1	1.450975E+1
		1	.294063E+1
5012188080-1 LL 06.930024E+1		-	1.338479E+1
5012188080-2 LL 0 -5.160013E+1		1	2 589958E+1

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-3.846837E+12
-5.107416E+12
-8.206825E+12
-3.864164E+12
-1.715666E+12
-6.896905E+11
                                                                                                                                      -2.217306E+11
-7.346723E+11
-1.318715E+12
                                                                                                                                                                                E+10
                                     -4.671759E+10
                                               -2.963313E+10
                                                                                        2.102683E+11
5.688214E+10
                                                                                                                                                                -1.159266E+10
-1.318221E+11
                                                                                                                                                                                    -5.390317E+10
                                                          -3.677042E+10
                                                              -1.407423E+11
-2.634143E+11
                                                                        -6.279534E+11
                                                                                                                                                                                                                        -6.283119E+10
-1.759989E+11
                                                                                                             -1.486621E+11
-2.976242E+11
                                                                                                                      -4.468862E+11
                                                                                                                           -8.560373E+11
                                                                                                                                                                                         -1.778133E+11
                                                                                                                                                                                              -3.398252E+11
                                                                                                                                                                                                   -6.421389E+11
                                                                                                                                                                                                                    9.335852E+09
                                                                                                                                                                                                                                  .094669E+11
                                                                                                  1.459621E+11
                                                                                                                                                                                                         -1.686474E+11
                                                                                                                                                                               1.390287
 -6.293198E+11
-1.127006E+11
-7.350027E+10
-6.300002E+09
-2.5E+09
                                                                                                                               -5.002125E+11
-1.174007E+11
-2.580003E+10
-5.300001E+09
-3.607951E+12
-2.65553E+12
-1.714747E+12
-3.930008E+10
-3.070005E+10
-6.381204E+11
                                   -1.710001E+10
-8.000003E+09
-3.935077E+11
-2.193024E+11
               -3.17105E+11
-1.554012E+11
-7.520028E+10
                                                                                                                                                                                                                  -1.554012E+11
-7.520028E+10
-3.600006E+10
                                                                                                                 -6E+08
-1E+08
                                                                                                                                                                         -7.697296E+11
-5.162133E+11
-3.444059E+11
                               -3.600006E+10
                                                        -1.115006E+11
-7.090025E+10
                                                                   -4.900012E+10
-1.869975E+12
                                                                             -1.187471E+12
                                                                                                                           -1.960792E+12
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-1.511011E+11
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-1.26398E+12
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                                                                                                                                                                                                        6.381204E+11
                                                                                                                                                                                                             -3.17105
4810012537542-7
4810012537542-8
14810012537542-9
14810012537542-10
4810012537542-11
4810012537542-11
                                             4810013377136TP1
4810013377136TP2
4810013377136TP3 1
4810013377136TP4 1
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5821012483022FX6
5895012913073F7
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5895012913073F9
5895012913073F10
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5985013902368E10
                                         810012537542-13
                                                                                                                                               5895013640160LN6
                                                                       5821012483022FX2
5821012483022FX3
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5895013640160LN2
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5895013640160LN5
                                                                                                                                                    5895013823225FX2
5895013823225FX3
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                                                                                                                                                                                                        5985013934820EW3
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5985013934820EW8
    835012188080-4
8350121
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-5.007704E+11 -7.284378E+11 -1.585879E+13 -5.262483E+12 -2.406279E+12 -1.489941E+12 -7.085813E+11 1.95716E+11 1.95716E+11 1.95716E+11 1.95716E+11 1.95716E+11 1.95716E+11		. DUAL ACTIVITY	1.510864E+12 0 1.097035E+12 1.173229E+13 2.589686E+12 2.539618E+12 3.272004E+12
ਜਜਜਜਜਜਜਜਜ		UPPER LIMIT.	NONE 2700222 1 1 1 1 1
000000000000		LOWER LIMIT.	NONE NONE 1 NONE 1 NONE 1
-1.929019E+11 -1.12706E+11 -2.640493E+13 -1.553015E+13 -1.239548E+13 -1.120067E+13 -1.014084E+13 -9.153788E+12 -5.220014E+10 -1.050001E+10		SLACK ACTIVITY	1.907437E+13 0 0 1 0 1 0 0 0 0 0 0 0
1000 1100 1100 1100 1110 1110 1110 111	(MAX)	ACTIVITY	-1.907437E+13 2700222 1 0 0 1 1 1 1
998013410403FX1 LL 5998013410403FX2 LL 5998013410403FX3 LL 5605012400136FX4 LL 5605012400136FX5 LL 5605012400136FX7 LL 5605012400136FX7 LL 5605012400136FX9 LL 5605012400136FX9 LL 5605012400136FX9 LL 5605012400136FX9 LL 5610013195039-36 LL 5610013195039-37 UL 5610013195039-41 LL 5610013195039-41 LL 5610013195039-42 LL 5610013195039-41 LL 5610013195039-42 LL 5610013195039-42 LL 5610013195039-43 LL 5610013195039-43 LL 5610013195039-43 LL	E obj rhs BOUND 1 - ROWS	ROW AT	bbidget UL order1 EQ order2 EQ order4 EQ order5 Order5 Order6 EQ order6 EQ order6 EQ order6 EQ order7 EQ order8
110 599801 111 599801 112 599801 113 660501 114 660501 115 660501 116 660501 117 660501 118 660501 119 661001 120 661001 121 661001 122 661001 123 661001 124 661001 125 661001 125 661001 126 61001 127 60001 127 60001 128 61001 128 61001 128 61001 128 61001 128 61001 128 61001 128 61001 128 61001 128 61001 128 61001 128 61001 128 61001 128 81001 128 81001 128 81001 128 81001 128 81001 128 81001 128 81001 128 81001	OBJECTIVE RHS RANGES BOUNDS	NUMBER	10845978801

0 4.398023E+11 4.408471E+11 9.259803E+11 1.889828E+12 3.481568E+12 1.677947E+12 1.677947E+12 1.077947E+12 1.077947E+12 5.087288E+11 		REDUCED COST.	-5.432913E+11	01	1 2004000	-2.386166E+11 -5.78436E+11	7.808194E+1	5.143987E+1	1.329992E+1	7.604845E+1	4.084015E+1	.962762E+1	7.154813E+1	1	6.698361E+1	-4.241447E+10	2.364772E+1	1.028308E+1	2.020361E+0	.240593E+0	0-	.000762E+1	1.001088E+1	.101281E+1		3.913354E+1	\vdash	2.413136E+1
350000		UPPER LIMIT.	1	← ←	4.		1	1	 1	Н	н	\leftarrow	н	⊣	Н	1	1	~	, , ,	Н	T	П	1	Н	П	1	П	Н
NONE 1 1 1 1 1 1 1 1 NONE 1 NONE		LOWER LIMIT.	0	0 0	,	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
ноооооопооо		INPUT COST	.645235E+1	6.93024E+1 2.84104E+1	1380081	-4.47001E+10	.644221E+1	2.81604E+1	1.439696E+1	8.674962E+1	5.127214E+1	79044E+1	1.704845E+1	9.624463E+1	2.642249E+1	2.544424E+1	2.452401E+1	2.36578E+1	2.284261E+1	2.207744E+1	2.135728E+1	6.176191E+1	2.348028E+1	.382351E+1	6.679223E+1	5.788168E+1	5.10113E+1	.755005E+1
350000		ACTIVITY		0.4345089	1000	00	0	0	0	0	0	0	0	← 1	0	0	0 (0	0	1	0	0	0	\leftarrow	0	0	0	0
L V V V V V V V V V V V V V V V V V V V		AT				11																		UĽ	BS	LL	디	김
11 order9 12 order10 13 order11 14 order12 15 order13 16 order14 17 order15 18 order16 19 order17 20 order19 21 order19 22 order20 23 subbud	2 - 0	BERCOLUMN	4 1005012982522	5 1005012982522 6 1005012982522	7 1005012080500	28 1005012982522-5	9 1270013562584	0 1270013562584	1 156001291259	2 1560012912590	3 1560012912590	4 1560012912590	5 1560012912590	6 156001291259	7 1630012251893	8 1630012251893	9 1630012251893	0 1630012251893	1 1630012251893	2 1630012251893	3 1630012251893	4 1650013969218	5 1650013969218	6 1660013387046	7 1660013387046	8 1660013387046BO	9 1660013387	0 1660013389649B
	SECTION	NUMBE																										

0 -1.141165E+12 0 -7.697296E+11 0 -3.444059E+11 1 -2.287026E+11 0 -1.26398E+12 0 -6.381204E+11 0 -1.26398E+12 0 -6.381204E+11 0 -1.554012E+11 1 -7.520028E+10 0 -1.554012E+11 1 -7.520028E+10 0 -1.929019E+11 0 -1.12706E+10 0 -1.23015E+13 0 -1.23067E+13 0 -1.23067E+13 0 -1.23067E+13 0 -1.24084E+13 1 -1.340001E+10 1 -1.340001E+10 0 -5.20014E+10 0 -6.60002E+09 0 -6.600002E+09 0 -6.600002E+09 0 -6.600001E+09 0 -6.10001E+09

(MAX)

obj rhs BOUND

OBJECTIVE RHS RANGES BOUNDS

SECTION	1 - ROWS						
NUMBER	ROW	AT	ACTIVITY	SLACK ACTIVITY	LOWER LIMIT.	UPPER LIMIT.	.DUAL ACTIVITY
1	obj	BS	-1.932966E+13	1.932966E+13	NONE	NONE	
2	budget	or I	70022	0 (NONE	2700222	.774068E+0
m ·	orderl	Ö	. (0	П		4.4902/9E+11
4	order2	BS	0		NONE	- 1	
വ	order3	S S	Н	0	.	. 1	1.249112E+12
9	order4	O O	Н	0	Н	Н	.220438
7	order5	BS	0	-	NONE	7	0
∞	order6	EO	\leftarrow	0	Н	\vdash	4.761164E+12
9	order7	EQ	ᆏ	0	Н	Н	6.144633E+11
10	order8	EQ	-	0	П	Н	3.90628E+12
11	order9	BS	0	₽	NONE	Н	
12	order10	OH OH	H	0	Н	Н	8.543236E+11
13	order11	EQ.	٣	0	П	г	.585285E+1
14	order12	EO	Н	0	Н	Н	3+1
15	order13	EO	Н	0	++	Н	.1860
16	order14	E O	-	0	٠	1	.838033E+1
17	order15	EO	~	0	-	4	.477969E
18	order16	E O		0	-		.136698E+1
0 -	order17	i E	-	C		-	079679E+1
000	order18	א ני א ני	10	· -	HINON	-, 1	1
7 0	0146118 014014	i C	-	4 C	1	4 ←	162052
4 (א כ ם ם	1 -		4 ~	4 ←	7.0107.
77	orderzu	3 :			T	T	7.108381E+12
73	suppna	3	000005	0	000005	NONE	.501948E
SECTION	2 - COLUMNS						
NUMBER	····COLUMN	ΑT	ACTIVITY	INPUT COST	LOWER LIMIT.	UPPER LIMIT.	REDUCED COST.
	0050129825	LL	0	-1.645235E+12	0	. !	-1.277073E+12
	0050129825		C	6.93024E+1	C	-	_
	0050129825		» c	2 84104E		4 ~	-7 76728E+10
) ,	4 -		4 +	7 77770777
17	1005012982522~4		-I C			-1	
	0000125000	, t		4/00151		-1 - -	1024155.
	2700135625			816045+1		- H	-7 77442BE+11
	5600109105			96968	o C	+ ←	-1 3147855+13
	5600129125	H	0	(- + (0)	0	1 	-7.483183E+12
	5600129125	П	0	27214E+1	0	-	-3.992769E+12
	5600129125	ΓΓ	0	79044E+1	0	1	.901931
	5600129125		0	04845E+1	0	1	ω.
	5600129125		⊣	24463E	0	1	

1630012251893125 UL	Η ¢	2.0	00	~ ~	5.820603E+10
012231833120	00	4524018+1) C	٠,	6.400841E+1
012251893128	0	-2.36578E+1	0	i (-1	.334189E+1
012251893129	0	2.284261E+1	0	Ļ	2.079314E+1
012251893130	0	2.207744E+1	0	~	2.874456E+1
012251893131	0 0	2.135728E+1	0 (н	3.714613E+1
013969218-1	> 0	0.1/6191E+1		٦ -	-I.43369E+1
0013387046	O F	.382351E+1	> 0	٠, -	8.529977E+11
0013387046BO4	0	6.679223E+1	0	H	1
0013387046BO5	0	5.788168E+1	0	⊣	9.34205E+1
0013387046BO6	0	5.10113E+1	0	\vdash	1.888812E+1
0013389649B5	0	3.755005E+1	0	Н	-3.377401E+12
0013389649B6	0	.101321E+1	0	Н	1.771089E+1
0013389649B7	0	1.154067E+1	0	Н	8.712068E+1
0013389649B8	0	6.232194E+1	0	Н	3.877316E+1
0013389649B9	0	3.313055E+1	0	Н	1.431896E+1
0013389649B10	0	1.737015E+1	0	Н	3.295754E+1
0013389649B11	T	8.99004E+1	0	Н	.471632E+0
0013389649B12	0	4.600011E+1	0	Ч	
0013389649B13	0	2.330003E+1	0	1	-2.467185E+10
5012180143-1	1	2.710667E+1	0	7	1
5012180143-2	0	2.149331E+1	0	⊣	.342766E+1
5012180143-3	0	1.740952E+1	0	П	1.42151E+1
5012180143-4	0	1.373694E+1	0	~	2.249866E+1
5012188080-1	0	6.930024E+1	0	⊶	1.323031E+1
5012188080-2	0	5.160013E+1	0	Н	2.559061E+1
5012188080-3	0	.93000BE+1	0	~	┥.
5012188080-4	0	3.070005E+1	0		5.045622E+1
0012537542-7	0 (6.381204E+1	0 (Н,	3.274031E+1
0012537542-8	00	-3.1/105E+1	.	⊢ ,	8.4045//E+1
001253/542-9) t	1.554012E+1		٦,	1 0 0 0 0 0
001753/542-IO	⊣ <	7.520028E+1	~	٠,	7.5428/9E+U
001253/542-11	0 0	3.600006E+1	~	٠,	.591495E+1
001253/542-12	0 (1./10001E+1	- (⊣ ,	9.46/294E+1
0012537542-13	0	8.000003E+0	0	Н.	1.63231E+1
0013377136TP1	0	3.935077E+1	0	\vdash	2.568849E+1
0013377136	0	2.193024E+1	0	⊣	53E+1
0013377136TP3	0	1.115006E+1	0	1	1.868915E+1
013377136TP4		7.090025E+1	0	₽	54230
0013377136	0	.900012E+1	0	\vdash	
1012483022FX2	0	1.869975E+1	0	7	6.354112E+1
012483022	0	.187471E+1	0	Н	.555288E+1
1012483022	0	.293198E+1	0	⊣	

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-7.20943E+11
-9.858638E+11
-1.587574E+13
-5.276041E+12
                                                                                                                                                                                                                                                                                -7.587657E+10
-1.325649E+11
-1.895533E+11
                                                                                                                                                                                                                                      -2.416448E+12
-1.49672E+12
-7.119709E+11
                                                                                                                                                                              E+10
      -4.942429E+10
                            -1.468392E+11
-2.939783E+11
                                         -4.414175E+11
                                                 -1.66019E+12
                                                                             -7.110062E+10
-1.159266E+10
                                                                                                                       1.681946E+10
                                                                                                                              -4.806999E+10
                                                                                                                                           -3.281589E+11
-6.570387E+11
                                                                                                                                                                .119049E+10
                                                                                                                                                                                     -1.816255E+11
-3.132388E+11
                                                                                                                                                                                                                                                                          -1.998822E+10
                                                                                                                                                                                                                                                                                                      .468416E+11
 2.139973E+11
                                                                                                                                     -1.690635E+11
                                                                                                                                                         -1.816925E+11
                                                                                                                                                                                                    -4.97023E+11
                                                                                                                                                                                                                                                                                                             .0443E+11
              1.441392E+11
                                                                                                         -1.347386E+11
                                                                                                                                                                               -7.031241
 -66+08
-1.9607926+12
-5.0021256+11
-1.1740076+11
-2.5800036+10
-5.3000116+09
-3.6079516+12
-2.655536+12
-1.7147476+12
-1.7147476+12
-1.7147476+12
-1.127006E+11
-7.350027E+10
-6.300002E+09
-2.5E+09
-1.4E+09
                                                                                                                             -3.444059E+11
-2.287026E+11
-1.511011E+11
-1.26398E+12
                                                                                                                                                                      -1.554012E+11
-7.520028E+10
-3.60006E+10
-1.710001E+10
                                                                                                                                                                                                                                                    -1.014084E+13
-9.153788E+12
-5.220014E+10
                                                                                                                                                                                                                                             -1.120067E+13
                                                                                                                                                                                                                                                                                       .400004E+09
                                                                                                                                                                                                                                                                                               .600002E+09
                                                                                                                                                         -6.381204E+11
                                                                                                                                                                -3.17105E+11
                                                                                                                                                                                                   -1.929019E+11
                                                                                                                                                                                                          -1.127006E+11
                                                                                                                                                                                                                  -7.350027E+10
                                                                                                                                                                                                                        -2.640493E+13
                                                                                                                                                                                                                               -1.553015E+13
                                                                                                                                                                                                                                                                         -1.340001E+10
                                                                                                                                                                                                                                                                                 -1.050001E+10
-8.400004E+09
                                                                                                                                                                                                                                                                                                     -5.100001E+09
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 HOHOOOOO
                                                              0.3229087
                                                                     0.6770913
                                                                                                  0.9367179
                                                                                                         0010000001000000000011000000
                                                                                                               5985013902368E10
                                  5895012913073F10
5895012913073F11
                                                                                                                                    5985013902368E13
                                                                                                                                           5985013902368E14
                                                                                                                                                         5985013934820EW3
                                                                                                                                                                              5985013934820EW6
                                                                                                                                                                                     5985013934820EW7
5985013934820EW8
                                                                                                                                                                                                                        6605012400136FX4
                                                                                                                                                                                                                               6605012400136FX5
6605012400136FX6
                                                                                                                                                                                                                                                    6605012400136FX8
6605012400136FX9
                                                                                                                                                                                                                                                                  6610013195039-36
                                                                                                                                                                                                                                                                                       6610013195039-39
                                                                                                                                                                                                                                                                                               610013195039-40
       821012483022FX6
             5895012913073F7
5895012913073F8
5895012913073F9
                                                 895013640160LN2
                                                        5895013640160LN3
5895013640160LN4
                                                                     895013640160LN5
                                                                             895013640160LN6
                                                                                   5895013823225FX2
                                                                                          5895013823225FX3
                                                                                                  5895013823225FX4
5985013902368E9
                                                                                                                       5985013902368E11
                                                                                                                              5985013902368E12
                                                                                                                                                   5985013934820EW2
                                                                                                                                                                5985013934820EW4
5985013934820EW5
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5998013410403FX3
                                                                                                                                                                                                                                              6605012400136FX7
                                                                                                                                                                                                                                                                         6610013195039-37
                                                                                                                                                                                                                                                                                 6610013195039-38
                                                                                                                                                                                                                                                                                                            6610013195039-42
 821012483022FX5
                                                                                                                                                                                                                                                                                                      6610013195039-41
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Level	
Control	
Inventory	
Modeled:	
Constraint	
Additional	

TRABT									
INGICOTY COULTS						(MAX)			
T :DATADOM INTE	tqinvc.mps	scaledg.mps	-1.925901E+13	OPTIMAL SOLN	59	obj	rhs		BOUND
PROTECTIONAL CONSCIUNT MODELEUS INVENTOLY CONTROL DEVEL	PROBLEM NAME			STATUS	ITERATION	OBJECTIVE	RHS	RANGES	BOUNDS

SECTION 1 - ROWS

.DUAL ACTIVITY	1 -8188136	1.478418E+12	0	1.094756E+12	1.156978E+13	0	2.557141E+12	2.958531E+12	3.262498E+12	0	4.302703E+11	6.498736E+11	9.115435E+11	4.842649E+11	1.775209E+12	3.451647E+12	1.655363E+12	5.027452E+11	0	1.029645E+13	1.029007E+12	-1.493711E+11
UPPER LIMIT.	NONE 2700222		← 1		\vdash	1	1		1	1		Н	1	П	1	1			+	₩	Н	15
LOWER LIMIT.	NONE	+-1	NONE	1	Н	NONE	1	Н	П	NONE	Н	Н	П	7	7	7	\leftarrow	H	NONE	4	Н	NONE
SLACK ACTIVITY	1.925901E+13	0	ч	0	0	, - 1	0	0	0	Н	0	0	0	0	0	0	0	0	⊢ 1	0	0	0
ACTIVITY	-1.925901E+13 2700222	Н	0	H	Н	0	Н	Н	н	0	Н	Н	н	Н	H	F	F	e	0	\leftarrow	⊣	15
AT	BS	EQ	BS	ద	G G	BS	O E	ద	OG G	BS	Ğ G	Ğ Б	O B O	O B O	ద	Ö Ш	Ö Ш	Ŏ Н	BS	O G	O E O	ď
ROW	obj budget			order3		order5	order6		-	-	-	-	order12		-	•	•	order17	Ĭ	order19	order20	invcont
NUMBER	7 7	3	4	2	9	7	80	6	10	11	12	13	14	15	16	17	18	19	20	21	22	23

SECTION 2 - COLUMNS

NUMBER	····COLUMN	AT	ACTIVITY	INPUT COST	LOWER LIMIT.	UPPER LIMIT.	REDUCED COST.
24	1005012982522-1	LL	0	645235E+1	0	1	-5.595145E+11
25	005012982522-2	BS	0	3024E+1	0	-	
26	005012982522-3	Ωľ	-	2.84104E+1	0	-	.622319E+1
27	005012982522-4	Ľ	0	38006E+1	0	₹-1	.061702E+1
28	005012982522-5	ΓΓ	0	4.47001E+1	0	⊣	.297664E+
29	270013562584FX1	ΓĽ	0	.644221E+1	0		7.788482E+1
30	270013562584FX2	ΓΓ	0	2.81604E+1	0	। स्न	4563E+1
31	560012912590FX0	ΓΓ	0	.439696E+1	0	-	1.33022E+1
32	560012912590FX1	LL	0	.674962E+1	0		.606668E+1
33	560012912590FX2	Ľ	0	27214E+	0	I (I	4.085382E
34	560012912590FX3	Ľ	0	.979044E+1	0		.963674E+1
32	560012912590FX4	ΓĽ	0	.704845E+1	0	н	7.159372E+1
36	560012912590FX5	BS	↔	9.624463E+1	0	Н	
37	630012251893125	$\Gamma\Gamma$	0	.642249E+1	0	-	.442716E+1
38	630012251893126	LL	0	.544424E+1	0	₽	4.861744E+1
39	530012251893127	LL	0	2.452401E+1	0	l (2.861009E+1
40	530012251893128	$\Gamma\Gamma$	0	2.36578E+1	0	-	.400486E+1
41	530012251893129	ΓΓ	0	2.284261E+1	0	1 5-1	4.501546E+0
42	530012251893130	BS	35878	2.207744E+1	0	-	
43	530012251893131	BS	.564121	2.135728E+1	0	l e l	0 1
44	550013969218-1	ΓΓ	0	6.176191E+1	0	l (.942733E+1
45	550013969218-2	LL	0	.348028E+1	0	l (9.881113E+1
46	560013387046B03	Ωľ	Н	8.382351E+1	0	l (3.019919E+1
47	560013387046BO4	BS	0	.679223E+1	0	1	1
48	560013387046B05	LL	0	5.788168E+1	0	-	3.831991E+1
49	560013387046BO6	ΓĽ	0	5.10113E+1	0	-	7.868001E+1
20	560013389649B5	LL	0	.755005E+1	0	I ←	256044E+1
51	560013389649B6	ĽĽ	0	.101321E+1	0		8.942735E+1
52	560013389649B7	ĽĽ	0	1.154067E+1	0		2.389332E+1
53	560013389649B8	BS	1	6.232194E+1	0	-	
54	560013389649B9	BS	-3.108624E-15	313055E+1	0	I ←	
52	560013389649B10	$\Gamma\Gamma$	0	1.737015E+1	0		431E+1
26	560013389649B11	LL	0	8.99004E+1	0	4 +	424228E+
57	560013389649B12	$\Gamma\Gamma$	0	.600011E+1	0	1	5.904364E+1
28	560013389649B13	ĽĽ	0	.330003E+1	0		8.5965038+1
29	35012180143-1	BS	0	.710667E+1	0		
0.9	35012180143-2	Ωľ	₽	.149331E+1	0	-	.506219E+0
61	35012180143-3	TT	0	.740952E+1	0	Н	.339445E+1
62	35012180143-4	LL	0	.373694E+1	0	+	.185175E+1
63	35012188080-1	LL	0	-6.930024E+10	0	1	479543E
64	35012188080-2	Ľ	0	5.160013E+1	0	П	1.208908E+1

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5985013902368E10
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810013377136TP4
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                                                                                                                              895013640160LN4
                                                                                                                                  5895013640160LN5
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895013823225FX3
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                                                                                                                                                                     5985013902368E11
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                                                                                                                                                                                    5985013902368E14
                                                                                                                895012913073F11
                                                                                                                                                                          5985013902368E12
                                                                                                                                                                                         5985013934820EW2
                                                                                                                                                                                             5985013934820EW3
                                                                                                                                                                                                  5985013934820EW4
                                                                                                                                                                                                            5985013934820EW6
                                                                                                                                                                                                                      5985013934820EW8
                                                                                                                                                                                                        5985013934820EW5
                                                                                                                                                                                                                 5985013934820EW7
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6605012400136FX5 L
6605012400136FX6 L
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6610013195039-39 I
6610013195039-40 I
6610013195039-41 I
6610013195039-42 I
5998013410403FX1
5998013410403FX2
```

Appendix H	: Parametrio	Analys	is Output D	ata			
Parametric C	Output Data fo	r the PL	DMa Budge	t Constraint			
Variable	Variable	Pivot	RHS	Dual Price	Obj Value	Obj Value	Q
OUT	IN	Row	Value	Before Pivot	(scaled)	(unscaled)	
			2700220	8.67209	-18852600	-0.00188526	0.99811652
NSN16-12	NSN4-130	5	2699100	8.67209	-18862300	-0.00188623	0.99811555
NSN4-130	NSN10-10	5	2690310	8.69993	-18938900	-0.00189389	0.9981079
NSN10-10	NSN7-10	5	2685930	8.95514	-18978100	-0.00189781	0.99810399
NSN7-10	NSN4-128	5	2668520	9.0533	-19135700	-0.00191357	0.99808826
NSN4-128	NSN17-5	5	2659730	9.26866	-19217200	-0.00192172	0.99808013
NSN17-5	NSN4-127	5	2651240	9.4531	-19297400	-0.00192974	0.99807212
NSN4-129	NSN4-128	21	2651240	9.5587	-19297400	-0.00192974	0.99807212
NSN4-128	NSN4-126	21	2642450	9.84875	-19384000	-0.00193840	0.99806348
NSN4-126	NSN16-11	21	2633650	10.463	-19476000	-0.00194760	0.9980543
NSN16-13	NSN4-125	3	2633650	10.7746	-19476000	-0.00194760	0.9980543
NSN4-127	NSN4-126	5	2633650	10.7928	-19476000	-0.00194760	0.9980543
NSN4-126	NSN14-3	5	2624860	11.1227	-19573900	-0.00195739	0.99804452
NSN14-3	NSN20-37	5	2591200	11.3723	-19956700	-0.00199567	0.99800632
NSN20-37	NSN16-12	5	2587880	11.7088	-19995500	-0.00199955	0.99800245
NSN16-12	NSN11-2	5	2574540	12.8771	-20167300	-0.00201673	0.9979853
NSN11-2	NSN10-9	5	2566490	13.3915	-20275100	-0.00202751	0.99797454
NSN10-11	NSN1-2	19	2566490	13.6384	-20275100	-0.00202751	0.99797454
NSN1-2	NSN17-4	19	2536770	13.7605	-20684000	-0.00206840	0.99793374
NSN17-6	NSN12-4	18	2536770	14.2564	-20684000	-0.00206840	0.99793374
NSN12-6	NSN7-8	16	2536770	16.292	-20684000	-0.00206840	0.99793374
NSN7-8	NSN11-1	16	2519360	16.7685	-20975900	-0.00209759	0.99790461
NSN11-3	NSN15-3	14	2519360	17.516	-20975900	-0.00209759	0.99790461
NSN15-3	NSN15-2	14	2466330	17.7407	-21916700	-0.00219167	0.99781073
NSN15-4	NSN15-3	13	2466330	17.85	-21916700	-0.00219167	0.99781073
NSN15-3	NSN10-10	13	2413300	17.9593	-22869100	-0.00228691	0.9977157
NSN10-10	NSN16-10	13	2408930	18.3216	-22949300	-0.00229493	0.9977077
NSN16-10	NSN17-5	13	2395580	19.0013	-23202800	-0.00232028	0.99768241
NSN17-5	NSN11-2	13	2387100	19.0597	-23364500	-0.00233645	0.99766628
NSN11-2	NSN1-1	13	2379050	21.6404	-23538700	-0.00235387	0.9976489
NSN1-3	NSN16-9	17	2379050	22.9017	-23538700	-0.00235387	0.9976489
NSN16-11	NSN7-7	21	2379050	23.4204	-23538700	-0.00235387	0.9976489
NSN7-9	NSN14-2	6	2379050	23.6311	-23538700	-0.00235387	0.9976489
NSN14-4	NSN16-10	9	2379050	27.381	-23538700	-0.00235387	0.9976489
NSN16-10	NSN12-5	9	2365710	27.8395	-23910200	-0.00239102	0.99761184
NSN12-5	NSN7-8	9	2348650	30.2859	-24426800	-0.00244268	0.9975603
NSN7-8	NSN1-2	9	2331240	30.4936	-24957600	-0.00249576	0.99750735
NSN1-2	NSN12-3	9	2301520	32.0428	-25909900	-0.00259099	0.99741236
NSN12-3	NSN12-2	9	2284470	32.7206	-26468000	-0.00264680	0.9973567

NSN12-4							,
	NSN10-8	18	2284470	36.3656	-26468000	-0.00264680	0.9973567
	NSN17-3	18	2280090	36.9406	-26629700	-0.00266297	0.99734057
NSN17-3	NSN12-3	18	2271600	37.8374	-26950700	-0.00269507	0.99730856
NSN12-3	NSN14-3	18	2254550	40.0106	-27633200	-0.00276332	0.99724049
NSN14-3	NSN7-6	18	2220880	43.3898	-29093800	-0.00290938	0.99709485
NSN7-6	NSN10-7	18	2203480	54.4134	-30041100	-0.00300411	0.9970004
NSN10-9	NSN17-2	5	2203480	55.1377	-30041100	-0.00300411	0.9970004
NSN17-4	NSN19-8	19	2203480	55.803	-30041100	-0.00300411	0.9970004
NSN19-8	NSN19-7	19	2187970	63.6575	-31028100	-0.00310281	0.996902
NSN19-9	NSN19-8	2	2187970	66.0043	-31028100	-0.00310281	0.996902
NSN19-8	NSN10-8	2	2172460	68.3512	-32087900	-0.00320879	0.99679635
NSN10-8	NSN17-3	2	2168090	73.3347	-32409000	-0.00324090	0.99676435
NSN17-3	NSN7-5	2	2159600	73.7687	-33034800	-0.00330348	0.99670197
NSN7-7	NSN19-6	21	2159600	74.7033	-33034800	-0.00330348	0.99670197
NSN19-6	NSN7-6	21	2144100	77.0564	-34229600	-0.00342296	0.99658289
NSN7-6	NSN19-5	21	2126690	94.9931	-35883300	-0.00358833	0.9964181
NSN19-7	NSN19-6	19	2126690	139.61	-35883300	-0.00358833	0.9964181
NSN19-6	NSN3-5	19	2111180	202.163	-39018000	-0.00390180	0.9961058
NSN3-5	NSN3-3	19	2107950	229.722	-39760400	-0.00397604	0.99603185
NSN3-3	NSN3-2	19	2104720	394.278	-41034600	-0.00410346	0.99590495
NSN3-4	NSN3-3	12	2104720	529.495	-41034600	-0.00410346	0.99590495
NSN3-3	NSN19-4	12	2101490	664.712	-43182800	-0.00431828	0.99569103
NSN19-4	NSN3-1	12	2085980	701.343	-54057500	-0.00540575	0.99460883
NSN3-1	NSN3-0	12	2082750	1097.79	-57605300	-0.00576053	0.99425603
NSN3-2	NSN3-1	19	2082750	1434.18	-57605300	-0.00576053	0.99425603
NSN3-1	ART	19	2079520	1770.57	-63327300	-0.00633273	0.99368728
			1900200	+INFINITY	INFEASIBLE		
Parametric Ou	utput Data for	the RF	IS of Two Si	ub-budget Con	straints		
VAR	VAR	Pivot	RHS	Dual Price	Obj Val	Obj Value	Q
OUT	IN	Row	Val	Before Pivot	(scaled)	(unscaled)	
			0	5.43135	-19074400.	-0.00190744	0.99809438
SLK 24	NSN10-10	17	0.630859	5.43135	-19074400.	-0.00190744	0.99809438
NSN10-10	NSN10-9	17	4378.03	4.8054	-19053300.	-0.00190533	0.99809648
NSN10-11	NSN12-4	5	4378.03	0.12217	-19053300.	-0.00190533	0.99809648
NSN12-6	NSN15-4	12	4378.03	-2.53144	-19053300.	-0.00190533	0.99809648
NSN1-2	NSN11-2	3	12912.2	-3.98014	-19087300.	-0.00190873	0.99809309
NSN11-2	NSN14-3	3	20962.2	-4.34915	-19122300.	-0.00191223	0.9980896
NSN14-3	NSN7-10	3	54624.1	-6.3684	-19336700.	-0.00193367	0.9980682
NSN15-4	NSN15-2	12	57409	-8.68737	-19360900.	-0.00193609	0.99806578
NSN7-10	SLK 23	3	72032.5	-8.90598	-19491100.	-0.00194911	0.99805279
NSN8-1	NSN4-130	23	79617.8	-9.63009	-19564200.	-0.00195642	0.99804549
110110-1							

NSN7-9	NSN20-38	18	88412.9	-11.0257	-19650100.	-0.00196501	0.99803692
NSN20-36	NSN8-3	21	88412.9	-11.6673	-19650100.	-0.00196501	0.99803692
NSN15-2	NSN10-10	12	110440	-11.8997	-19912200.	-0.00199122	0.99801076
NSN10-10	NSN12-5	12	114817	-12.262	-19965900.	-0.00199659	0.9980054
NSN12-5	NSN12-3	12	131875	-24.2263	-20379100.	-0.00203791	0.99796417
NSN12-3	NSN12-2	12	148934	-26.661	-20833900.	-0.00208339	0.99791878
NSN12-4	NSN10-8	5	148934	-30.306	-20833900.	-0.00208339	0.99791878
NSN10-8	NSN12-3	5	153311	-30.881	-20969100.	-0.00209691	0.99790529
NSN8-3	NSN16-14	21	155807	-33.951	-21053800.	-0.00210538	0.99789683
NSN16-14	NSN8-4	21	169149	-34.1943	-21510100.	-0.00215101	0.9978513
NSN8-2	NSN1-4	10	169149	-34.2561	-21510100.	-0.00215101	0.9978513
NSN12-3	NSN10-7	5	170369	-34.2798	-21551900.	-0.00215519	0.99784713
NSN10-9	NSN10-8	17	170369	-49.4068	-21551900.	-0.00215519	0.99784713
NSN10-8	NSN3-5	17	174746	-67.6039	-21847800.	-0.00218478	0.9978176
NSN3-5	NSN3-3	17	177978	-223.991	-22571700.	-0.00225717	0.99774538
NSN3-3	NSN3-2	17	181210	-388.547	-23827400.	-0.00238274	0.9976201
NSN3-4	NSN3-3	14	181210	-523.764	-23827400.	-0.00238274	0.9976201
NSN3-3	NSN3-1	14	184442	-658.981	-25957000.	-0.00259570	0.99740767
NSN3-1	NSN3-0	14	187673	-1092.06	-29486300.	-0.00294863	0.99705571
NSN3-2	NSN3-1	17	187673	-1428.45	-29486300.	-0.00294863	0.99705571
NSN3-1	ART	17	190905	-1764.84	-35189700.	-0.00351897	0.99648721
			200000	-Infinity	Infeasible		

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REPORT DOCUMENTATION PAGE

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1. AGENCY USE ONLY (Leave blank)	2. REPORT DATE	3. REPORT TYPE AND	ster's The	VERED
	March 96	IVIA		G NUMBERS
4. TITLE AND SUBTITLE	ATO MADOINIAL DETLID	NC. AN		
MODELING DIMINISHING APPLICATION TO THE	NG MARGINAL RETUR AIRCRAFT AVAILABIL	ITY MODEL		
6. AUTHOR(S)				
Wayne L. Zorn, CPT, USA	N F			
7. PERFORMING ORGANIZATION NAM	E(S) AND ADDRESS(ES)			MING ORGANIZATION NUMBER
Air Force Institute of Tech				
WPAFB OH 45433-6583			AFI	[/GOA/ENS/96M-10
9. SPONSORING/MONITORING AGEN	CY NAME(S) AND ADDRESS(ES)		10. SPONS	ORING/MONITORING Y REPORT NUMBER
AFMC/SAO			AGENC	I REPORT HOMBER
4375 Chidlaw Rd, Suite 6				
WPAFB, OH 45433-5006	5			
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11. SUPPLEMENTARY NOTES				
			112h DIST	RIBUTION CODE
12a. DISTRIBUTION / AVAILABILITY ST	ATEMENT		120. Disti	AIDO HOM CODE
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13. ABSTRACT (Maximum 200 words) The Aircraft Avail	anuity whole caalyn nio	vides the Air Force	with a w	orldwide peacetime
mayirament for reparable	snare parts. This research	n models AAM me	thodology	y as it relates to the
of diminishing me	arginal returns in resource	application. Three	separate	modernig techniques
are investigated with the	goal of reformulating the	AAM as a mathema	aticai pro	analysis. The general
provides a comparable so	lution and a capable tool to	or the conduct of se	ensiuvity	analysis. The general
formulations presented he	re are continuous non-line	ear, conunuous ime	discrete/	continuous model are
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presented. The piecewise	linear model based on A/	AM sort values sho	The ni	ecewise linear model
optimization routine relat	ive to the AAM shopping	movimize the miss	ion desig	n series (MDS)
based on availability rates	s provides the capability to	ighast possible MT	gieva 201	hility relative to
availability level. It has t	he potential to obtain the hy levels. This mathematic	of model is giscussing mr	ed in com	plete detail as a robust
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platform for conducting e	extensive post-optimality a	ilarysis.		
14. SUBJECT TERMS				15. NUMBER OF PAGES 131
Reparable Spares; Aircra	ft Availability; Linear Pro	ogramming		16. PRICE CODE
CONTRACTOR IN	8. SECURITY CLASSIFICATION	19. SECURITY CLASSIF	ICATION	20. LIMITATION OF ABSTRAC
17. SECURITY CLASSIFICATION 1 OF REPORT Unclassified	OF THIS PAGE Unclassified	of abstract Unclassified		UL
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